UNIVERSITY OF PENNSYLVANIA
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The Moore School of Electrical Engineering

September 1, 19

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Attn: Computer & Guidance Technology Division

Dear Sir:

Enclosed are one reproducible and two duplicated copies of the final technical report, "Designer's Manual for Computer-Aided Design Control Circuits", prepared by S. D. Bedrosian and D. I. Howe under Contract NAS12-2137.

This completes the report requirements for the subject contract.

Edward L. Parker

cc: Dr. S. D. Bedrosian Mr. R. L. Keane, ONR Resident Representative Mr. A. Merritt, ORA Contract file (MS6920)

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NATIONAL TECHNICAL INFORMATION SERVICE Springfield, Va. 22151

# DESIGNERS MANUAL FOR COMPUTER-AIDED DESIGN OF CONTROL CIRCUITS

FINAL TECHNICAL REPORT

Contract NAS 12-2137

National Aeronautics and Space Administration

Electronics Research Center

575 Technology Square

Cambridge, Massachusetts 02139

Prepared by

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June 15, 1970

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#### TABLE OF CONTENTS

CHAPT	ER I	1
INTRO	DUCTION	1.
IA	REVIEW OF CODING PROCEDURES FOR NASAP	14
ΙΒ	ERROR MESSAGES	17
IC	DOCUMENTATION OF NASAP 69/I VERSION USED AT THE UNIVERSITY OF PENNSYLVANIA	20
CHAPI	ER II NASAP TREE SELECTION ALGORITHMUSER OPTIONS	36
ITA	GENERAL DESCRIPTION	36
IIB	ILLUSTRATIVE EXAMPLE	38
IIC '	THE OPTIMUM TREE	<u> </u>
CHAPT	ER III MODELING A CONTROL SYSTEM FOR NASAP	63
IIIA	GENERAL DISCUSSION OF CONTROL SYSTEMS	63
IIIBl	Equivalent Electrical Networks for Transfer Functions	65
IIIB2	Cascade Interconnection of Transfer Function Models	68
IIIC	ADDITIONAL EQUIVALENT NETWORK MODELS	69
IIIC1	Use of Negative R, L or C	69
IIIGS	Illustrative Examples	74
IIID	MODELS OF FEEDBACK CONTROL SYSTEMS	78
IIDl	Examples of System Models	78
IIID2	Control System Model and its Step Response	<b>7</b> 9
CHAPTI	ER IV CONTROL SYSTEM ANALYSIS IN THE FREQUENCY DOMAIN	85
IVA	ANALYSIS OBJECTIVES	85
IVB	BODE AND ROOT LOCUS PLOTS	90
IVC	USE OF COMPENSATION	101

CHAPI	ER V CONTROL SYSTEMS ANALYSIS IN THE TIME DOMAIN	126
VA	INPUT SIGNALS FOR TIME RESPONSE	126
<b>V</b> B	ADDITIONAL INPUTS FOR CONTROL APPLICATIONS	127
AG	ERROR ANALYSIS	140
VD	FIGURES OF MERIT BASED ON ERROR SIGNAL	152
CHAPI	ER VI SENSITIVITY ANALYSIS	156
AIV	INTRODUCTION TO SENSITIVITY	156
VIB	DERIVATION OF SENSITIVITY FORMULAS	158
AIG	DISCUSSION OF SENSITIVITY FORMULAS IN SENS	160
AID	DISCUSSION OF REVISED SENSITIVITY SUBROUTINE	164
VIE	ROOT SENSITIVITY	168
VIF	EXAMPLES	170
CHAPT	ER VII SPECIAL CONTROL SYSTEM EXAMPLES	21.0
VIIA	EXAMPLE INVOLVING TIME DOMAIN APPROXIMATION	211
AIIB	EXAMPLE OF A CONTROL SYSTEM WITH TRANSPORT LAG	220
AIIC	EXAMPLE SHOWING NASAP LIMITATION	229
VIID	EXAMPLE INVOLVING LUENBERGER OBSERVER	239
REFER	ENCES	246
APPEN	DIX A	249
APPEN	DIX B	252

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CHAPTER I

This manual describes the necessary preliminary electric circuit modeling and methods of computer analysis using the NASAP digital computer program to aid in the design of control circuits used in aerospace systems. The scope of design treated is limited to single-input single-output linear time invariant control systems that can be described by rational transfer functions.

Two different approaches can be followed in the design of such linear time invariant feedback control systems. In one case the designer seeks compensators for a given plant to satisfy the over-all system requirements. This approach generally involves cut and try and the well known conventional design techniques such as the Bode and Nyquist plots and use of the root locus. In the other case, the designer starts by obtaining the over-all transfer function from the given plant and the specifications. He is then in a position to determine the required compensators. The second of these two approaches seems more amenable to computer-aided design of control circuits using the NASAP program.

NASAP is an acronym for Network Analysis for Systems Applications Program. NASAP has been developed and is being maintained by the Automated Techniques Branch, NASA Electronics Research Center, Cambridge, Massachusetts. The NASAP Program is based on Mason's signal-flow graph [MA-1] as extended by Happ for the closed signal-flow graph [HA 1]. The program is based upon symbol oriented techniques which with proper tagging and loop evaluation permit both the transfer function and the sensitivity to be made available.

This chapter provides brief discussions on the basic options presently available in the NASAP program and the basic procedures used in computer aided design of control circuits.



The NASAP Program

NASAP is a linear electrical circuit analysis program which computes a specified transfer function in terms of the complex frequency variable, s.

The basic coding rules and description of the program are contained in the booklet "Coding Instructions for NASAP 69/I" by Gaertner Research Incorporated [GA 1]
written under NASA contract NAS 12-663. A number of special options are introduced and described later in this manual. The input for NASAP is by punched card
and the output is by printer tabulation of data and printer graphics. It is
worth noting that the input format of NASAP is simple and that use of this
program requires little knowledge of circuit theory or computer programming.

The present version of NASAP can handle linear circuits which consist of constant- value passive elements, and independent or dependent current and voltage sources. The dependent sources must be linearly related to a voltage or current in another part of the circuit. Nonlinear functional relationships (dependencies) and time-varying parameters cannot be handled.

Embodied in NASAP is the ability to give both a mathematical formulation and a numerical tabulation of the output results with some printer graphics.

A brief summary of the options presently available in the program available on the RCA Spectra 10/146; at the Moore School, follows:

- OUTPUT The transfer function which is specified by the user is printed out as the ratio of two polynomials in the complex frequency variable, s. The poles and zeros of the transfer function are evaluated.
- FREQ A Bode plot of the transfer function is printed in tabular and graphical form.
- 3. TIME The impulse response of the network is printed in tabular and graphical form. To facilitate control circuit design we

- have also made available the step and ramp responses.
- 4. SENSITIVITY The sensitivity of the transfer function is computed with respect to a designated element in the network. Furthermore the program can print out in numerical form: the sensitivity of the real part of the transfer function, of the imaginary part of the transfer function, of the magnitude of the transfer function, and of the phase of the transfer function to changes in specified circuit parameters.

Details of these options are documented in Section ID.

## Precedures Used in Computer Aided Design

The major steps in computer aided circuit design are:

- a. Choose the electrical circuit model for the control system.
- b. Calculate element values from design equations.
- c. Analyze circuit using computer.
- d. Change element values if computer analysis results in discrepancies between the electrical circuit model response and desired control circuit response.

Before a control system can be analyzed using NASAP and before the necessary compensation can be determined, the plant's dynamic characteristics must be first simulated by an electric network which has an equivalent dynamic characteristic. The choice of circuit models is based on the specified response for the control circuit. Details of circuit modeling are given in chapter III. Computer analysis is amply demonstrated in chapter IV.

# IA REVIEW OF CODING PROCEDURES FOR NASAP

NASAP is a computer-aided electrical circuit analysis program which can be used by engineers without knowledge of computer programming. Using NASAP to analyze a circuit it is possible to calculate a transfer function, the sensitivity of the transfer function, the frequency response, and the impulse response. The main steps for preparing NASAP computer instructions are

- a) Obtain an electrical circuit model for the control circuit
- b) Preparation of the circuit diagram in a form from which all the information required by the computer can be readily extracted.
- c) The preparation of the computer instructions themselves.

  The first step will be discussed in chapter III. The second step has been decribed elsewhere [GA 1] and will be illustrated by many examples throughout this manual. The third step will be reviewed in this chapter for the convenience of the reader. For additional information, see [GA 1]. The coding rule will be presented by an example taken virtually unchanged from [MO 1].

  Example REC Filter

We shall analyze the RLC filter shown in Fig. 1.1(a) to find its open circuit transfer voltage function.

## Numbering the Nodes and Elements

The first step in preparing the circuit for NASAP analysis is to number the circuit nodes and elements. The nodes must be numbered sequentially, starting with 1, without skipping any numbers.

The second step is numbering all circuit elements (resistors, capacitors, inductors, and current and voltage sources) consecutively within each category i.e., R1, R2, . . . , L1, L2, . . . , C1, C2, etc. No two elements can have the same number designation regardless of their component values. One

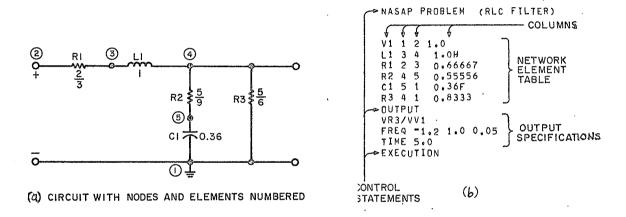


Fig. 1.1: RLC Filter Network and the Corresponding NASAP Input Instructions

possible set of number assignments for the RLC filter is shown in Fig. 1.1(b).

#### - Overall Appearance of Input Instructions

Figure 1.2 shows the general appearance of the input instructions. The instructions fall into three different categories: a) Control Statements,
b) Network Element Table, and c) Output Specifications. Each type of instructions will be explained briefly below.

#### Control Statements

The first line of the set of instruction must start with the word: NASAP which simply indicates the beginning of a circuit description. The letter N must be in the first column of the card. The word NASAP may be followed by any identifying information but only the first 50 columns of the card will be printed by the computer.

The end of the network element table is designated by the control card with the word: OUTPUT on it. Following the OUTPUT control card are the output specifications. The final control card appearing after the output specifications is the card with the word: EXECUTION.

This card signals the end of the description for the problem and starts the computer on the task of analysis. If it is desired to analyze several problems in one run, the EXECUTION card can be followed by another NASAP card, etc.

#### Network Element Table

#### General Format

The network elements and topology are described in a five column network element table. (Note that the example in Fig. 1.2 has only four columns since no dependent generators are used.) A brief description of each column follows:

- Column 1: Identifies the element itself, i.e., V1, R3, etc.
- Column 2 and 3: Define the nodes between which the element appears. The positive current direction is always from the first to the second node. Thus, for passive elements the first node is assumed positive with respect to the second, and for active elements the second node is assumed positive with respect to the first.
- Column 4: Contains the value of the circuit component.
- Column 5: Used only for dependent sources and will be described in detail later.

## Input Voltage or Current

The first line after the NASAP control statement contains a description of the applied voltage or current. For example, the statement V1 1 2 1.0 in Fig. 1.2 indicates that V1 is a voltage of magnitude 1.0 applied between nodes 1 and 2 with node 2 being positive. The fourth column contains the value of the generated current or voltage and is usually set to 1.0. If any other value is used, it will act as a constant multiplier for the transfer function under consideration.

#### Resistors, Capacitors and Inductors

Resistors, capacitors and inductors are identified in column 1 by the letters R, C, and L, respectively. The letter is immediately followed by a one or two digit integer indicating the element number. The fourth column contains the component value. The value is a number followed by up to two letters which denote a multiplying factor according to the convention given in Table (1)1. The network element table in Fig. 1.2 follows directly from the circuit diagram of Fig. 1.1 (b).

Table 14.1. Units Following the Component Values

Letters Used in NASAP	Electrical Units	Multiplying Factor
No letter	Ohms	1.
K.	Kilohms	10 <b>3</b>
M.	Megohms	106
F	Farads	ı~";
UF	Microfarads	10-6
PF	Picofarads	10-13
H	Henries	1
MH	Millihenries	10-3
UH	Microhenries	10-46

#### Output Specifications

Once the electrical circuit model of the control system has been described, we need to specify what we want calculated. This specification always starts with a transfer function.

#### Transfer Function

The transfer functions are always specified as a ratio of the voltages across or current through a circuit element at the network output over the input voltage or current. The input voltage or current are specified by the letters VVI or III respectively and either one must appear in the denominator of the transfer function specification. For example, VR3/VVI used in Fig. 12 implies that we want to calculate the ratio of the voltage across R3 to the input voltage VI, i.e., the open circuit transfer voltage function. Since R3 was defined by the statement

R3 4 1 0.8333

node 4 is assumed to be positive with respect to node 1. If R3 has been defined by

R3 1 4 0.8333

the sign of the transfer function would be negative.

When the program is executed using the circuit description shown in Fig. 1.2 and the transfer function specification, the computer generates the output shown in Fig. 1.3. The first information printed under the heading "NUMBER OF LOOPS FER ORDER" describes the complexity of the circuit flowgraph by indicating the number of first order loops, the number of second order loops, etc. This information is only of theoretical interest and can usually be ignored during design. However, since the program prints this data, it will always be included for completeness.

#### Dependent Current and Voltage Sources

NASAP permits use of any of the four possible types of dependent generators (also known as controlled sources):

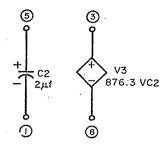
- a) voltage controlled voltage sources (VCVS)
- b) current controlled current sources (ICIS)
- c) voltage controlled current sources (VCIS)
- d) current controlled voltage sources (ICVS)

Each dependent generator involves two pairs of nodes and two elements: the dependent generator itself and a <u>passive</u> element which defines the controlling voltage or current. An example of each type of dependent source taken from [MO 1] is shown in Fig. 1.4. The node numbers are chosen to indicate that they are elements in a larger circuit and the dependent source is indicated by a diamond to distinguish it from an independent source which will be represented by a circle.

A description of the NASAP coding for dependent generators is in order. The VCVS shown in Fig. 1.4(a) is specified in NASAP by the instructions found immediately below the figure. The first instruction specifies a dependent voltage source, V3, from node 8 to node 3 (node 3 positive). The value of the source is 867.3 times the voltage across capacitor C2. The

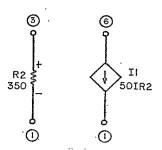
```
NUMBER OF LOOPS PER ORDER
  1 = 5
2 = 4
TRANSFER FUNCTION VR3/VV1
               ( 5.00E 00 +1.00E 00 S )
H(S)= 3.333E=01+=====
               ( 3.00E 00 +3.00E 00 S +1.00E 00 S )
ZEROS OF TRANSFER FUNCTION
ZEROS REAL PART IMAG. PART
  1 ".50000E 01 0.
POLES OF TRANSFER FUNCTION
POLES REAL PART IMAG. PART
  1 -.15000E 01 -.86599E 00
  2 -.15000E Q1 .86599E 00
```

Figure 1.3. Transfer Function for RLC Filter



V3 8 3 876.3 VC2 C2 5 1 2.0 UF

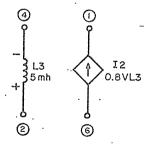
(a) VCVS



I1 6 1 50 IR 2

: R2 3-1 350 .

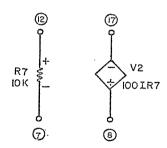
(b) ICIS



L3 2 4 5.0MH

I2 6 1 0.8 VL3

(c) VCIS



R7 12 7 10K

V2 17 8 100.IR7

(d) ICVS

Figure 1.4.

Examples of the Four Types of Dependent Generators and the Corresponding NASAP Instructions second instruction specifies a capacitor from node 5 to node 1 of 2.0µf. Thus node 5 of the capacitor is assumed positive as noted in Section: Network Element Table, page 1.4. The polarity of the passive controlling element will always be shown on the circuit diagram to help insure that the nodes will be numbered in the correct sequence since the passive element may appear far from the controlle source in the network element table.

Similarly the ICIS shown in Fig. 1.4(b) is specified by the instructions below it. That is, a current source, Il, from node 6 to node 1 with a value of 50 times the current flowing through R2. R2 is defined so that node 3 is assume positive and thus the current is assumed to flow from node 3 to node 1.

The corresponding NASAP instructions for the VCIS shown in Fig. 1.4(c) and the ICVS shown in Fig. 1.4(d) are written to indicate that it does not matter whether the dependent generator or the passive controlling element is specified first in the network element table.

#### Sensitivity

The NASAP program is capable of determining the sensitivity of the transfer function to changes in the value of any single element. The request for a sensitivity analysis is optional and, if it is desired, is specified following the transfer function specification. This has the typical form:

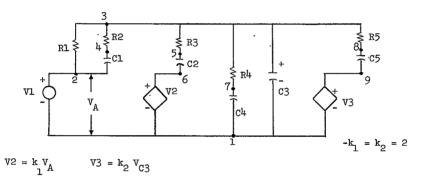
## VR11/VV1/L3

This output specification requests the sensitivity of the transfer function VR11/VV1 with respect to element L3.

The frequency range over which the sensitivity is analyzed is the same as that for which the frequency response is calculated so they are both defined in the same output specification. For the RLC filter of Fig. 1.1, Moe [MO 1] tabulates and displays the response for FREQ -1.2 I.O 0.05.

#### Further Discussion of Dependent Sources

As stated in Gaertner's Coding manual, dependent sources can be related only to the voltages or currents of <u>passive</u> elements of the flowgraph. However, the controlling current or voltage in the circuit may be that of an active element. Such a situation is illustrated in Fig. 1.5 by the circuit realization for a normalized three-pole low-pass Chebyshev transfer function.



Desired Transfer Function: VC3/VV1

# Fig. 1.5

This circuit is an application of a general circuit introduced by Cooper and Harbourt [CO-1]. Note that the controlling voltage, VA, of the dependent source V2, is the independent voltage source V1. However if the following card

where  $k_1 = -2$ 

is included in the input list, the error message

INPUT CODING ERROR IN COLUMN 12

will result. The error is the second letter V since the program in only searching for the letter R, L, or C.

However, this difficulty is easily resolved by connecting a resistor R6 across the terminals of V1 (i.e., between nodes 2 and 1) and by making the voltage source dependent on the current through R6. The current through R6 (IR6) equals V1/R6.

Thus V1 = (R6)IR6. Since  $V2 = k_1 V1$ , then

$$V_2 = k_1 \cdot R6 \cdot IR6$$

Thus the dependency value between V2 and IR6 is  $k_1 \cdot R6$ . Note that R6 can have any nonzero numerical value. If, as is the case in this example, R6 is chosen to have a value of 4 ohms, input list must include the following two cards;

The presence of this extra resistor neither increases the complexity of the flowgraph by generating additional loop sets nor does it affect any of the electrical properties of the original network.

This can be seen by comparison of Figs. 1.6 and 1.7. Fig. 1.6 is a partial flowgraph for the original network in Fig. 1.5.: Fig. 1.7 is a partial flowgraph for the addition of R6 to the network.

Note that in both Figs. 1.6 and 1.7 There is only one path from the voltage node of VI to the voltage node of V2.

The computer results for the circuit in Fig. 1.5 are given in Figure 1.8.

A similar procedure is followed when a dependent source is a function of the current of a current source. In this case a resistor  $R_{\rm s}$  is added in series with,

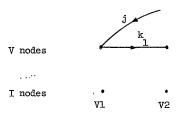
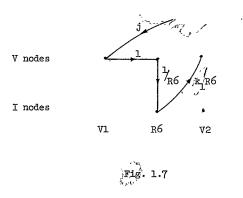


Fig. 1.6\_



the current source. The dependent source is then made a function of the voltage across this resistor—the dependency value being  $k_1/R_{\rm S}$  where  $k_1$  is the dependency value between the dependent source and the current source. As in the previous case addition of this resistor to the network under consideration, will in no way affect the flow graph or the electrical properties of the original network.

NASAP PROBLEM COOPER AND HARBOURT CCT		
HERTZ .	<u></u>	«. • ، ښار
HERTZ NONE		
VI 1 2 1.		<del></del>
R1 2 3 4.08 C1 2 4 .1228F		
V2 1 6 - 8 IR6	\ <del>\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\</del>	
72 1 0 - 6 180 C2 6 5 . 2455F R3 5 3 4.08		
C3 3 1 1F R4 3 7 1.95		
C4 7 L .5125F V3 1 9 2 VC3	•	
75 1 7 2 V 3 75 9 8 1,63F NUMBER OF LOOPS PER ORDER		^
R6 2 1 4		
OUTPUT 1= 13 VC3/VV1 2= 35 FREQ -2, -0.75 .01 3= 37		
EXECUTE 4= 16 5= 2		
-		
. /ø³		
TRANSFER FUNCTION VC3/VV1		
TRANSFER FUNCTION VC9/VV1		
2		
( 4.92E 03 +7.39E 03 S +2.47E 03 S +1.00E 00 S )		Ψ.
H(S)= 1.984E-04*		
( 9,77E-01 +3.93E 00 5 +6.16E 00 5 +6.19E 00 5 +3.98E 00 5 +1.00E 00 5 }		
. ( 9.77E-01		
		, <u></u>
ZERO OF TRANSFER FUNCTION POLE OF TRANSFER FUNCTION		
ZERO REAL PART IMAG, PART POLE PEAL PART IMAG, PART		-
1 -0.10006E 01 0.00000E 00 1 -0.2476IE 00 0.96444E 00 2 -0.19984E 01 0.00000E 00 2 -0.2476IE 00 -0.96444E 00		÷.
3 -0.246216 04 0.00000E 00 3 -0.99910E 00 0.00000E 00 4 -0.49402E 00 0.00000E 00		
5 -0.19957E 01 0.00000E 00		
	مراتي سموتيو	
•		

Figure 1.8

# IB ERROR MESSAGES

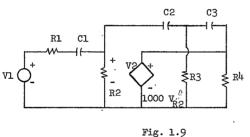
Here are provided a few comments on the meaning of selected error messages available in NASAP.

In subroutine GETCON, there are two error messages.

The message

ALGORITHM FAILURE REVIEW CIRCUIT CODING RULES

usually occurs when the NASAP program is unable to select a legitimate tree from the available resistors or capacitors. This case exists when the candidate type 1 or 2 elements form an R or C loop or when all elements connected to a node are type 6 or 7 elements; i.e., these excluded elements from a cut set. If, for example, the transfer function VR4/VV1 is desired for the circuit in Fig. 1:9.



V2 = 1000 VR<sub>2</sub>

then the above error message will be printed out. This is necessitated by the loop formed by the elements V2 and R4 which must be in the tree. This difficulty can easily be resolved by calling for the transfer function VV2/VV1 which is identical to VR4/VV1.

The other error message is

FLOWGRAPH HAS TOO MANY CONNECTIONS EXECUTION TERMINATED

The connections of the primitive flowgraph are stored in the two dimensional connection matrix LCONC. The size of this matrix is such that it is assumed that no more than nine (edges) branches will emanate from a single flowgraph node. Thus if ten or more branches must emanate from a node, the above error message will be printed and execution stopped. This limitation is completely arbitrary and exists to restrict the size of the matrix LCONC. If one wishes to increase the maximum number of node connections, then the number 10 which appears twice on lines 4010, 5460, and 6220 and which appears once on line 5110 should be changed to a suitable integer N which is defined as the maximum number of node connections (M) plus one. Also the numeral 9 on line 6250 should be changed to the integer M. When these changes are made, the above error message will result when the number of node connections exceeds M instead of when the number of connections exceeds nine.

In subroutine FSORL, there is the error message

FLOWGRAPH FIRST ORDER LOOPS EXCEED 927.

This limitation on the actual loops of the flowgraph, the so-called first order loops, is completely arbitrary. It is necessary to store the first order loops since the higher order loops are determined from these first order loops. However, if this error message is printed out, it usually means that the tree selected was a rather poor choice. A more complete explanation of tree selection to minimize the number of loops of a flowgraph will be given later.

In subroutine BODE the error message is

PROGRAM RESTRICTS GRAPH TO 250 STEPS.

The subscript for the evaluation of the transfer function at various frequencies cannot exceed 250. Thus, if the information on the FREQ input card results in more than 250 frequency evaluations, the NASAP program will not perform any of the calculations included in subroutine BODE including the sensitivity calculations (if this has been called for). The program will jump to the time response calculation if this has been called for. Otherwise, execution will cease after the above error message.

In subroutine SENS there is the error message

SENSITIVITY PLOTS RESTRICTED TO 120 POINTS.

If the input information on the FREQ card results in more than 120 frequency points, the sensitivity results in tabular form will be printed out. However the 3-curve plot and the phase sensitivity plot will be deleted.

At present, extensive diagnostics and debugging capabilities are lacking. Input data can be written on a field-free format, and a circuit tree selection need not be specified by the user since it is done internally by the program. As is sometimes the case, when a proper tree cannot be found, a message is printed out indicating the difficulty and where it occurs in the circuit. Detailed discussion of the tree selection algorithm is found in Chapter II.

IC DOCUMENTATION OF NASAP 69/I VERSION USED AT THE UNIVERSITY OF PENNSYLVANIA

Summary

This section details the differences in input data and output results of the University of Pennsylvania version as compared to the standard NASAP 69/I as described in the Gaertner coding manual. [GA-1]

Input Cards

The NASAP version used at the Moore School of Electrical Engineering in the University of Pennsylvania (hereafter called the MSE-NASAP version) requires the user to supply two additional data cards immediately after the first data card (the NASAP PROBLEM card). The first of these cards indicates the frequency units to be used in the evaluation of the transfer function. There are four permissible entries for this card (starting in column 1)

RADIANS

HERTZ

CYCLES PER SECOND

NONE

Only the first two letters (those underlined) must be correct since the NASAP program checks only these letters. Any other information can be included on this card since the program evaluates only the information contained in columns 1 and 2.

The second card indicates the type of time response desired by the user. There are four choices (starting in column 1)

IMPULSE RESPONSE

STEP RESPONSE

RAMP RESPONSE

NONE

The programs again only evaluate the data in columns 1 and 2.

Table 1.2 shows the input Tisting necessary on the MSE-NASAP version to find the step response for the circuit of Fig. 1.10. The response is the voltage across C1 and the excitation is a step voltage with a magnitude of 3 volts. The BODE plots of the specified transfer function are not being requested.

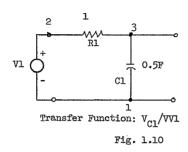


Table 1.2.

NASAP PROBLEM

NONE

STEP RESPONSE

V1 1 2 3.

R1 2 3 1

C1 3 1 0.5F

OUTPUT

VC1/VV1

TIME 2.0

EXECUTE

#### Printed Output Results

The MSE-NASAP version prints out much data on the primitive flowgraph which is used within the computer to determine the user-specified transfer function. The additional output data is printed between the printed listing of the input data cards and the NUMBER OF LOOPS PER ORDER table--both of which are printed by the standard NASAP package.

As an example, Fig. 1.11 gives printed output of a legitimate input listing for circuit 6 introduced in Hutton's report. [HU 1] Fig. 1.12 gives the 5 computer sheets of additional data printed out by the MSE-NASAP version based on the listing of Fig. 1.11. On the sheet immediately following the input list sheet are printed two matrices. The first matrix is the compressed cut set matrix. This matrix has (b + 2) rows and (l + 2) columns where

b = number of branches in the tree = n - 1

n = number of nodes in circuit

· 1 = number of links in the co-tree

It must be recalled that

$$b + 2 = \lambda$$

where  $\lambda$  is the number of elements in the circuit (For the circuit described in Fig. 1.11,  $\lambda$  = 30 and n = 15). This matrix is useful in that it shows which circuit elements have been selected as tree branches by the NASAP tree-selection algorithm.

As each circuit element is inputted, it is assigned an integer flag (beginning with unity). Thus for the circuit listing of Fig. 1.11.

	•	
NONE		÷
NONE		``
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V1 1 2 1.		•
R6 7 1 390		
R15 8 1 25 R1 2 3 6.9K		•
R2 3 4 6.8K		
R3 4 5 100		
R4-5 6 100K	•	
R5_5_7_1.00		
R7 6 1 1.2K.		
R8 9 1 100⊀ R9 9 7 100		
R10 10 9 100		
R11 10 12 6.4K		
R12 12 11 6. K		
R13 13 1 3.6K		
R14 6 8 TOT	<del></del>	<del> </del>
R16 8 11 10(K		
R17 11 1 1K C1 3 1 50F		
C2 4 6 .035' 5		
C3 10 1 .Cu3UF		
C4 10 12 16:12		
C5 13 11 100-1		•
Cb 12 1 20 b	<del> </del>	
07 6-11 -6120F 11 6 5 100 123		
12 1 9 100 1810		
13:11 8 100 1214		
V2 1 14 1.0 V47		
V3 1 15 1.0 VS13		
OUTPUT -		-
VR17/VV1 EXECUTE		
1/20012		
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		Fig. 1.11
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#### COMPRESSED CUTSET I/ [+1]

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#### FLOWGRAPH CONTECTION MATRIX

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11 12.

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8 16 25 29

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Element	Integer Flag
ΔŢ	1
R6 -	2
R15	3
•	•
•	•
•	•
V3	30

An element in the compressed outset matrix can have one of three values -1, 0, or +1. The top and bottom rows and the left-most and right-most columns of the compressed cutset matrix are used for identification purposes described in the following paragraphs.

The non-zero entries in the left-most column are the integer flags of those circuit elements which have been selected as tree branches. The corresponding entry in the right-most column gives the tree hierarchy value of the circuit element (see description of tree-selection algorithm). Hence in Fig. 1.12 we see that Vl(flag = 1) and R7(flag = 9) are tree branches and both have a hierarchy value of 2.

Similarly the non-zero entries in the top row are the integer flags of the circuit elements that are links of the co-tree. The bottom row gives the hierarchy value of these elements. For instance, R1(flag = 4) and R2(flag = 5) are links of the co-tree and have hierarchy values of 4.

The information contained in the compressed cutset matrix is used to develop the flowgraph connection matrix which is a mathematical description of the primitive flowgraph. This matrix consists of  $\lambda$  (= number of elements) rows. The entries in the left-most column represent either the voltage node or the current node of the circuit elements (depending upon whether the elements are branches or links respectively) identified by the integer flags numbered consecutively from 1 to  $\lambda$ .

If the left-most entry of a particular row of the flowgraph connection matrix represents a voltage node of an element, then each of the other entries of this row indicates a connection from the voltage node of the left-most entry to the voltage node of the corresponding entry. There is one exception—if one of these entries refers to a voltage controlled current source, then there is a connection from the voltage node of the left-most entry to the current node of this particular entry. Conversely, if the left-most entry of a particular row of the flowgraph connection matrix represents a current node of an element, then each of the other entries of this row indicates a connection from the current node of the left-most entry to the current node of the corresponding entry. There is one exception—if one of these entries refers to a current controlled voltage source, then there is a connection from the current node of the left-most entry to the voltage node of this particular entry. A few examples from Figure 1.12 will clarify this description. The second row of the flowgraph connection matrix in Figure 1.12 contains

From the cutset matrix it is seen that the element with integer flag 2 (i.e. R6) is a tree branch. Thus there are two connections (with a value -1) from the voltage node of R6 - one to the voltage node of R5(flag = 8) and the other to the voltage node of R9(flag = 11). The zero indicates the end of the row.

As a second example, the fifth row of this connection matrix contains

Since R2(flag = 5) is a link in the co-tree, there is a connection with a value of +1 from current node of R2 to the current node of R7(flag = 9). Also there is a connection (value = -1) to the current node of C1(flag = 19) and one (with value = -1) to the current node of C2(flag = 20). Use of Ohm's Law yields the passive element (R,L,C) joining the voltage and current nodes, since the voltage across an element is related to the current flowing through the element by means

of the element's impedance.

The next printed output consists of all the closed loops (first order loops) contained in the flowgraph determined by means of the flowgraph connection matrix. The heading of this output block of data is

#### FIRST ORDER LOOPS BY CONSECUTIVE LOOPS

Each loop is defined by the nodes contained in the loop. This output shows the order in which the nodes have been found by NASAP for each loop. Each loop is given an identification integer starting with unity. This identification integer is shown in the left-most columns. The remaining integers in a given row refer to the integer flags of the circuit elements.

In Figure 1.12 we see that the flowgraph under discussion has a total of 102 first order loops. Let us examine one of these loops more closely--say loop 81 defined by

The first and last integers are always identical since it is the starting point of the loop. From the input listing we have

Element		Integer	Flag
R3		6	
Il	•	26	
R <sup>1</sup> 4		7	

Each loop is found by the path-finding procedure on the flowgraph connection matrix (for details see the Potash-McNamee User's Manual). From the cutset matrix we note that R4 is a tree branch while Il and R3 are co-tree links.

To illustrate this we now show how this loop 81 can be found from the flow-graph connection matrix. Start at the current node of R3 (R3 is a link). There is a connection from this node to the current node of the current source I1 (i.e., an integer 26 in row 6 of the connection matrix). There is a connection from the current node of I1 to the current node of R4 (i.e., an integer 7 in the 26th

row of the connection matrix). Since R4 is a passive element, there is a connection (with a value = R4) from the current node of R4 to the voltage node of R4 (recall that R4 is a tree branch). From the 7th row of the connection matrix (integer flag of R4 = 7) we observe that 6 is an entry. Thus there is a connection from the voltage node of R4 to the voltage node of R3 (with a value of -1). Since R3 is a passive element that is a co-tree link, there is a connection (with value = \frac{1}{R3}) from the voltage node of R3 to the current node of R3 (the starting point)--thus completing the loop.

The higher order loops, the sets of non-touching first order loops, are easily found by assigning each first order loop an integer value based upon the nodes contained in the loop (each node is identified by the circuit element integer flag). This integer value is stored in the one-dimensional array LOOP defined by

LOOP(J) = 
$$\sum_{k=1}^{M_k}$$
 2  $|^{N_k}|$  -1

where J is the loop identification integer

 $N_{\mathbf{k}}$  refers to the kth flowgraph node in the Jth loop

n = number of flowgraph nodes in the Jth loop

As an example, for the loop numbered 79 in Fig. 1.12, we have

LOOP(79) = 
$$2^{|-6|-1} + 2^{|7|-1} = 2^5 + 2^6$$

$$= (96)_{10}$$

$$= (110000)_0$$

(Note: see Potash-McNamee Manual for details of how higher-order loop are found by use of the array LOOP).

Finally the sheet with the heading

ORDER OF LOOP

LOOP NUMBERS

is printed out to assist the user in locating the point of termination if the number of flowgraph loops is so large that the allowable computer time is used up before completion of the analysis.

The information of this sheet is presented in this manner:

- Every 50th second order loop is printed out with the identification integers of the first order loop comprising the second order loop.
- When the number of some jth order loop (j = 2,3,4,...) equals 500, the number of all loops of all order at this point of the loop enumeration procedure. (Note: see the Potash-McNamee Manual for details of the HIGORL subroutine which determines the higher order loops from the first order loops).

From Figure 1.12 we see that the output data

2 18 88

is the fourth of this type in the output data. Consequently the second order loop consisting of loop 18 and loop 88 is the 200th second order loop found by the NASAP subroutine called HIGORL. (Note: from the list of first order loops, loop 88 consists of nodes 10 and 12 which do not appear as nodes in loop 18). Immediately following this line of output, we observe that the number of 9th order loops found by NASAP equals 500. When this occurred, NASAP had found 209 2nd order loops, 987 3rd order loops, etc.

It should be noted that, if a flowgraph has less than 50 second order loops and the number of each of the nth (n = 3,4,5,...) order loops of this flowgraph is less than 500, only the heading

ORDER OF LOOP

LOOP NUMBERS

will be printed in the MSE-NASAP version.

In order to find all the higher order loops and at the same time to avoid repeating any of these loops, the HIGORL subroutine selects each first order

loop in order of its identification integer and determines all the higher order loops formed by this selected first order loop and those loops having identification integers greater than that of the selected loop (see Potash-McNamee manual for details).

With this procedure in mind, we can use the higher-order loop data printed out by the MSE-NASAP version to determine approximately where the HIGORL subroutine was in the higher order loop finding process if execution is terminated before the desired transfer function is obtained. This will enable the user to determine whether the problem should be executed with a longer running time specified or should be cancelled since the generated flowgraph is too complicated (with regard to running time) for the computer in use.

As an example, let us assume that the printed output of Figure 1.12 ended with the line

2 68 88

There was no sheet with the heading

## NUMBER OF LOOPS PER ORDER

and no sheet listing the specified transfer function. From the list of first order loops, we see that this flowgraph contains 102 loops. From the above output line, we see that the loop under selection by HIGORL is the loop numbered 68. In other words, when this line was printed loops 69 through 101 have not yet been selected as the starting loop in the higher order loop finding process.

Since the number of higher order loops generated by the starting loop decreases as the identification integer of the starting loop increases, knowledge that loop 68 (in a group of 102 loops) is the present starting loop enables the user to decide whether or not to rerun the problem. It must be noted that the last line printed does not mean that this was the last loop set found by the HIGORL subroutine before termination. It is possible that as many as 49 more

2nd order loops and many more nth (n = 3, 4, 5...) order loops have been found since the printing of the last output line and before the termination.

Following this output data, the output results of the MSE-NASAP version conform with the output data of NASAP 69/I. One remaining minor difference is the order of the sensitivity output data.

The order for NASAP 69/I is:

Table of Sensitivities of ReH, [mH], [H], Phase H as a function of frequency.

- 2. Table of the Logarithm of the above sensitivities as a function of frequency.
- 3. Plot of 3 Sensitivity Expressions.
- 4. Plot of the Logarithm of the Sensitivity.
- 5. Table of the Sensitivity Function as a function of frequency.
- Plot of the Logarithm of the Absolute Value of the Sensitivity function.
- 7. Plot of the Phase of the Sensitivity Function.
- 8. Pole and Zero Sensitivities.

On the other hand, the order of the MSE-NASAP version is:

- 1. Table of Sensitivity Function as a function of frequency.
- 2. Plot of Logarithm of Absolute Value of Sensitivity Function.
- Plot of Phase of Sensitivity Function.
- 4. Table of Sensitivities of ReH, ImH, [H], Phase H as a function of frequency.
- 5. Table of Logarithms of the above sensitivities as a function of frequency
- 6. Plot of 3 Sensitivity Expressions.
- 7. Plot of the Logarithm of the Sensitivity of the Phase H.
- 8. Pole and Zero Sensitivities.

#### CHAPTER II

#### NASAP TREE SELECTION ALGORITHM--USER OPTIONS

# IIA GENERAL DESCRIPTION

Although the graph representation of an electric network usually has a large number of possible trees (i.e., a structure containing n-1 branches which interconnect the n nodes of the circuit without forming any closed paths), NASAP has an algorithm that selects only a particular tree configuration. This tree is the basis for subsequent circuit analysis.

Each electrical circuit element is assigned a Type number as shown.

Independent voltage source	1.
Dependent voltage source	2
Capacitor	3
Resistor	4
Inductor	5
Dependent current source	6
Independent current source	7

Elements of type 1 and 2 are always included in the tree while type 6 and 7 elements are never included in branches of a tree. If there are not enough elements of type 1 and 2 to form a tree, a search is made of type 3 elements (i.e. capacitors) starting with the first capacitance listed in the input data and working down the input list. If a tree is still not found after searching through all the type 3 elements, a similar search is made of all type 4 elements (selecting those type 4 elements that do not form closed paths and neglecting those that do). If a tree does not result, a search is made of type 5 elements. If a tree is not found after this search, an error message will be printed.

The element type categories 2 and 6 need a further explanation. The elements in category 2 include not only dependent voltage sources, but also those elements

whose voltages control the voltage or current of some dependent source or whose voltage is the required output variable of input variable. For example, the following is a legal NASAP input record.

## I3 3 4 5.2 VR3

Since the voltage across resistor R3 controls the dependent current source I3, resistor R3 will be assigned element type 2 not element type 4. Also the following is a legal NASAP output record

# VL5/VV1/R2

Since the voltage across inductor L5 is the desired output variable, Element type 2 not element type 5 will be assigned to inductor L5. Similarly since V1 is the input, it will be assigned element type 2 not element type 1.

Similarly the elements in category 6 include not only dependent current sources but also those elements whose <u>currents</u> control the voltage or current of some dependent source or whose current is the required output variable or input variable.

# I3 3 4 5.2 IR3

Resistor R3 is assigned element type 6 since the current through R3 controls the dependent current source I3. In

# IC5/II2

capacitor C5 is assigned element type 6 since the current through C5 is the required output current. Also, I2 will be a type 6 element (not type 7) since it is the input variable.

Due to the search technique that reads down the input list looking for elements. to be branches of a tree, the actual tree selected by NASAP can be varied simply by rearranging the order in which the elements are placed in the input list (NOTE: There is no restriction as to the order in which the elements are listed in NASAP). However, not all of the possible tree configurations can be selected by NASAP due to the requirement that all type 1 and 2 elements <u>must</u> be included in the tree while all type 6 and 7 elements cannot be included in the tree.

### IIB ILLUSTRATIVE EXAMPLE

The complexity of the flowgraph is greatly dependent on the particular tree. By complexity is meant the number of loop sets present in the flowgraph. The values of these loop sets are used in NASAP to calculate the transfer function by means of Mason's formula as extended by Happ for the closed signal-flow graph. Since much time is consumed by the NASAP algorithms in finding the loop sets, selection of the tree that minimizes the number of loop set can save computer time as well as increase the accuracy of the coefficients of the polynomials in the transfer function.

In Fig. 2.1 is shown a transistor with known h-parameters. The input resistance of the circuit is to be calculated.

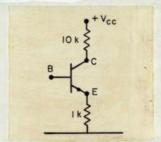


Fig. 2.1. A Common Emitter Transistor

The NASAP equivalent circuit model is given in Fig. 2.2.

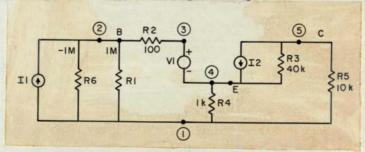
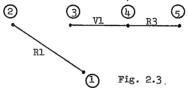


Fig. 2.2. Equivalent Circuit for Transistor in Fig. 2.1.

Il is the independent current source. Rl and R6 are positive and negative resistances of equal numberical value. These resistances, when added to the network, yield an element whose voltage equals the input voltage and at the same time does not load the circuit (the parallel connection of a positive and negative resistance yields an infinite resistance). Thus the required transfer function for the input impedance is

# VR1/II1

The network in Fig. 2.2 has five nodes; thus the tree for this circuit must have four elements. The elements R1, V1, and R3 are type 2 elements and must be included in the tree while I1, I2, and R2 are type 6 elements and cannot be part of the tree. Thus one more element must be selected to form the tree. The partially completed tree structure is shown in Fig. 2.3.



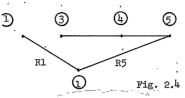
R6 cannot be used as a tree element since it forms a closed path with R1 which is an element in tree. However either R5 or R4 can be used to form a tree. Thus the NASAP tree selection algorithm will pick that resistance which is listed first in the input data. Thus if the input data is listed as follows.

II 1 2 1. 5 4 100 IR2 4 3 0.0001 VR3 Rl 2 1 lM R2 2 3 1K 5 4 40K R3 R5 5 1 10k R4 4 1 1K R6 2 1 -1M OUTPUT VR1/II1

MASAP IIT PROBLEM	with	±/M	resistors
MONE	,		
NONE			-
		<u> </u>	
T1 ·1 ·2 1. 12 5 4 100 IR2			
V1 4 3 0,0001 VR3		·····	····
R1 2 1 1M . R2 2 3 1K			
R3 5 4 40K			
R4 4 1 1K R6 2 1 -1M			
R6 2 1 -1M R5 5 1 10K			
OUTPUT VR1/II1			
EXECUTE	•		
NUMBER OF LOOPS PER ORDER	-		
1 = 9 2 = 16			
3= 4			
TRANSFER FUNCTION VR1/III			
The state of the s			
·	-		
( 1.00E 00	)		
	,		
HK('S) = 8.033E 04*		•	
( ( 1.00F 00	)		
7 1.50 12 00			
ZERO OF TRANSFER FUNCTION			
- NONE	_		
POLE OF TRANSFER FUNCTION			
NONE			
	<u> </u>		
Fig. 2.7	•		
	٠,,		
	·············		
42			

NASAP IIT PROBLEM	with	± IM resistans
NONE .	,	
- 1 Shot 1 S In		
11 1 2 1.		
<u>I.2 5 4 100 IR2</u> V1 4 3 0.0001 VR3		
R2 2 3 1K .		
R3 5 4 40K R5 5 1 10K	·	•
R4 4 1 1K		
R6 2 l -1M OUTPUT		
VR1/II1 EXECUTE		
,		
NUMBER OF LOUPS PER ORDER		
1= 14 .		
2= 29 3= 10	····	
TRESCECO CULCATON (01/YI)		
TRANSFER FUNCTION VR1/III		
( ) ( 1.00E 00 )		
H(S)= 8.033E 04*	* *************************************	
1137- 6:0336 0-4-		
( 1.00E 00 )		
<u> </u>		
ZERO OF TRANSFER FUNCTION		
NDNE		
		-
POLE OF TRANSFER FUNCTION		•
NONE .		
	<del></del>	
		-
41.		

R5 will be included in the tree elements. The chosen tree is shown in Fig. 2.4.



The output results are given in Fig. 2.5.

However, if the input listing format is given as

11 1 2 1.

I2 5 4 100 IR2

V1 4 3 0.0001 VR3

ΙK

R1 2 1 IM

R2 2 3

R3 5 4 40k

R4 4 1 1K

R6 2 i -1M

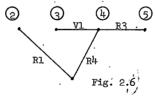
R5 5 1 10K

OUTPUT

VR1/II1

(Note that R5 is now the last element described)

Ttne tree selected by NASAP will now contain R4 as shown in Fig. 2.6.



The output results are shown in Fig. 2.7.

Note that both coding formats yield the same transfer function, as expected.

However, the tree with R4 yields a flowgraph with 29 loop sets as compared with 53 loop sets in the flowgraph obtained from the tree with R5. Thus the number of loop sets is almost halved by the proper choice of a tree for this circuit

configuration. This reduction of loop sets is apparent in the execution time.

The tree with R5, NASAP required an execution time of 24.3 seconds on the RCA

Spectra 70/46 while the execution time for the tree with R4 was 22.6 seconds, a saving of 1.7 seconds.

## IIC THE OPTIMUM TREE

There is a procedure to select the optimum tree (optimum in the sense that such a tree will minimize the total number of loops in the primitive flowgraph) that does not require a great deal of effort on the part of the NASAP user.

The details and proof of this procedure are given in reference [ZO-1]. The procedure begins by putting all type 1 and 2 elements in the tree. Next all capacitors (type 3 elements) are included in the tree. If a capacitor forms a loop with some type 1 or 2 elements, it is removed from the tree. If two capacitors form a loop with some other tree branches, then the user arbitrarily picks one of these capacitors to be a tree branch--realizing that the capacitor picked to be the tree branch must precede the other capacitor in the input lists. All type 6 and 7 elements and any element that forms a loop with the chosen tree branches are put in the co-tree. Note that if the sum of the type 1, 2, and 3 elements equals the number of nodes minus one and if these elements do not form any loops, then the NASAP tree selection algorithm will have picked a tree after a search of all capacitors. The user thus will not be able to vary the tree.

If, on the other hand, the number of resistors in the circuit is greater than the number of elements necessary to complete the tree, the NASAP user will have some flexibility in the type of tree selected by NASAP by permutting the resistor input cards.

Once the user has selected a tree, the optimum tree search procedure goes as follows:

Each link forms a loop with some of the branches of the tree. For each link, the number of tree branches in each loop is recorded as well as the specific branches that form the loop. The Branch Count is the sum of the number of tree branches in each loop. The Circuit Count is the sum of the number of loops for a specified tree branch. The Branch Count will always equal the Circuit Count. However the tree that yields a smaller Branch Count will yield a flowgraph with fewer loops.

As an example let us reconsider the input impedance circuit given above.

Recall that it was shown that V1, R1, and R3 must be included in the tree while

I1, I2, R2 and R6 must be links in the co-tree. However either R4 or R5 can be

in the tree depending on the order of the input cards. If R4 is a branch of the

tree, then there are five links in the co-tree - I1, I2, R2, R6, and R5.

The link Il forms a loop with branch Rl

The link I2 forms a loop with branch R3

The link R2 forms a loop with branches Rl, Vl, R4

The link R6 forms a loop with branch Rl

Finally, the link R5 forms a loop with branches R3, R4. Table 2.1 summarizes this information. ("Branch" refers to a tree branch.)

Table 2.1

Links	Il	12	R2	R6	R5	branch count
Branches/Loop	1	1.	.3	, 1	· _2	8
Branches		V1.	Rl	R3	R4	circuit count
Loops/Branch		1	3	2	2	8

Note that the Branch Count equals the Circuit Count, as required.

However, if R5 is made a tree branch, then the co-tree links are Il, I2, R2, R6, R4.

The link Il forms a loop with branch Rl

The link I2 forms a loop with branch R3

The link R2 forms a loop with branches Rl, Vl, R3, and R5

The link R6 forms a loop with branch Rl

The link R4 forms a loop with branches R3 and R5

Table 2.2 summarizes this information.

Table 2.2

Links	Il	IS.	R2	R6	R4	Branch count
Branches/Loop	1	1	1	4	2	9
Branches		Vl	Rl	R3	R5	Circuit count
Loops/Branch		1	3	3	2	9

Both the Branch Count and Circuit Count equal nine. Since the Branch Count for the tree containing R4 is less than that for the tree with R5, then the number of loops for the flowgraph formed from the tree with R4 will be less than that obtained from the tree with R5. As noted above, there are 29 loop sets including 9 first order loops in the flowgraph formed from the R4 tree as opposed to the 53 loop sets including 14 first order loops in the flowgraph formed from the R5 tree.

# Illustrative Example

The circuit shown in Fig. 2.8 from [MO-1] illustrates the case when different trees yield the same branch count.

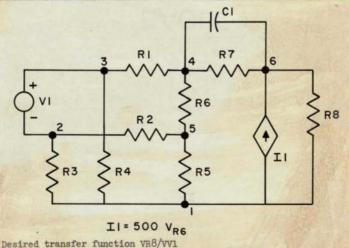


Fig. 2.8. An EOG Filter from [MO-1]

It is apparent that V1, R6, and R8 (type 2 elements) and C1 must be branches of the tree while I1, R5, and R7 must be links in the co-tree since they form loop with the above mentioned tree branches. For the six node circuit in Fig. 2.8 a tree has five branches. Since four of these branches have already been designated the last branch can be chosen from resistor R1, R2, R3 or R4. Thus four different trees can be formed by the NASAP algorithm. The question remains which of these four trees will yield the fewest loops in the flowgraph.

If R2 is selected as the fifth tree branch, then the links of the co-tree are Il, R5, R7, R1, R3, and R4. Table 2,3 gives the pertinent information on the number of branches in each loop formed by each link and the number of loops that each branch is a part of.

Table 2.3: Tree with R2

Links	Il	R5	R7	Rl	R3	R <sup>1</sup> 4
Branches/Loop	1	3	1	3	Ļ	5
Branches	V٦	R6	R8	Cl	R2	
Loops/Branch	2	4	4	4	. 3	

The Branch Count for the R2 tree is 17.

R5, R7, R1, R2, and R3. Table 2.4 gives the corresponding branch and loop information.

Table 2.4: Tree with R4

Links	Il	R5	R7	Rl	R2	R3
Branches/Loop	1	3	1.	3	5	2
Branches	Vl	R6	r8	Cl	R4	
Loops/Branch	2	2	4	4	3	

Here the Branch Count is 15. Since the branch count for the R4 tree is smaller, then this tree is a better choice than the R2 tree in terms of fewer loops for the flowgraph.

If we next let R3 be a tree branch, the co-tree links become Il, R5, R7, R1, R2, and  $R^{l}$ . Table 2.5 gives the branch and loop data for this case.

	Table 2.5:	Tree	with R3			
Link	IJ	R5	R7	R1	R2	R <sup>1</sup> 4
Branches/Loop	1	3	1	4	14	2
Branch	Vl	R6	r8	Cl	R3	
Loop/Branch	2	2	14	4	3	

Note that the branch count is 15, the same as that obtained for the  ${\tt R4}$  tree.

Finally Table 2.6 gives the branch and loop data for the case when the tree contains the element R1.

Table 2.6: Tree with Rl

Link	Il	R5	R7	R2	R3	R4
Branches/Link	1.	3	1	3	4	3
Branch	V1	Rб	r8	Cl	R1	
Loops/Branch	2	2	4	4	3	

The Branch Count for the Rl tree is also 15.

Thus three of the four trees have the same low Branch count. Thus the other criteria, the Branch product and the Loop Product, must be used to determine which of these three trees will yield the flowgraph with the fewest loops. The Loop Product, defined as the product of the number of loops involving each branch, is the same for the three trees; namely 192. However, the Branch Product, defined as the product of the number of tree branches in each loop formed by each co-tree link, is different in each case. The Branch Product is  $1 \times 3 \times 1 \times 3 \times 5 \times 2 = 90$  for the R4 tree while the Branch Product for the R3 tree is  $1 \times 3 \times 1 \times 4 \times 4 \times 2 = 96$ . The Branch Product for the R1 tree is  $1 \times 3 \times 1 \times 3 \times 1 \times 4 \times 4 \times 2 = 96$ . The Branch Product for the R1 tree is  $1 \times 3 \times 1 \times 3 \times 1 \times 4 \times 4 \times 2 = 96$ .

Note that the Branch Counts and Branch Products of both trees are equal. Since the Loop Product of the C2-C5 tree is smaller, it would seem that this tree would yield the flowgraph with the fewer loops.

However, the modified Branch count of the C3-C6 tree is smaller than that of the C2-C5 tree. This criterion indicates that the C3-C6 tree gives the fewer flow-graph loops. This, in fact, is the case as the computer results of Figs. 2.18, 2.19, 2.20, 2.21 show. The tree with C3 and C6 generates a flowgraph of 969 loops including 19 first order loops while there are 1529 loopsincluding 25 first order loops in the flowgraph formed from the C2-C5 tree.

From Dunn and Chan, [DU 1] it has been shown that the star tree (a tree in which all the branches have a common node) yields the minimum number of flowgraph loops. The more star-like the tree structure, the fewer the number of loops in the corresponding flowgraph.

In the circuit of Fig. 2.17, all of the type 2 elements are connected together at node 1. Thus 5 of the 9 branches are joined at a single node. Examination of this circuit reveals that two other elements: (R4 and R8) are also connected to node 1. If these resistors were branches of the tree, then 7 of the 9 tree branches would be connected to a single node—a tree structure that is definitely more star-like than the two trees described above. However, since R4 and R8 are resistors and type 4 elements, they are not considered for eligibility as tree branches by the NASAP tree selection algorithm until all type 3 elements (i.e. capacitors) are considered. As is shown above, the capacitors are so connected in the circuit that they do form legitimate trees (in fact, 4 trees depending upon the input listing). Thus R4 and R8, as type 4 elements, can never be tree branches. We next indicate how to overcome this problem.

If somehow the voltages across R4 and R8 controlled some dependent sources, they would become type 2 elements and would therefore to be branches of the

NOVE NOVE				
V1 2 3 1.0 R4 3 1 1K		`		
R2 2 5 10K		•		
R3 2 1 1K				
R1 3 4 10K R5 5 1 500K	•			
R6 5 4 1M				
R7 4 6 500K R8 6 1 200				
C1. 4 6 0.015HF				
Il 1 6 500 VR6 DUTPUT		_		
VR8/VVI	NUMBER	OF LOOPS PER	ORDER	
EXECUTE	1=		•	
	2= 3=			
	<del>4=</del> _	14		
		332		
. (			)	
·	1,24E 04	+1.00F 00 S	•	
·			•	
H('S)=-5,382E01*		7 ann 200 700 700 200 200 200 200 200 200 200	) 	
			•	
H('S)=-5,382E01*		7 ann 200 700 700 200 200 200 200 200 200 200	) 	
H('S)=-5,382E01*	1.33E 02	7 ann 200 700 700 200 200 200 200 200 200 200	) 	
(H('S)=-5.382F01*(	1.33E 02	+1.00E 00 S	) 	
(H('S)=-5.3825-01* ( ( ZERO (IF TRANSFER	1.33E 02  FUNCTION  IMAG. PART	+1.00E 00 S	) 	
ZERO OF TRANSFER	1.33E 02  FUNCTION  IMAG. PART	+1.00E 00 S	) 	
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ZERO OF TRANSFER ZERO REAL PART 1 -0.12368E 05	1.33E 02  FUNCTION  INAG. PART  0.00000E 00	+1.00E 00 S	) 	
ZERO OF TRANSFER ZERO REAL PART  1 -0.12368E 05	1.33E 02  FUNCTION  INAG. PART  0.00000E 00	+1.00E 00 S	) 	
ZERO OF TRANSFER ZERO REAL PART 1 -0.12368E 05	1.33E 02  FUNCTION  IMAG. PART  0.00000E 00  FUNCTION  IMAG. PART	+1.00E 00 S	) 	he to l
TERO OF TRANSFER  ZERO REAL PART  1 -0.12388E 05  POLE OF TRANSFER  POLE REAL PART  10.13346E 03	1.33E 02  FUNCTION  IMAG. PART  0.00000E 00  .  FUNCTION  IMAG. PART	+1.00E 00 S	) 	Lead section

NASAP FRUM 1-STAGE	UG FILIEK	nut	
NONE			
NONE	•	•	
V1 2 3 1.0			
R3_2_1_1-K			
R2 2 5 10K			
R1 3 4 10K			
R4 3 1 1K R5 5 1 500K			
R6 5 4 1M			
R7 4 6 500K			
R8 6 1 200			
C1 4 6 0.015UF			
II 1 6 500 VR6			
DUTPUT		DE 10005 050	CODEO
VR8/VV1 —EXECUTE	NUMBER	OF LOCPS PER	UKUEK
	1=	74	
· · · · · · · · · · · · · · · · · · ·	<u>2</u> =	151	
	3≠	93	
	4=_	16	
		334	
TRANSFER FUNCTION	VR8/VV1		
			)
(	1. 34E 04	+1.00E 00 S	,
·	14255 07	T 16 17/16 (10 3	
H(S)=-5.382E-01*			
(			)
( 1	1.33E 02	+1.00E 00 S	)
	-		
ZERO OF TRANSFER FI	INCTION		
, 1			
ZERO. REAL PART	IMAG. PART	·	<del> </del>
1 -0.12388E 05 (	0.0000QE 00		
1 -0.123886 05 (	).000000E 00		
		•	
POLE OF TRANSFER FO	JNCTION		
Anne and are			
POLE REAL PART	IMAG. PART		
1 -0,13346E 03 (	0.00000E''00		
			<del></del>
Titre 2	.11 and 2.12:	R3 in tree	

•			
NONE NONE			***
NUNF			
V1 2 3 1.0 R1 3 4 10K			
R2 2 5 10K R3 2 1 1K			
R4 3 1 1K R5 5 1 500K			
R6 5 4 1M R7 4 6 500K	,		
R8 6 1 200 C1 4 6 0.015UF			•
II 1 6 500 VR6 DUTPUT			
VR8/VVl FXECUTE	NUMBER	OF LOOPS PER	ORDER .
	1 = 2 =	80 163	
	3= 4≃	104	_
		366	
	•		
TRANSFER FUNCTION	VR8/VV1		
(	1.24F 04	+1.50E 00 S	)
H(S)=-5.3825-014		***	
			)
(	1.33E 02	+1.00E 00 S	<b>)</b>
•			
ZERO OF TRANSFER	FUNCTION		
ZERO REA: PART	TMAG. PART		
71 -0.12388E 05	0.00000E 00		
POLE OF TRANSFER	FUNCTION		<del> </del>
POLE :REA: PART	IMAG. PART		
1 -0.13345E 03	0.03000E 00		
· The co	0 72 0 77	le Di in tree	

NASAP FROM 1-STAGE EDG FILTER MOE

NASAP FROM 1-STAGE EDG FILTER MOE
NONE NONE
_NUME
V1 2 3 1 -0 R2 2 5 1:0K
R1 3 4 LOK R3 2 1 LK
R4 3 1 1K R5 5 1 500K
R6 5 4 1 <sup>M</sup> R7 4 6 500K
R8 6 1 200 C1 4 6 0.0157F
11 1 6 500 VR6 NUTPUT
VR8/VV1. EXECUTE
NUMBER OF LOUPS PER CROER
1= 186 2= 369
3= 210 4= 31
796
TRANSFER FUNCTION VKB/VVI
( 1.245 04 +1.035 00 5 )
H(S)==5.382E-C1*
1
( 1.23E 02 +1.00E 00 S )
,
ZERO OF TRANSFER FUNCTION
ZERO REAL PART IMAG. PART
1 -0.12367E 05 0.00000E 00
POLE OF TRANSFER FUNCTION
POLE REAL FART IMAG. PAST
•
1 -0.13346E 03. 0.00000E 00
Figs. 2.15 and 2.16: R2 in tree

loops. Conversely, the tree having the largest Branch Product (R1) yields the flowgraph with the greatest number of loops when compared with the flowgraphs generated by the R4 and R3 trees. However, the flowgraph generated by the R1 tree will give fewer loops than the flowgraph generated by the R2 tree since the R1 tree yields a smaller branch count.

The circuit in Table 2.1 was analyzed using the NASAP program for the four possible trees available from the NASAP tree selection algorithm. The computer results are given in Figs. 2.9-2.16. Fig. 2.9 gives an input listing that includes R4 in the tree. Note that this is not the only listing order that will cause R1 to be a branch of the tree-the only requirement on the input listing is that the card describing R4 must precede those describing R1, R2, and R3. Note that there are 332 flowgraph loops including 72 first order loops Fig. 2.12 shows an input listing that makes R3 a tree branch and show that there are 334 flowgraph loops including 74 first order loops. In Fig. 2.14 is a listing with R1 in the tree. The flowgraph loops generated by the R1 tree total 366 including 80 first order loops. Finally Fig. 2.16 gives a listing with R2 a tree branch. The flowgraph loops number 796 including 186 first order loops. Figs. 2.10, 2.11, 2.14, 2.15 give, the transfer functions obtained for the different trees.

Note that the R4 tree does indeed yield the fewest flowgraph loops. However there is almost no difference between the number of loops generated by the R3 tree and the R4 tree. The R1 tree yields about 10% more loops than either the R4 tree or the R3 tree. The R2 tree generates more than twice as many loops as either of the other trees.

## A Needed Modification

It should be noted that the primitive flowgraph as developed by the NASAP program does differ slightly from the actual primitive flowgraph developed from Kirchhoff's voltage and current laws and Ohm's Law. In the NASAP flow-

graph there can be <u>no</u> connections <u>to</u> the current node of an independent or dependent voltage source as well as no connections <u>to</u> the voltage node of an independent or dependent current source. However such connections may exist in a true primitive flowgraph. If there are no connections emanating from these nodes, then these nodes will not be a part of any loop and no information will be lost in determining the transfer function. This is the reason why one is not able to call for the current of a voltage source or the voltage of a current source as an output variable in the NASAP program. Furthermore, this difference between the NASAP and true primitive flowgraph affects the procedure for determining the optimum tree.

Since there can be no connection between the voltage and current nodes of current and voltage sources (either dependent or independent), let us modify the branch count by omitting the branch count of those loops which are formed from independent and dependent current sources and by deleting from the branch count of each remaining loop those branches representing independent or dependent voltage sources. Similarly the Loop Count will be modified by omitting the loop count of those tree branches which represent independent or dependent voltage sources and by deleting those loops, which are formed by independent and dependent current sources from the loop count of the remaining tree branches. In other words, the modified branch count is the sum of the passive element tree branches that are part of those loops formed from the passive element links while the modified loop count is the sum of the loops, formed from passive element links, that pass through passive element tree branches. Note that the modified loop count will always equal the modified branch count.

The need for the modified Branch Count, Branch Product, and Loop Product is demonstrated from the analysis of the Butterworth filter circuit in Fig. 2.17 [SA-1]

Desired Transfer Function: VV3/VV1

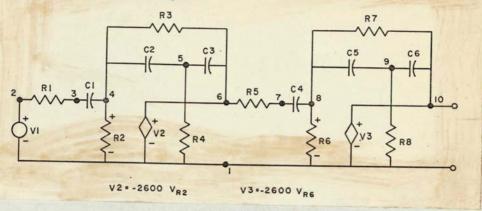


Fig. 2.17: Equivalent Circuit of a Butterworth Filter

The type 2 elements, V1-R2-V2-R6-V3 will be tree branches as will C1 and C4 due to the topology of the network. Either C2 or C3 but not both can be branches and the same situation holds for C5 and C6. There are four trees to choose from, namely

- 1. with C2 and C5
- 2. with C3 and C6
- 3. with C2 and C6
- 4. with C3 and C5

We will concern ourselves only with the first two choices. Table 2.7 gives branch-loop data for the C3-C6 tree while the same data for the C2-C5 tree is shown in Table 2.8.

Table 2.7: Tree with C3 and C6

Link R1 R3 R4 C2 R5 R7 R8 C5

3 2 2 3 3 2 2 3

Branch V1 V2 V3 C1 R2 C3 C4 R6 C6

1 4 3 1 3 2 1 3 2

Branch Count = 20 Branch Product = 1296 Loop Product = 432

Passive Link R1 R3 R4 C2 R5 R7 R8 C5

2 1 1 2 2 1 1 2

Passive Branch Cl R2 C3 C4 R6 C6

1 3 2 1 3 2

Modified Branch Count = 12 Modified Branch Product = 16 Modified Loop Product = 36

Table 2.8: Tree with C2 and C5

Link R1 R3 R4 C3 R5 R7 R8 C6

3 2 2 3 3 2 2 3

Branch V1 V2 V3 C1 R2 C2 C4 R6 C5

1 3 2 1 4 2 1 4 2

Branch Count = 20 Branch Product = 1296

Loop Product = 384

Passive Link Rl R3 R4 C3 R5 R7 R8 C6

2 1 2 2 2 1 2 2

Passive Branch Cl R2 C2 C4 R6 C5

1 4 2 1 4 2

Modified Branch Count = 14 Modified Branch Product = 64 Modified Loop Product = 64

	LKENCU #1 DO	JTTERWORTH								-		-	
NONE												-	
NONE	•												
										. :			
	7.4146										-		
	202UF												-
R2 4 1								•					
6 C3 5 6	20UF										•	,	
R34_6	10.5) QK								7				
	U523K	11.8											قي د
R5 6 7	7 8.54?K												_
C4_7_E R6 8 1	3 282UF		NUMBER-UF-LO	OPS_PER_E	1R-DER		•					•	
_17_C5_8_S	2_20UE	<u> </u>	<u> 1 = -25</u>							;			
14 C6 9 1	LO 20UF	-	2= 186 3=-474										
	10-12-108K 1 -06025K		4= 529										
V311	-0260UVR6-		5=266										
0UTPU1			6= 49 ·				4-			2-4			
EXECU1			1529									•	
										•	-		
TRANSI	EER EUNCTION												
TRANS	FER_FUNCTION_												
TRANSI	FER_FUNCT-ION_	VV3/VV1						4.1					
TRANSI	FER_FUNCTION_		+0.00E 00 S	+1.988	2 05 S +1		+1.00E 00	, , , , , , , , , , , , , , , , , , ,					
	(	0.00E 00	+0.00E 00 S			3.93E 02 S	+1.00E 00	4 }					
	(												
	(	0.00E 00						4	03.5	00E 00.5			
	(	0.00E 00						4	5 -03_S+1(	00E_00_5			
	(	0.00E 00	+3+71E_10_S					4		00E_00_5			
	(	0.00E 00						4		006_00_5			
H(S)=	(	0.00E 00	+3+71E_10_S			39E_07_S		4		00E_00_5	> }		
H(S)=	1.578E 02*	0.00E 00	+3+71E_10_S		2 _09 S+	39E_07_S	+3.05E_05	4		00E_00_5	) )		
H(S)= ZERO ZERO	( ( 1.578E 02* ( ( ( ) ) ( ) ( ) ( ) ( ) ( ) ( ) ( )	0.00E 00  4.92E-12  FUI:CTION  IMAG. PART	+3+71E_10_S	+2,335 POLE OF	2 -09-S+. TRANSFER REAL PART 42975E 01	FUNCTION  IMAG. PAR  0.58384E C	+3.05E_05	4		10E_00_5	) )		
H(S)=  ZERO ZERO	0 TRANSFER REAL PART 0.0000E 00	0.00E 00  4.92E-12  FUI:CTION  IMAG. PART 0.0000E 00	+3+71E_10_S	+2.335 POLE OF	2 	31-39E-07-S- FUNCTION IMAG. PAR 0.58384E C -0.58386F.C	+3.05E_05	4		10E_00_5	) }		
H(S)=  ZERO  ZERO  1 2	0F TRANSFER REAL PART 0.00000E 00 0.00000E-00	0.00E 00  4.32E-12  FUNCTION  IMAG. PART 0.0000E 00 0.0000E 0.0 0.7680E-09	+3+71E_10_S	+2-335  POLE OF  POLE  1 -0 2 -0 3 -0 4 -0 4 -0 4 -0 1	2 .09-S -+ FTRANSFER REAL PART 42975E 01 42975E 01 49350E 01	FUNCTION  IMAG. PAR  0.58384E C  0.5838AE C  0.67260E C	+3.05E_05	4 +1+10E	.03_S+1.,(	6 10E_00_5	) )		
H(S)=  ZERO  ZERO  1 2	0F TRANSFER REAL PART 0.00000E 00 0.00000E-00	0.00E 00  4.92E-12  FUI:CTION  IMAG. PART 0.0000E 00	+3+71E_10_S	+2-338  POLE OF  POLE  1 -0. 2 -0. 3 -0. 4 -0. 5 -0.	2 2 0.9 S	FUNCTION  IMAG. PAR  0.58384E C  -0.58384E C  0.67260E C  -0.47260E C  -0.47260E C  -0.7377E-C	+3.05E_05	4		10E_00_5			
H(S)=  ZERO  ZERO  1 2	0F TRANSFER REAL PART 0.00000E 00 0.00000E-00	0.00E 00  4.32E-12  FUNCTION  IMAG. PART 0.0000E 00 0.0000E 0.0 0.7680E-09	+3+71E_10_S	+2-338  POLE OF  POLE  1 -0. 2 -0. 3 -0. 4 -0. 5 -0.	2 2 0.9 S	FUNCTION  IMAG. PAR  0.58384E C  0.5838AE C  0.67260E C	+3.05E_05	4 +1+10E	.03_S+1.,(	10E_00_S	) )		

Figs. 2.18 and 2.19: Tree with C2 and C5

NASAP_ERENCH_1_dUITER:::RT4			
NONE	,		
,	,		
○ V1 1 2 1.	,		
C1 3 4 .202JF		ت	27-4- (
R2-4-1-101 5- C3-5-6-20UF		- ' ' ' ' ' ' ' ' ' ' ' ' ' ' ' ' ' ' '	
C2_4 5_20UE R3 4 6 10.510K			and the second second
R4 5 1 .0523K V2 1 6 -2600 VR2			
	BER OF LOUPS PER PROER		
	1= 19		<del>سېر</del> دول
	2 <u>s 115</u> 3= 286		
R8 9 1 .06025k	5= 333 5= 180		
	ÓR. 36		
EXECUTE	<u>969</u> ·		
ja			с
TRANSFER FUNCTION VV3/VV1			
TRANSPER, PONCTION VVIVVI	· · · · · · · · · · · · · · · · · · ·		
} }			
( 0.00E 00 +0.0	2 3 00E 00 5 +1.98E 05 S +8.93E 02 S +7.00E 00	4 ) S )	
H(S)= 1.578E 02*			
	2 3	4 5 6.)	١
( 4.32E 12 +3.	71E 10 S +2.33E 09 S +1.39E 07 S +3.05E 05	S +1.106 03 5 +1.00E 00 S )	
	* *		
ZERO OF TRANSFER FUNCTION	POLE OF TRANSFER FUNCTION	······································	
•			
ZERO REAL PART LIMO. PARI	2 POLE REAL PART IMAG. PART		
1 0.0000E 00 0.0000E 00 2 0.0000E 00 0.0000E 00	1 -0.42956E 01 -0.56382E 02 2 -0.42956E 01 -0.56382E 02	1	
i 3 -0.41494E 03 0.97890E-09 i 4 -0.47891E 03 -0.79611E-08	3 -0.493746 01 0.672616 02 4 -0.493746 01 -0.672616 02		
<u>į.`.</u>	5-0.41512E 03 0.10178E-04 6-0.41512E 03 0.10862E-04 - Pole	6 aguals pole 5	
<u> </u>	10/7/69 nico pole 600	-6777 E 03	
<u></u>			<u>.</u>
<u> </u>			

Figs. 2.20 and 2.21: Tree with C3 and C6

tree. The problem remains of selecting these dependent sources such that they do not affect the circuit being analyzed. This is easily accomplished by making these sources dependent voltage sources with one node of the source connected to any node of the original circuit and with the other node left unconnected. Each unconnected node is actually an additional node in the modified circuit. Since a tree is an interconnection of all nodes and since the only connection to these hanging nodes is the source itself, then each of these sources must be a tree branch and thus a voltage source. However since one node of these voltage source is left floating, these sources will in no way affect the original circuit because no current can flow through these sources. The zero-load feature of this type of "dummy" source is also quite apparent in the flowgraph. There is a connection to the voltage node of the voltage source from the voltage node of the controlling element. However no connection emanates from the voltage node of the voltage source since this "dummy" voltage source is not involved in any of the network loops formed by the links of the co-tree. A node can be part of a flowgraph loop only if there is a connection leading to and away from the node. Since these "dummy" voltage sources are not part of any flowgraph loop, then they cannot affect the determination of the transfer function.

Thus the addition of the following two cards

to the input lists of either Fig. 2.18 or Fig. 2.20 will make R4 and R8 tree branches without affecting the electrical properties of the original circuit. Nodes 11 and 12 are the floating nodes. Note that the dependency value (1.0 in this case) is completely arbitrary and can have any value except 0.0. In essence, the above "trick" simply is an artificial means to tell the NASAP program what elements we wish to have in the tree. It does have the drawback in that elements are needlessly wasted but this only becomes a factor when the

number of elements in the circuit is near the limit set by the length of the computer word. Note also that if an element which one desires to put into the tree by the above "trick" is also declared a type 6 element somewhere else in the input list (i.e., its current controls some source or is the desired output variable), then an error message will result.

Fig. 2.22 gives the necessary branch data for the R4-R8 tree. Take note that the branch count, branch product, and loop product were determined without regard to the "dummy" sources V4 and V5.

Fig. 2.22: Tree with R4 and R8

Branch count	= 18	Modified Branch count = 1	2
Branch product	= 576	Modified Branch product = 16	6
Loop product	= 216	Modified Loop product = 30	6

Note that the modified data is identical to that obtained for the C3-C6 tree. However the unmodified branch count is two less than that of either the C2-C5 tree or the C3-C6 tree. Figs. 2.24 and 2.25 give the computer results. The R4-R8 tree generates a flowgraph of 737 loops (including 17 first order loops). This is less than one-half the loops generated by the C2-C5 tree and more than 200 loops less than the number of loops derived from the C3-C6 tree--a substantial reduction.

~	NASAP FRENCH 1 BUTTERN IRTH
~	NONE
	NONE
· .	W. 1. 2. 1.
	VI 1 2 1, RI 2 3 7,4141 — C1 3 4 ,20245
	P2 4 1 10M 
	02 4 5 20UF 
<u></u>	R4 5 1 .052°4 
	R 5 6 7 6 . 5424 C4-7-8-28245 NUMBER GE_L-1195_DEF LRDL
- \ 	R6 8 1 10H 
	C5 8 9 20UF . 2= 94 
	R8 9 1 .06027k
<u> </u>	V4 1 11 1.0 VR4 6= 75 '
	OUTPUT 737
	EXECUTE
	TRANSECR_FU_CIIO*
	,
	( C.1'E 00 +0.00F 00 S +1.70E 05 S +8.93F 02.S 11.00E 00 S )
	H(S)= 1.578F (027
	4.32E 12 +3.71E 10 S +2.33E 09 S +1.35E 07 S +3.05E 05 S +1.10E 03 S +1.00E 00 S
	ZERO UF TRIISFER FU CITAL
	ZERO PEAL PART (MAG. PART
	1 -0.42914E 01 0.58393E 02
	1 0 00000E 00 0 00000E 00 2 -0.429(4E 01 -0.50363E 02 2 3.0000E 00 0,0000E 00 3 -0.415(3E 03 0.000)0E 00
	3 -0,416/4E //3 (-m.th.05 (ft)
	6 -0.467735 D3 0.00000E D0

#### CHAPTER III

### MODELING A CONTROL SYSTEM FOR NASAP

### IIIA GENERAL DISCUSSION OF CONTROL SYSTEMS

The preliminary discussion of feedback control systems is kept brief on the assumption that the reader already is generally acquainted with feedback control theory. Familiarity with introductory textbooks such as Dorf's Modern Control Systems [D0-1] and Perkins and Cruz Engineering of Dynamic Systems [PE-1] would be particularly helpful in that they use aerospace feedback control system problems as illustrative examples.

The major subdivisions of feedback control systems usually are:

- 1. A plant, process or controlled system wherein the position or state is being regulated or monitored.
- 2. The controller consisting of a sensor and control elements.
- 3. A comparator or error-sensing device to detect the difference between the input reference and the output signal.

Next we itemize the major steps involved in the design of a feedback control system. These steps are:

- a. Establish performance specifications for the system
   (e.g. type of control, tolerance on accuracy, speed of response, overshoot, etc.)
- b. Interpret the specification data in terms of design parameters and components of the control system. (give due consideration to reliabilit space, cost, etc.)
- c. Formulation of the transfer functions of the components and analysis of the preliminary design.
- d. Improve the performance of the preliminary design by suitable compensation to meet the specifications.

The scope of computer-aided design in this manual only covers aspects of steps c and d.

Control system design can be carried out either in the frequency or in the time domain. This is important in considering the possible role of NASAP in such applications. Control engineers have found it convenient, in the analysis of linear feedback control systems, to use the transfer function concept and the block diagram representation of the system. The transfer function concept is basic in the application of the frequency response method of analysis. In this approach the steady state response of the system to a sinusoidal input is used. The output/input signal relationship for each component of a control system is described by a transfer function. The operations of these components are represented by noninteracting blocks which are interconnected to form the block diagram or the corresponding signal flow graph of the overall system. Thus one obtains a functional representation of the feedback control system equivalent to the set of simultaneous differential equations that relate the variables of the physical system.

The basic procedures usually followed to analyze and design a feedback control system by the frequency response method are:

- i) Determine transfer functions for each of the components used in the system (from the differential equations via transforms or from physical measurements).
- ii) Formulate the signal flow graph from the system block diagram.
- iii) Reduce the complicated block diagram of the system to a simple single loop configuration having a transfer function for the forward and the feedback branch if the open loop transfer function and output transform of the control system are to be used.
- iv) Determine the system characteristics using the Bode plot or Nyquist diagram (an alternative graphical method uses the Nichols chart).
- v) To have the system meet the prescribed performance specifications, design the necessary compensators that will reshape the plots obtained in step iv. This may involve cut and try.

In addition to the above, the designer often has to investigate sensitivity of parameters to variation of individual elements. The final step may include analog simulation or physical model tests.

As an alternative to the frequency response approach, the analysis and synthesis of feedback control systems determination of the system stability and the evaluation of the output of the system in response to impulse, step or ramp input functions. Here again there is often the need for compensation of the system so that it will meet specs.

In the remaining chapters of this manual we shall indicate how NASAP can assist the design engineer to accomplish some of this work. It should be noted that some of these procedures are best carried out with a hybrid computer. Dr. C. H. Beck [BE-1] has developed a hybrid NASAP module for such applications as part of this cooperative development of the NASAP program.

# IIIBl Equivalent Electrical Networks for Transfer Functions

Before a control system can be analyzed using NASAP and before any necessary compensation can be determined, the dynamic characteristics of the plant must first be simulated by an electric network which has an equivalent dynamic characteristic. The transfer function of a lumped linear plant can be expressed as a ratio of two polynomials. The problem of modeling the plant transfer function can be simplified if the polynomials are put in factored form. The individual factors or group of factors can be modeled by using simple RLC circuits. Then for a complicated transfer function these circuits are connected in cascade with suitable isolation between each circuit to prevent loading that would result in a change in the modeled transfer function. This necessary isolation is obtained by using ideal dependent voltage or current sources (which are available in NASAP). Table 3.1 gives a list of some elementary circuits with isolation and their corresponding transfer functions.

Table 3.1

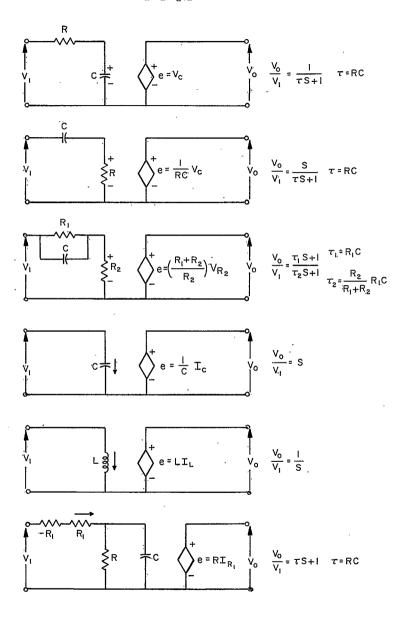
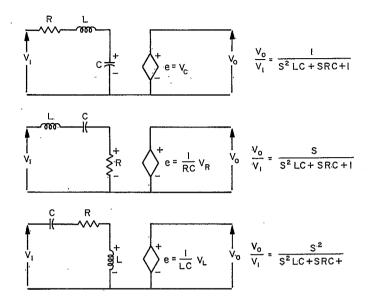


Table 3. E (continued)



# IIIB2 Cascade Interconnection of Transfer Function Models

As indicated earlier the simple transfer function models can be cascaded.

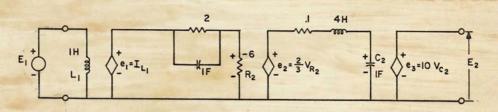
Consider a plant transfer function given as:

$$\frac{E_2(s)}{E_1(s)} = \frac{10(2s+1)}{s(3s+1)(4s^2+0.1s+1)}$$
(3.1)

This can be rewritten as:

$$\frac{E_2(s)}{E_1(s)} = \frac{1}{s} \cdot \left(\frac{2s+1}{3s+1}\right) \cdot \left(\frac{10}{4s^2 + 0.1s + 1}\right)$$
(3.2)

Thus a descade interconnection of three circuits from Table 3.1 can be used to model the above transfer function.



Note that  $R_2$  is a negative resistance and that the gain factor (for this example, 10) is included in the dependency relation for the third dependent voltage source  $(e_3)$ . The gain factor could just as easily be included in the dependency relations of  $e_1$  or  $e_2$ .

Many of the subsequent examples used to illustrate various aspects of computeraided control system design will incorporate techniques for modeling the pertinent transfer function.

#### IIIC ADDITIONAL EQUIVALENT NETWORK MODELS

#### IIIC1 Use of Negative R, L or C

Since negative element values of R, L, and C are permitted in the NASAP input coding, rational transfer functions of control systems can be modeled simply by application of the continued fraction expansion procedure. Accordingly the rational function will be represented in general by the input admittance or impedance of a ladder structure consistings of positive or negative R, L, and C elements. It is emphasized that this approach works because physical realizability as a passive network is not a consideration. Only the equivalent dynamic characteristic matters.

As an example, let us consider the biquadratic all-pass function

$$F(s) = \frac{s^2 - as + b}{s^2 + as + b}$$
 (3.3)

Performing the continued fraction expansion of F(s) yields

$$s^{2} + as + b \int_{s^{2} - as + b}^{1}$$

$$s^{2} + as + b - \frac{1}{2a} s$$

$$-2as \int_{s^{2} + as + b}^{2} -2as$$

$$\frac{s^{2}}{as + b} - \frac{2}{2as}$$

$$\frac{-2as}{2b} - \frac{a}{2b} s$$

$$\frac{as}{2b} - \frac{2}{2b}$$

$$\frac{as}{2b} - \frac{2}{2b}$$

If F(s) is assumed to be an admittance  $Y_1$ , then the resulting ladder network is shown in Fig. 3.1.

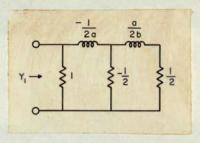
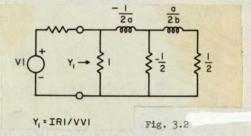


Fig. 3.1

In other words, the input admittance  $Y_1$  of the circuit of Fig. 3.1 is a representation of the specified rational function F(s).

To utilize this input admittance model with the NASAP program, two additional elements, a voltage source and a resistance of very small value, must be included in the circuit of Fig. 3.1 (see Fig. 3.2).

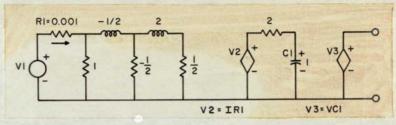


The voltage source VI represents the excitation for the input admittance  $Y_1 = \frac{I_1}{V_1}$ . The response is the current  $I_1$ . However the current flowing through a voltage source cannot be specified with the NASAP program. Since no element of the circuit of Fig. 3.1 is in series with the source VI, it is necessary to include the small resistor R1. Thus the input admittance of this circuit can be specified as

$$Y_1 = IR1/VV1$$
 (3.5)

The circuit of Fig. 3.2 can be easily cascaded with other isolated circuits to model more complex rational functions. As an example, the transfer voltage ratio of the circuit of Fig. 3.3 models the function.

$$\frac{s^2 - s + 4}{(s^2 + s + 4)(2s + 1)} \tag{3.6}$$



$$VV3/VV1 = \frac{s^2 - s + 4}{(s^2 + s + 4)(2s + 1)}$$

Fig. 3.3

Alternatively the function F(s) given above can be assumed to be an input impedance  $Z_1$ . From the continued fraction expansion, we obtain the NASAP applicable circuit of Fig. 3.4.

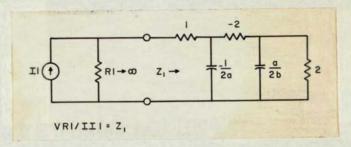


Fig. 3.4

The current source II represents the excitation necessary for the input impedance. The response is the voltage across the very large resistance Rl which must be added to the circuit since no single element obtained from the continued fraction expansion is connected across the ideal current source terminals.

However it is possible to avoid the use of the small series resistor of Fig. 3.2 and the large shunt resistor of Fig. 3.4 by taking the reciprocal of (i.e. inverting) the rational function that is to be modelled by NASAP <u>before</u> performing the continued fraction expansion.

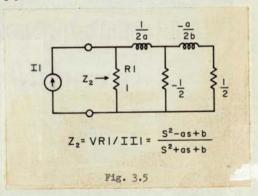
As an example, let us desire to model the biquadratic all-pass function given above by the input impedance of some ladder circuit. Thus we desire a circuit whose input impedance is defined by

$$Z_2(s) = \frac{s^2 - as + b}{s^2 + as + b}$$
 (3.7)

Inverting this expression we obtain

$$Y_2(s) = \frac{s^2 + as + b}{s^2 - as + b}$$
 (3.8)

Performing the continued fraction expansion this time yields the NASAP circuit is shown in Fig. 3.5.



Note that now there is no need to include a large shunt resistor across the Il current source terminals (as in Fig. 3.4) since the resistor R1 already shunts these terminals.

Similarly, we can model the biquadratic all-pass function by the input

admittance of a ladder network defined by

$$Y_3 = \frac{s^2 - as + b}{s^2 + as + b} \tag{3.9}$$

Inverting this expression and then performing the continued fraction expansion (given above), we obtain the ladder circuit of Fig. 3.6.

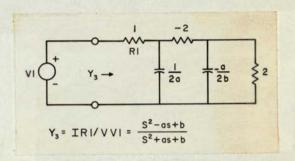


Fig. 3.6

Note that addition of a small series resistor (as in Fig. 3.2) is not needed since the current flowing in the resistor Rl is from the voltage source Vl.

In summary, by use of the continued fraction expansion procedure, we have obtained four NASAP-codable circuits to model the specified all-pass function F(s). The circuits of Figs. 3.5 and 3.6 are more desirable as models than those of Figs. 3.2 and 3.4 since they require one less element. It should be further noted that each of these four circuits has another desirable feature. The NASAP tree-selection algorithm will automatically select the shunt elements of each circuit as tree branches. This will lead to a star tree which generates the flow-graph with the fewest loops.

This will always occur if the polynomials of the specified rational function are arranged in descending powers of s. The resulting continued fraction expansion will either make the series elements inductors or the shunt elements capacitors.

#### IIIC2 Illustrative Examples

Sometimes it is necessary to arrange the polynomials in ascending powers to attain a ladder network with both positive and negative elements. For example, let us assume we wish to model the function

$$F_1(s) = \frac{1}{s^3 + 2s^2 + s + 1}$$
 (3.10)

as the input impedance of a ladder network. We cannot perform a continued fraction expansion on  $\mathbb{F}_1^{-1}(s) = s^3 + 2s^2 + s + 1$ . Consequently we will need a large shunt resistor in the NASAP model. Furthermore we must rearrange the denominator of  $\mathbb{F}_1(s)$  in ascending powers of s before performing the continued fraction expansion. The resulting NASAP model with shunting resistor Rl is shown in Fig. 3.7. Note that, since the shunt elements are

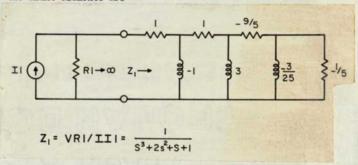


Fig. 3.7

inductors, the NASAP tree-selection algorithm will pick a linear tree consisting of resistor Rl and three of the other four resistances (the particular R's depending upon their location in the input list). This type of tree yields the largest number of loops in the corresponding primitive flowgraph.

Sometimes in the continued fraction expansion procedure more than one term is eliminated by subtraction. This may necessitate a rearranging of the remaining polynomials to achieve a NASAP model. Such a case exists for the function

$$F_2(s) = \frac{1}{s^3 + s^2 + s + 1}$$
 (3.11)

The first three steps of the continued fraction expansion process is based on ascending order of the denominator. Then three terms become zero. This necessitates reversing the polynomial -s-s<sup>2</sup>-s<sup>3</sup> to -s<sup>3</sup>-s<sup>2</sup>-s.

In Fig. 3.8 is given a NASAP-codable ladder network whose input impedance equals the desired function Fo(s).

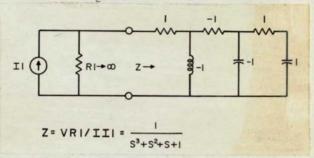


Fig. 3.8

Another example is the biquadratic function

$$F_3(s) = \frac{s^2 + as + b}{s^2 + as + c}$$
 (3.12)

Let us model this function as an input impedance. Inverting  $F_3(s)$  and then per-

Let us model this function as an input impedance. Inverting 
$$F_3(s)$$
 and then proforming the continued fraction expansion yields

$$\begin{array}{c}
1 \\
s^2 + as + b
\end{array}$$

$$\begin{array}{c}
\frac{1}{s^2 + as + c}
\end{array}$$

$$\begin{array}{c}
\frac{s^2 + as + b}{(c - b)}
\end{array}$$

$$\begin{array}{c}
\frac{b}{as}
\end{array}$$

$$\begin{array}{c}
\frac{c - b}{as}
\end{array}$$

$$\begin{array}{c}
\frac{c - b}{as}
\end{array}$$

$$\begin{array}{c}
\frac{-a^2}{c - b}
\end{array}$$

$$\begin{array}{c}
\frac{c - b}{as}
\end{array}$$

$$\begin{array}{c}
\frac{c - b}{as}
\end{array}$$

$$\begin{array}{c}
\frac{c - b}{as}
\end{array}$$

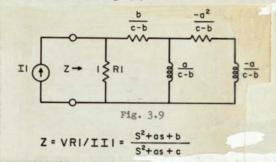
$$\begin{array}{c}
\frac{as + s^2}{as + s^2}
\end{array}$$

$$\begin{array}{c}
\frac{as + s^2}{as + s^2}
\end{array}$$

$$\begin{array}{c}
\frac{as + s^2}{as + s^2}
\end{array}$$

$$\frac{as - \frac{c - b}{as}}{s^2 - \frac{c - b}{a}s}$$
 (3.13)  
$$\frac{c - b}{a}s$$

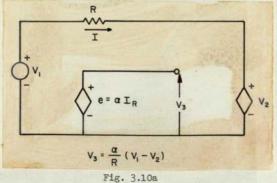
The resulting network is shown in Fig. 3.9.



Note the large shunt resistor is again avoided by use of the initial inversion. Note also that in the underlined section of the continued fraction process it was necessary to reverse the polynomical s2 + as + b since two terms were eliminated in the preceding subtraction.

# IIIC3 Equivalent Networks for Summing Element

Since most control systems require some sort of feedback loop, an electrical network equivalent to the summing (or subtracting) element that is compatible with NASAP must be used. Such networks are shown in Figs. 3.10a and 3.10b.



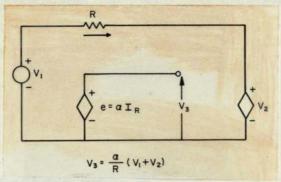


Fig. 3.10b

In Fig. 3.10a if  $\alpha$  = R = 1, the output voltage is equal to the difference of the two input voltage. Similarly if  $\alpha$  = R = 1 in Fig. 3.10b, the output voltage is equal to the sum of the two input voltages.

## IIID MODELS OF FEEDBACK CONTROL SYSTEMS

# IIIDl Examples of System Models

Thus we now have all the elements necessary to model a feedback control system with an electric network that is compatable with NASAP. As an example, the unity feedback control system shown in Fig. 3.11.

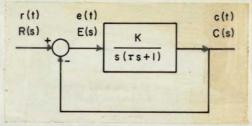


Fig. 3.11

has the following equivalent electric network

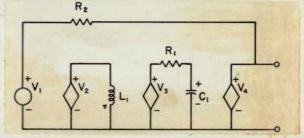


Fig. 3.12

where  $V_1$  is equivalent to r(t)

Vo is equivalent to e(t)

Vh is equivalent to c(t)

A second example shows a NASAP model for a non-unity feedback system (Fig. 3.13).

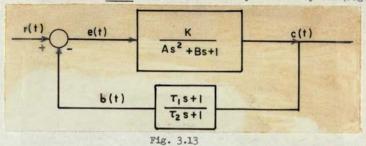
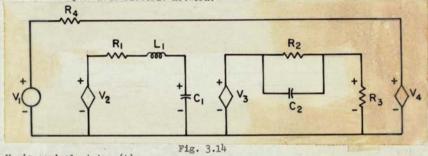


Fig. 3.14 is the equivalent electric network.



where V, is equivalent to r(t)

Vo is equivalent to e(t)

 $V_2$  is equivalent to c(t)

Vh is equivalent to b(t)

# IIID2 Control System Model and Its Step Response

Using a control system design problem adapted from D'Azzo and Houpis, pp. 408-411 [DA-1] we illustrate modeling of the system and use of NASAP to tabulate and plot the step response.

Consider the unity feedback control system with cascade lead compensation shown in Fig. 3.15. To determine the step response when K = 10 we first obtain the NASAP

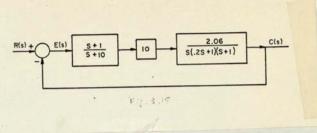


Fig. 3.15

circuit model shown in Fig. 3.16. In this model

V5 represents the input R(s)

V4 represents the output C(s)

V6 represents 2.06 times the error signal; 2.06 E(s)

Note that the system gain, K = 10, is included in the dependency relation of V1. Also in Fig. 3.16 we have NASAP output, namely the transfer function zeros and poles based on a simple flowgraph having only right first order loops. The desired step response is given in Fig. 3.17. Figure 3.17a is the response function and 3.17b gives 51 discrete time values from zero to six seconds in equal increments. Finally in Fig. 3.18 we have the plot of this time response.

These NASAP outputs can be used to determine the key step response characteristics. Note in particular that the steady state value is unity since Fig. 3.17a we see that the residue of the pole at the origin is unity. Furthermore in Fig. 3.17b the peak overshoot occurs at t = 1.44 seconds and is 9.15%. This response settles (for 2% tolerance) in 2.04 seconds.

# NASAP MODEL FOR CONTROL SYSTEM

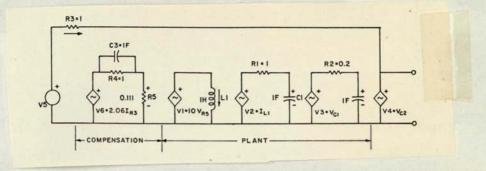


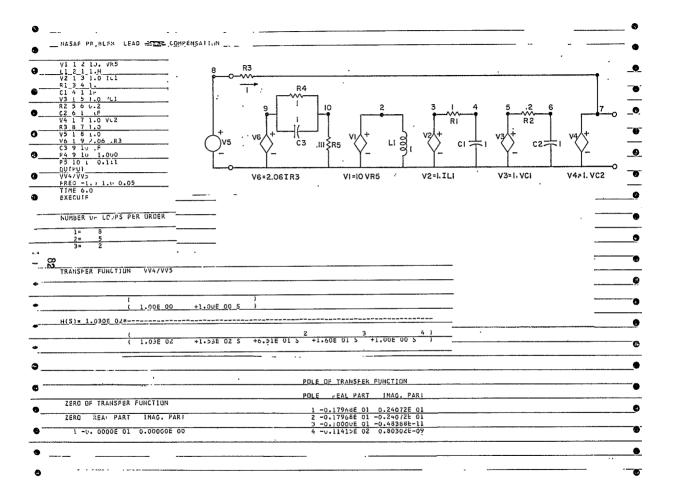
Fig. 3.16

Resistance Values in Ohms

V5 represents the input R(s)

V4 represents the output C(s)

V6 represents 2.06 times the error signal; 2.06 E(s)



STEP RESPUNSE FUNCTION	STEP RESPONSE	
F(T) =	TIME	VV4/VV5
	0.00001-00	0.0000000000000000000000000000000000000
(-0.1797E 01 J 0.2407E 01 ] T	0.12006 00	U.19343615E-01
(-0.45+1E 00 J 0.5566E 00 ) E	0.2400E 00 0.3600E 00	0.104/8669E 00 0.24626642E 00
(-0.1797E 01 J-0.2407E 01 ) T	0.4800L 00	. U.4149/654E OU
(-0.45+1E 00 J-0.5566E 00 ) E	0.6000£ 00	Q.58518541E 00
(-0.4512 00 3-0.55002 00 / 2	0.72001 00	U./3J95842E 00
(-0.1000E 01 J-0.4839E-11 ) T	0.84001 00	U.86608770E 00
( U.2904E-05 J 0.7443E-11 ) E	0.9600E 00	0.96.66139E 00
	0.1080E 01	U.10293307E U1
(-0.1142E 02 J 0.8030E-09 ) T	0.12008 01	U.10695372E Ul
(-0.91.8E-01 J-0.6499E-11 ) E	0.1320L 01	k . 0.10684190b 01
	→ 0.1320E 01 pea	U.10914555€ 01 <-7/
( 0.0000E 00 J 0.0000E 00 ) T	0.15005 01	0,108307875 01
( 0.1000E 01 J 0.6551E-10 ) E	0.1680E 01	0.10.01990E 01 0.10.39808E 01
	0.1800E 01 0.1920E 01 .se#1	
	0.1321'C 01 3277	1 >0.10233526 01 - 2% tolerand
	0.2160E 01	v.10115232E 01
	0.22806 01	C.10(26340E 01 .
;	0.2400E 01	0.99(58346E 00
	0.2520E 01	0.99300891E 00
	0.264UE 01	U.99141634E UO
· ···· · · · · · · · · · · · · · · · ·	0.2760E U1	0.99127769E 00
	0.2880+ 01	0.99:09821: 00 .
	. 0.3000E 01	0.993456186 00
	0.3120± 01	U.99502158E UO
•	0.32406 01	U.99655831E 00
	. 0.3360E 01	0.99/915986 00
•	0.3480E 01	0.999015574 00
	0.3600E 01	0.99983263€ 00
	0.37201 01	0.10003805E 01 0.10006971E 01
	0.3840E 01 0.3960E 01	0.10008971E 01 0.10008297E 01
	0.40806 01	0.10008297E 01
<del></del>	0.4200E 01	0.10000287E 01 0.1000/420E 01
	0.4320F 01	0.100060756 01
	0.444Ut 01	6.10004568E 01
	0.456UE 01	0.10003109E 01
	0.468JE 01	0.10001831c 01
•	0.480ut 01	U.10000811E 01
	0.4925E 01	0.1000000 / 6 01
	· 0.5040t 01	0.39995/386 00
	0.516vt 01	0.99992949= 00
	0.528vE 01	U.99591864E 00
	0.5400E 01	U.99991995E OU
	0.5400E 01 0.5520E 01	0.99941995E 00 0.99742901E 00
	0.5400E 01 0.5520E 01 0.5640E 01	0.99741995E 00 0.99742901E 00 0.9994224E 00
	0.5400E 01 0.5520E 01	0.99941995E 00 0.99742901E 00

Ð					STEP	RESPUNSE							
<b>D</b>						-1.00E-01				7.00E-01		1.10E 00	
	0.0000E 00	*****	••••••	• • • • • • • • • • • • • • • • • • • •	•••••••			•	· · · · · · · · · · · · · · · · · · ·	•	•	*****	
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#### CHAPTER IV

#### CONTROL SYSTEM ANALYSIS IN THE FREQUENCY DOMAIN

#### IVA ANALYSIS OBJECTIVES

As mentioned in Chapter III control system design is usually aimed at a set of specifications. Therefore we start with a summary of typical performance specifications as general background. For convenience we adapt the tabulations given by Grabbe, Ramo, and Woodruff [GA 2] and list some of them for transient response in Table 4.1a and for frequency response in Table 4.1b. These are sufficient to indicate the sort of specifications that can be expected for the class of linear time-invariant single input single output control systems being considered in this manual.

There are several approximations or rules of thumb which were developed by control engineers for use when time or facilities are not available for a more exact analysis of this class of systems. They are also useful as rough checks on the results of a computer analysis. The more common of these rules of thumb are presented, virtually unchanged from [GA 2] in Table 4.2. They must, however, be used with caution since being approximations, they do not apply with equal validity to all control systems. Note that the approximations for transient response are applicable only for step inputs.

Following Table 4.2 we have Fig. 4.1 which shows typical step and frequency response curves to help pin down the definition of some of the terms used in these tables.

	Common Peri	FORMANCE SPECIFICATIONS	Transient response
Type  1. Transient over		Definition sually taken as ratio of peak of transient to final value for a step input.	General Remarks  Convenient when transient solution is available. Can be estimated from 100t locus or frequency response. Useful for nonlinear systems System must be accreted by step input; and be underdamped
2. Settling time	, ;	efined as time to reach and remain within a spec- ified percentage of final value (often as 5% or 2%) after a step input,	See I above Used for systems which require rapid synchronization, e.g., fire control system.
3. Stendy-state en	(	nal error existing between desired and actual out- put.	See 1 above. Easily calculated from static characteristics or final value theorem. Use- ful when input is simple aperiodic function. Can include frequency components which
4. Rise time	1 : 1	fined as (a) time to $\frac{1}{2}$ the final value, or (b) slope at $\frac{1}{2}$ the final value, or (c) time between 10% and 00% of final value after a step input.	arise in nonlinear systems.  Easily estimated from frequency response or root locus and is indicative of band pass of system. Used for overdamped systems. Has found application in process controls where characteristics (1) or (2) may not be easily
''5. Dead time	· De	fined as (a) time for out- out action to be initiated, or (b) for output to reach a given level (10% or 10%), or (c) time to the ntersection of the slope	recognized.  See 1 above. Easily estimated from frequency response and is indicative of phase shift near gain crossover in systems. Useful when delay times exist in system. Used for overdamped systems. Both rise and delay time derive from filter theory.
6, Absolute dam decrement fact	ing, De	of the transient at ½ the final value and the initial value after a step input. Sined as the real part of the roots of a quadratic system and as such determines the rate of decay of transient.	Convenient method of interpreting more complex systems in terms of quadratic systems. Valuable in combination with relative damping in work with root locus analysis. Has had extensive use in systems demanding prescribed transient performance, particularly when the time decay is important, e.g., in autoalidate

autopilots.

of transient.

Useful because it is a parameter in nondimensional plot of quadratic response. Used in combination with 6 above in root locus analysis. Used when number and size of overshoot are important. In combination with 6

above defines decay of oscillatory component

Damping ratio is defined as  $\zeta$  in the quadratic  $s^2 + 2\omega_0 \zeta s + \omega_0^2$  and indicates

the decay per cycle of the natural frequency.

7. Damping ratio

Í	•	
Соммог	PERFORMANCE SPECIFICATION	
8. Phase margin	Defined as 180°+ phase shift at unity gain of the open loop frequency response.	Used as a rule of thumb in frequency response analysis to indicate stability and perform- ance. Basy to use and to obtain directly from frequency response diagram.
9Gain margin	Gain margin is ratio of max- imum stable gain to ac- tual gain, i.e., gain at phase crossover.	Same as 8. Indicates relative sensitivity of system to gain variations. Can be calcu- lated by Routh's criterion. Not as good a criterion for performance as 8. Little used.
$O_{\bullet}M_m$ peak	Ratio of maximum of closed loop frequency response to a low frequency value.	Used with Nyquist and frequency response analysis. Rules of thumb relate $M_m$ and transient overshoot. Easy to calculate from frequency response diagram.
11. Band width	Defined variously (a) usually as frequency where closed loop response falls to $\sqrt{\frac{1}{2}}$ or 3 db of its low frequency value, or (b) sometimes as the frequency at the significant peak $M_m$ , or (c) the crossover of the open loop response.	Used with frequency response analysis and is related to speed of response of system. Used also when definite frequency bandpass is needed for fidelity. $M_m$ , bandpass, and the phase shift at these valves give a good indication of the closed loop response and are often used when a number of closed loops are operated in tandem as system.
12. Static error coefficient	Defined as the final error resulting from a continuous input of position, or velocity, or acceleration, etc. The magnitude of the input and the maximum tolerable error must be specified.	Used to set low-frequency gain of open loop frequency response. Useful where steady inputs are encountered.
13. Dynamic error coefficients (or steady-state error coefficients)	Defined as the steady-state enfor resulting from the derivatives of the input function. The time function and/or its derivatives must be specified as well as the maximum tolerable error.	Relates system gain and time constants to errors arising from higher derivatives of input. Used to estimate error resulting from varying input to given system and conversely to determine closed loops pole-zero location to give desired error. Accurate where input varies at slow rate compared to bandpass. Becomes poorer as input varies more rapidly because of transient effects.

# Table 4.2

# RULE-OF-THUMB APPROXIMATIONS

Parameter		211 FROXIMATIONS
	Approximation	Remarks
Time to peak	where $t_p \approx \pi/\omega_c$ where $t_p = $ time from step input to peak value of response transent, seends $\omega_c = $ open loop crossover frequency, tadians/second	In eases with a dominant complex pair of closed loop poles, the open loop crossover frequency, $\omega_c$ , times the time to peak, $t_p$ , is about $3  \text{or}  \pi$ . In other words, the time to peak is about half the period corresponding to the open loop crossover frequency.
Peak over- shoot	$C/R _p \approx 0.85 M_m$ where $C/R _p = \text{peak}$ value of transient response to a step input $M_m = \text{maximum value of closed}$ loop frequency response	The peak value of the transient response, $C/R _p$ , to a unit step input is generally less than the maximum steady-state value, $M_m$ , of the closed loop frequency response. The maximum value of $C/R _p$ generally approaches 20 while the maximum value of $M_m$ approaches infanty. For many applications "good" servos are those with the values of $M_m$ between 1.3 and 1.5.
' Damping ratio	$\zeta = 1/(2M_c)$ where $\xi = { m damping ratio}$ $M_c = { m value of closed loop}$ frequency response at the corner frequency	The damping ratio may be approximated from the value of the closed loop frequency 10-sponse of the system at the corner frequency, $\omega_e$ (the frequency at which the lines asymptotic to the log magnitude curve intersect). This is exact for a second order system.
Settling time	$t_{*(5\%)} \approx 3\sqrt{1-\zeta^2/\zeta\omega_d}$ $t_{*(2\%)} \approx 5\sqrt{1-\zeta^2/\zeta\omega_d}$ $t_{*(5\%)} \approx 3T_{eq}$	The settling time, $t_*$ , is generally defined as the time for the system to settle to within 5 or
	where $t_s$ = time for response to step input to settle to within some per cent of final value, seconds $T_{\rm eq}$ = time for response to reach 63% of final value $\omega_d$ = damped natural frequency, radians/ second $\zeta$ = damping ratio	sometimes 2% of the final value. In either case it is quite difficult to predict t for an underdamped system because it is subject to fluctuations of about one-half the period of oscillation for only small changes in system parameters.

# Rule-of-Thumb Approximations (Continued)

# Parameter Approximation Rise time $t_r\omega_t \approx t_r\omega_m \approx 1.3$ where $t_r=$ rise time (10 to 90%) $\omega_t=$ (defined above) $\omega_m=$ (defined above)

## Remarks

The system's rise time,  $t_{r_t}$  which is here considered to be the time for the response to a step input to go from 10 to 90% of its final value may be approximated as indicated for systems with a  $M_m$  value of about 13 to 1.5.

Phase margin at where  $\gamma_c \ge 40^\circ$  where  $\gamma_c = 0$  open loop phase region at the crossover frequency

Oscillation

frequency

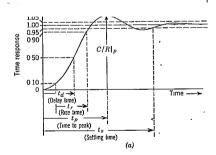
A phase margin of  $40^{\circ}$  at the unity gain (crossover) frequency generally corresponds to a  $M_m$  ratio of approximately 1.5. Since this value of  $M_m$  is the maximum ordinarily considered feasible, the phase margin should be  $40^{\circ}$  or greater.

where  $\omega_t = \text{oscillation fre-} \\ \text{quency of transient} \\ \text{response, radians/} \\ \text{second} \\ \omega_m = \text{frequency at which} \\ M_m \text{ occurs, radians/second} \\ \omega_c = \text{open loop gain} \\ \text{crossover fre-} \\ \text{quency, radians/}$ 

second

 $\omega_t \approx \omega_m \approx 0.75\omega_c$ 

The frequency of oscillation of the transient response,  $\omega_t$ , is generally about equal to the frequency,  $\omega_m$ , at which the frequency response peak, Mm, occurs. Both wm and wt are usually less than  $\omega_c$ , the open loop crossover frequency. For the "good" servos with Mm = 1.3 to 1.5 an approximate relationship is as indicated. In this approximation  $\omega_t$  is used to mean essentially the same thing as  $\omega_d$ , the damped natural frequency, previously defined for a system with a dominant complex pair of poles.



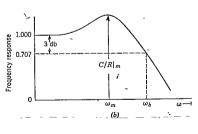


Figure 4.1. (a) Typical serve system response to unit step input.

(b) Typical system frequency response (closed loop).

#### IVB BODE AND ROOT LOCUS PLOTS

Bode showed that the phase angle of a (minimum phase) transfer function G could be related to the rate at which the magnitude of G decreases with increasing frequency. This is the basis for the "frequency response", method of analysis. In this method, the magnitude of G in decibels and the phase angle, are plotted on semilog paper as functions of the frequency  $\omega$  (plotted on the log scale) with j $\omega$  substituted for s in G. The value of |G| in decibels (dB) can be found from the value of |G| by the following equation.

$$\left| G \right|_{dB} = 20 \log_{10} \left| G \right| \tag{4.1}$$

For preliminary estimation of compensating networks to insure stability or improve performance, it is often possible to omit the phase angle plot and to make use of an approximate attenuation plot (or plot of [G]). Exact plots are needed for a final check after selection of the proposed stabilizing transfer functions, however. The method of drawing approximate attenuation plots is described in most textbooks on control theory. Before we discuss and illustrate how NASAP obtains exact plots of the magnitude and phase of G, we provide a collection of typical transfer functions with their corresponding Bode plots in Table 4.3. These plots indicate the gain and phase margins.

Another important tool for analysis and synthesis of linear control systems, usually attributed to Evans, is known as the "Root Locus" method. As with the frequency response methods, its importance derives from the fact that it helps provide insight into the significant aspects of any particular system. It is not restricted to direct feedback systems nor to systems with open loop poles and zeros in the left half plane.

It is recalled that for any closed-loop system with "degenerative feedback" see Fig. 4.2, the closed-loop transfer function is

$$\frac{C}{R} = \frac{G}{1 + GH} \tag{4.2}$$

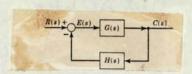


Fig. 4.2: Block diagram of a basic feedback control system.

The closed-loop response is determined by the roots of the denominator, i.e., the characteric equation. The roots must all be in the left half plane in order that the system be stable. Furthermore the time-domain design parameters, such as peak time maximum overshoot, damping factor, and settling time, are initimately related to the s-plane location of the roots of the characteristic equation of the control system, which are the poles of the closed-loop system function. Accordingly, a knowledge of how the roots of 1 + GH vary when the gain constant of GH varies should be of considerable assistance in understanding the system. A plot of the locus of the characteristic roots of the control system with the system loop gain as a parameter is commonly known as the root locus.

The design of feedback control systems by use of the root-locus method involves the reshaping of the root-locus plots by shifting or introducing open-loops poles and zeros. As a preliminary to the discussion of the design aspects, the effects of shifting open-loop poles and zeros are first indicated with the aid of examples in Table 4.3.

Gain Adjustment. When the preliminary analysis of a control system indicates that the system is unstable or that the over-all performance is inadequate, steps must be taken to improve the system performance. The most direct and simplest way of changing the performance is by the adjustment of the system gain.

Table 4.3

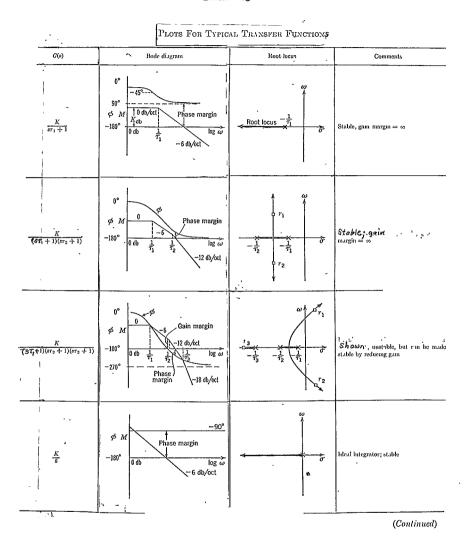


Table 4.3 (con't.)

$-18 \text{ db/oct}$ $-18 \text{ db/oct}$ $-90^{\circ} \phi M$ $-12$ $-6 \text{ db oct}$ $\text{margin}$ $\tau_2$ $\tau_1$ $\omega$	G(s)	Bode diagram	Root locus	Comments
Phase margin Gain margin $1/\tau_2$ $1/\tau$	K - s(3\tau_1 + 1)	φ M Phase margin -180° 0 db 1 log ω	$-\frac{1}{\tau_1}$	\$table, gain margin = ∞
Phase margin $S(s, r_1 + 1)$ $S(s, r_1 + 1)$ $S(s, r_2 + 1)$ $S(s, r_3 + 1)$ $S(s, r_4 + 1)$	K   S (5 (+ 1)(sr <sub>2</sub> + 1)	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c c} r_1 \\ \hline r_1 \\ \hline -\frac{1}{r_2} \\ -\frac{1}{r_1} \end{array}$	System is; stable as shown, but well become unstable with increased gain
Gain margin = 0 Phase	$\frac{K(sr_e+1)}{S\left(Sr_i+1\right)(sr_2+1)}$	$ \begin{array}{c c} -90 \\ \phi M \\ \hline -180^{\circ} \\ \hline 0 \text{ db} \\ \hline \frac{1}{71} \\ \hline \frac{1}{7a} \\ \hline -6 \\ \hline \end{array} \begin{array}{c c} \text{Phase margin} \\ \hline 0 \text{ db} \\ \hline \end{array} $	$\begin{array}{c c} r_1 \\ \hline \\ \hline \\ -\overline{r_2} \\ \hline \\ -\overline{r_2} \\ \hline \end{array}$	Above control system with phase-
		-12 db/oct φ	Double pole	Inherently unstable; must be compensated

Table 4.3 (con't.)

G(s)	Bode diagram	Root locus	Comments
$\frac{K}{\sqrt{s(sr_1+1)}}$	$ \phi M $ -180° $ 0 db \frac{1}{r_1} $ -270° $ 0 db \frac{1}{r_1} $ -18 db/oct	$\begin{array}{c} \omega \\ r_1 \\ Double \\ pole \\ \hline \\ r_2 \\ \end{array}$	Inherently unstable must be compensated
$\frac{K(s\tau_a+1)}{s^2(s\tau_1+1)}$	$ \phi M $ -180° $ \frac{1}{7} - 6 \frac{1}{7} $	$\begin{array}{c c} & \omega \\ & \gamma_1 \\ \hline \\ -\frac{1}{r_1} & -\frac{1}{r_a} \\ & \gamma_2 \\ \end{array}$	Stable for all gains
$\frac{K(s\tau_{s}+1)(s\tau_{s}+1)}{(+1)(s\tau_{s}+1)(s\tau_{s}+1)(s\tau_{s}+1)}$	-50° \$\delta M\$ \\ -180° \$\delta M\$ \\ -180°  \text{od} \\ \text{od} \text{od} \\ \text{od}	75 74 73 76 77 77 77 77 77 77 77 77 77 77 77 77	Conditionally stable; stable at low gain, becomes unstable as gain is raised, again becomes stable as gain is further increa-ed, and becomes unstable for very high gains
$\frac{K(s\tau_{o}+1)}{5^{2}(s\tau_{1}+1)(s\tau_{2}+1)}$	$\phi M$ -180° $0 \text{ db} \frac{1}{7_2}$	$\begin{array}{c c} & \omega \\ & r_1 \\ \hline & r_3 \\ \hline & -\frac{1}{\tau_2} \\ \hline & -\frac{1}{\tau_1} \\ \hline & -\frac{1}{\tau_2} \\ \end{array}$	Conditionally stable; becomes unstable at high gain
Pesign of Feedbac	f · · · from George J. Thaler and l k Control Systems, 2nd Ed., McGrav	Robert G. Brown, Analysis. y-Hill, New York, 1960.	

However, for most control systems the design specifications cannot be met by gain adjustment alone. The usual alternative is the introduction of compensating devices into the control system.

The adequate gain setting for a control system can be determined from the gain-phase plot of the system or from the Bode diagram of the system.

A change in system gain usually affects practically all of the system design parameters. For instance, an increase in system gain may cause a reduction of the system error, may increase the speed of response of the control system, and may make the system more oscillatory. The effects of gain variations upon the behavior of a control system are conveniently observed on the root locus plot of the control system also.

#### NASAP Output

For a given transfer function G with all the coefficients known, the frequency response is calculated by setting  $s = j\omega$  and simplifying the expression to a linear combination of real and imaginary terms:

$$G = A(\omega) + jB(\omega)$$
 (4.3)

The magnitude of G and the angle  $\theta(\omega)$  are computed according to the equations,

$$|G(j\omega)| = A^2(\omega) + B^2(\omega) , \qquad (4.4)$$

and

$$\theta(\omega) = \tan^{-1} \frac{B(\omega)}{A(\omega)} . \tag{4.5}$$

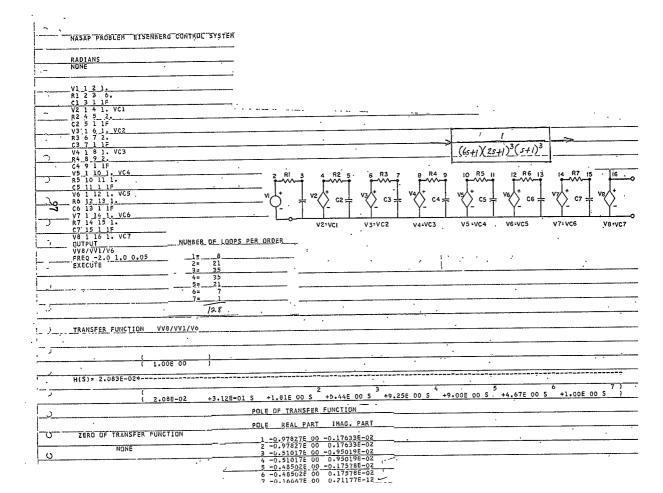
Now if  $\omega$  is made to vary, then for each value of  $\omega$  the  $|G(j\omega)|$  and  $\theta(\omega)$  can be obtained over the frequency range of interest and thus can be made available for plotting. With the complex arithmetic capability of FORTRAN IV, these computations are easily done in NASAP. The Bode plot consists of the  $|G(j\omega)|$  in decibel units and  $\theta(\omega)$  in degrees versus the  $\log_{10}\omega$ , taken over the frequency range specified

by the user.

To obtain a root locus plot for a control system, Fig. 4.2, it is required to find the values of s for which GH = -1 (or 1 + GH = 0). For this it is necessary that the angle of the complex number, GH, be 180 degrees and the magnitude of GH be unity. Thus, the complex number, s, must be selected so that the angle of the complex number, GH, is 180 degrees. When such a complex number for s is determined, a value of gain K can then be found which will make the magnitude of GH unity, although this value of K might not necessarily be the same as the value specified in the transfer function. However, after a locus of values of s for which GH = 180 degrees has been found, somewhere along this locus one can find a number that yields |GH| = 1 for the specified value of K. NASAP furnishes the necessary data in tabulated form to obtain the locus of points for which GH = 180 degrees. To obtain the root locus plot directly by the computer requires an extra program that will not be described here. Such programs are available in the literature as illustrated by Program D91RTL by Vernon [Appendix I in VE 1] and another by Krall and Fornaro [see KR 1 or KR2].

An alternative approach is to use the root sensitivity data available from NASAP to approximate the root locus plot. Such sensitivity data for an aerospace control problem is given in Chapter VI.

As an illustration of the open loop Bode plot output of NASAP we use a control system plant whose transfer function has a seventh degree polynomial denominator. The NASAP print out is shown in Fig. 4.3. This Eisenberg control problem [EI 1] is discussed further in Chapters V and VII.



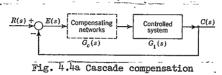
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#### IVC USE OF COMPENSATION

When the desired behavior of a control system cannot be obtained by the gain adjustment alone, compensation techniques must be used. Compensation means to improve the system performance by reshaping the open-loop transfer function characteristic of the system. The compensation of a control system can often be accomplished either by an element in series with other components as shown in Fig. 4.4a or by an element in parallel with one or more components



to form a subsidiary loop, as shown in Fig. 4.4b. The former arrangement is referred to as cascade or series compensation and the latter is called feedback or minor-loop compensation. A compensator or compensating device can

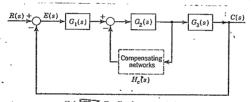


Fig. 4.4b Feedback compensation

stabilize a system which is unstable for all values of gain; it can improve both the transient and the steady-state performance of a system; and it can reduce the system error. Compensators are classified according to their operating characteristics into phase-lead (differentiating) type, phase-lag (integrating) type, and lag-lead (integro-differentiating) type. An example of the latter was given at the end of Chapter 3. The phase-lead type of compensator is generally used to modify the high-frequency portion of the open-loop transfer function plot and to improve the transient behavior of the system,

whereas the phase-lag type of compensator is often used to alter the low-frequency portion of the open-loop plot and to improve the steady-state performance of the system. The lag-lead compensation gives results intermediate between these two extremes. By proper adjustment of time constants, considerable flexibility of control system characteristics may be obtained.

Th choice of a method of compensation generally depends upon the specific system involved, the available components, cost considerations and the designers's experience and judgment.

The most commonly used configuration for compensation is shown in Fig. 4.4a. The procedure to compute  $G_{\mathbb{C}}(s)$  is to first compute the open loop transfer function and then compute  $G_{\mathbb{C}}(s)$ . There are two disadvantages in using this configuration. First if the overall open loop transfer function  $G_{\mathbb{F}}(s)$  is not properly chosen, the compensator computer in this manner may not be realizable as a RC network. Second, it generally requires pole-zero concellation. In system theory terminology, it means that some poles of the overall system are uncontrollable and/or unobservable. This poses a design problem in that these poles are dictated by the given plant  $G_{\mathbb{F}}(s)$  and cannot be controlled by the designer.

The feedback compensation, shown in Fig. 4.4b, is sometimes superior to \_\_\_\_ cascade compensation in that variation of the parameters of the system components bridged by the feedback elements of the minor loop have less effect upon system performance if the minor-loop gain is made sufficiently large and if the parameters of the feedback compensator do not vary. Although the freedom in choosing G<sub>1</sub>(s) and H<sub>c</sub>(s) is greatly increased, the difficulties encountered in Fig. 4.4a may still occur. Therefore the series and shunt compensation are not always applicable in practice.

Consider the configuration of compensators introduced by Chen [CH 1]. This is shown in Fig. 4.5, where k is a constant gain,  $C_1(s) = \frac{N_1(s)}{D_1(s)}$  and

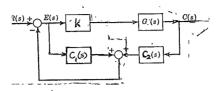


Fig. 4.5 Chen's Control System Configuration

 $\begin{array}{l} {\rm C_2(s)} = \frac{{\rm N_2(s)}}{{\rm D_2(s)}} \quad {\rm are \ proper \ rational \ functions \ with \ the \ dgree \ of \ polynomials} \\ {\rm D_1(s), \ D_2(s) \ and \ N_2(s) \ equal \ to \ n-1 \ and \ that \ of \ N_1(s) = n-2.} \end{array}$  This control system configuration has the overall transfer function

$$G_{f}(s) = \frac{kG(s)}{1 + C_{1}(s) + kC_{2}(s) G(s)}$$

$$= \frac{kND_{2} D_{1}}{D D_{1} D_{2} + N_{1} D_{2} D + kN_{2} N D_{1}}$$
(4.6)

If the denominators of  $C_1(s)$  and  $C_2(s)$  are chosen to be the same, that is  $D_1(s) = D_2(s)$ , then the last equation reduces to

$$G_{\hat{\mathbf{f}}}(s) = \frac{kND_1}{DD_1 + N_1D + kN_2N}$$
 (4.7)

It can be shown that by using this system configuration the compensators can be always chosen to be realizable by RC networks and the cancelled poles can also be controlled by the designer [see CH 1]. It is worth noting that the complexity of compensators in the system of Fig. 4.5 is comparable to that required for the compensator of the corresponding control system based on the configuration of Fig. 4.4a.

## Examples

An example of cascade compensation was included at the end of Chapter III (refer to Figs. 3.16 and 3.17). Here we provide the Bode plots in Figs. 4.6 and 4.7 for the uncompensated as well as the compensated case respectively to facilitate comparisons.

Next we illustrate basic feedback compensation with the aid of two examples having the configuration shown in Fig. 4.8. The feedback function  $\mathbf{H_c}$  is used to modify the characteristics of the plant G, while the cascade function  $\mathbf{G_c}$  is provided to aid in adjusting the performance of the major loop. Often the cascade compensation  $\mathbf{G_c}$  is a simple gain factor used to adjust the degree of stability of the system. The burden of modifying the transfer function G is placed on the feedback compensation  $\mathbf{H_c}$ . In addition, the feedback function is usually provided with an adjustable gain factor to permit setting the degree of stability of the minor loop.

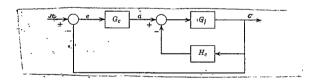


Fig. 4.8 General arrangement for feedback compensation.

The procedure for adjusting the feedback compensation can be based on the magnitude asymptotes of the minor loop. In the frequency ranges where the open-minor-loop frequency-response magnitude  $|G(j\omega)|H_C(j\omega)|$  is very large, the closed-minor-loop response  $|c(j\omega)/\alpha(j\omega)|$  behaves like the reciprocal of the feedback compensation. When the open-minor-loop response magnitude is very small, the closed-minor-loop response behaves like the plant.

The feedback compensation is used primarily to improve the dynamic behavior

of the plant in the mid-frequency range without altering the high gain of the plant at low frequencies. A high-frequency boundary will always exist since in any practical case the magnitude of  $G(j\omega)$   $H_c(j\omega)$  will become less than unity as frequency increase.

The procedure for adjusting the feedback function  $H_c$  and the cascade gain factor  $[G_c(s) = K_c]$  can thus be roughed out by means of asymptotic plots of the pertinent responses and then carried out in detail by means of the gain-phase or Bode plots. The asymptotic plots enable one to examine the form of the closed-minor-loop response as the feedback compensation is adjusted.

Since there are usually several parameters to adjust in the feedback compensation procedure, the process of design is one of trial and error.

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	-0.500021vE-01	0.79432409 00 0.8912466E 00	-0.1851054± 01 -0.2293255€ 01	-0.1374878E 03 -0.1418157E 03	0.8080658E 00	-0.9255320E-01
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1	0.5999975E_00	_0.3981049E_01_	O.2BO1645t_02	0.15557336 03	0.39735291-01	-0.1400823E 01
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J .	0.7499971E 00	0.56733768 01	-0.3530406E 02	U-1417252E 03	0.17171116-01	-0.17652010 01
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	100160501	FREQ	20.*LDG(AB5(H))	PH1(H)	ABS (H)	LDG(ABS(H))
	LOG(FREQ)	0.1000001E 00	0.8/77428E-01	-0.1781549E 02	0.1010157E 01	0.43887158-02
	· -:.9999996E 00		0.1081116E 00	-0.2008299E 02	0.1012525E UL	0.54055826-32
	-6.9499797E 00	0.1122019E 00		-0.2266541E 02	0.10153448 01	0.66130615-02
	-1. 89997976 00	0.12589266 00 /	0.1355915F 00	-0.2561649E 02	0.10186278 01	0.80152536-02
	-0.8499998E 00	0.1412538E 00	0.16030506 00		0.10223276 01	0.9590007E-02
	-0.7999598E UO	0.1584894E 00	0.1918001E 00	-0.2900237E 02	0.1026269E 01	0.1120119E-01
	-0.7499999E 00	0.1778280E 00	0.225223dE 00	-0.3290480E 02	0.10300508 01	0.12858421-01
	-0.6999y99E 00	0.19952636 00	0.2571684E 00	-0.3742506E 02		0.1404057E-01
	-0.6500000E 00	0.2238/21E 00	0.2808114E 00	0.4268726E 02	0.1032858E 01	
	-0.6000C00E 00	0.2511886E 00	0.2836820E 00	-U.4883908E 02	0.1033199E 01	0.14184106-01
	-0.5500001E 00	Q.2818382E 00	0.2441459E 00	-0.5604611E 02	0.1028507E 01	0.12207356-01
	-0.5000001E 00	0.31622/72 00	0.12717/1E 00	-U+6446948E 02	0.1014750E 01	0.63588546-02
	-0.4500002E 00	0.3548133E 00	-0.1194394E 00	-0.7421626E 02	0.98634316 00	-0.59719688-02
	-0.4000002E UO	0.3981070E 00	-0.5638217E 00	-0.85255831 02	0.9371495E 00	-0.2819109E-01
1	-0.0500003E 00	0.4466833E.00	-0.1277848E 01	-0.9733092E 02	0.863T923E 00	-0.6389242E-01
	-0.5000003E 00	0.5011868E 00	-0.23127/3E 01	-0.1099373E 03	0./662337t UO	-0.1156387E 00
	-0.2500004E UO	0.5623409E 00	-0.36/5883E 01	-U-1244468E 03	0.6549464E.00	-0.1837942E 00
	-0.2000004E 00	0.6309568E 00	-0.5328104E 01	-U-1343181E 03	0.5414953E UU	-0.1837942E 00 -0.2664052E 00
	-0.1500005E 00	0./079450E 00	-0.7204965E 01	-0.1452428E 03	0.4362663E 00	-0.3602483E 00
	-0.1000005E 00	0.1943273E 00	-0.9242250t 01	-0:1551485E 03	0.3450542E UO	-0.4621125E JO -
	-0.5000U55E-U1	0.8912498E 00	-0.1139055E 02	-0.1641129E 03	0.2694461E UO	-0.5695277E UO
	-0.5960464E-06	0.9999986E 00	0.13o1802E 02	-U.1722763E 03	0.2084963£ 00	-0.6809011E 00
	0.49998648-01	0.1122015E 01	-0.1590686E 02	-0.1797832E 03	0.1601979E UU	-0.7953428E 00
	0.9999JBJE~01	0.1258922E 01	-0:1824892E 02	U•1732430E 03	0.1223359E UO	-0.9124460E 00
,	0.1499/90E 00	0.1412535E 01	-0.2064151E 02	0.1667096E 03	0.9288013E-UI	-0.10320766 01
	0.1999992E UO	0.1584890E 01	-0.2308481E 02	0.1605530E 03	0.7010663E-01	-0.1154241E 01
	0.24999856 00	0.1//8273E 01	-0.2557968E 02	U.1547348E 03	0.5260354E-01	-0.1278984E 01
•	0.29997B6E 00	0.1995456E 01	-0.2812703E 02	0.1492349E 03	0.3923260E-UL	-0.1406352E 01
	0.3499988E 00	0.2238/15E 01	-0.3072656E 02	U.1440467E 03	0.2908516E-U1	-0.1536328E 01
	0.3999990E 00	0.2511881E 01	-0.3337682E 02	0.1391703E 03	0.2Î43671E-01	-0.1668841E 01
	0.4499983E 00	0.28183728 01	-0.3607518E 02	0.1346091E 03	0.1571231E-01	-0.1803760E 01
	0.49999856 00	0.31622678 01	-0.3881822E 02	U.130365ZE 03	0.1145746E-U1	-0.1940911E 01
	0.5499986E 00	0.3548122E 01	-0.4160159E 02	U.1264381E 03	0.8316088E-02	-0.2080080E 01:
	0.5999786E 00	0.3981061E 01	-0.4442075E 02	U:1228238E 03	0.6Ó11199E-UZ	÷0.2221038E 01
	0.6499981E 00	0.4466816E 01	0.4727100E 02	0.1195136E 03	0.4329611E-02	-0.2363550E 01
	0.69999836 00	0.5011852E 01	-0.5014796± 02	U.1164955E 03	0.3108854E-02	-0.2507399E 01
	0.74999856 00	0.5623393E 01	-0.5304749E 02	0:1137542E 03	0.2226512E-02	-0.2652374E 01
	0.7999986E 00	0.6309554E 01	-0.5596584E 02	0.1112729E 03	0.1591134EU2	-0.2798292E 01
	0.8499979E 00	0.7079423E 01	-0.5889972± 02	0.1090334E 03	0.1135043E-02	-0.2944986E 01
	0.8999981E 00	0.7943247E 01	-0.6184648£ 02	0.10/0167E 03	0.80848976-03	-0.3092324E 01
	0.94999831 00	0.8912474E 01	-0.6480367E 02	0.1052044E 03	0.5751951E-03	-0.3240184E 01
		0.99999455 01	-0.6776936E 02	U.1035783E 03	0.40881876-03	-0.3388469E 01
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This example, shown in Fig. 4.9 along with its NASAP circuit model, is taken from Newton Gould and Kaiser [NE 1 pp. 326-333]. One finds that the magnitude plot of the closed loop transfer function shows no sign of resonance effects so that a reasonable closed-loop performance may be expected. The corresponding phase curve is given in Fig. 4.10.

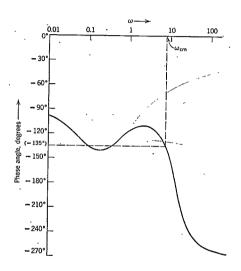


Fig. 4.10 Closed-minor-loop phase-angle response.

Using the  $45^{\circ}$  phase-margin criterion to adjust the cascade compensation, the magnitude crossover frequency of the major loop is found to be

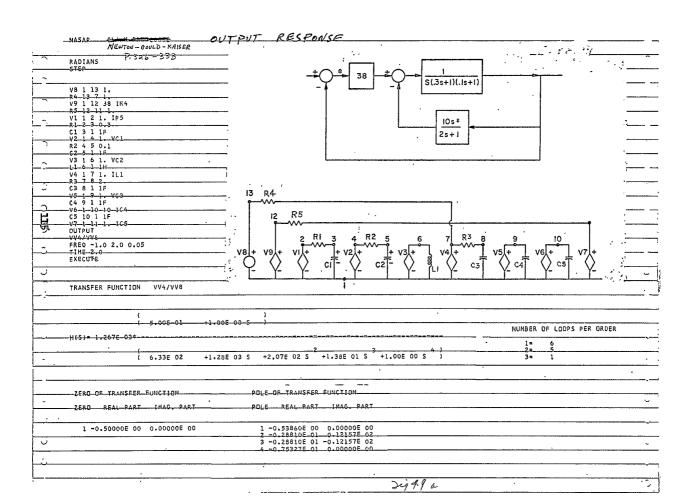
$$\omega_{\rm cm} = 7.7 \text{ rad sec}^{-1}$$
 (4.8)

and the corresponding gain factor of the cascade compensation is

$$K = 38 \tag{4.9}$$

If this control system exhibits undesirable performance because of the lag-compensation effect in the open-major-loop response at low frequencies, some

improvement can be expected by decreasing the feedback compensation time constant  $T_c$  and by some increase in the minor-loop gain factor  $K_c$ . The degree of improvement achievable must be ascertained by further NASAP runs. Further discussion of this example is found in Chapter V including step response and error response for the control system with its gain K=38.

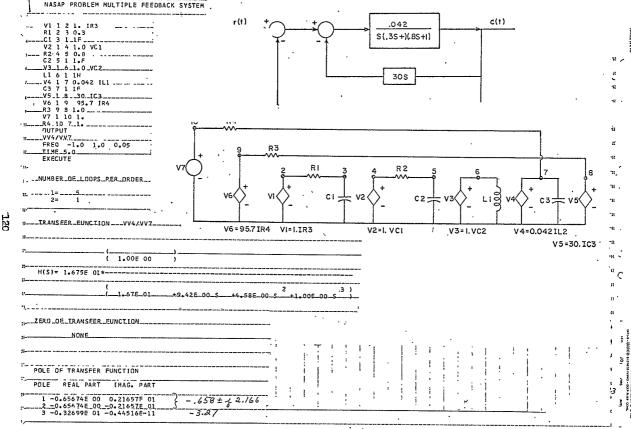


٠.	LDG(FREQ)	FREQ	20.*LDG(ABS(H))	PHI(H) 0-1298571E 03	ABS(H) 0.4107933E-02	LOG(ABS(H)) -0.2386375E 01
	-0.9999996E-00 -0.9499997E 00	0.1000001E 00 0.1122019E 00	-0.4772751E 02 -0.4613454E 02	0.1317182E 03	0.4934825E-02	-0.2306727E 01
	0.8999997E-00	0.12589266-00-	-0-4449901E-02-	0.1333188E_03	0.5957287E-02	-0.22249515 01
	-0.8499998E 00	0.1412538E 00	-0.4282719E 02	0.1346163E 03	0.7221695E-02 ·	-0.2141360E 01 -0.2056322E 01
	-0.7999998 00 -0.7499998 00	0.15848946 00 0.1778280E 00	-0.3940480E 02	0.1361707E 03	0.1070923E-01	-0.1970241E 01
<u> </u>	-0.6999996-00-	_0.1995263E_00_	0.37670906_02	0.1363828E_03	0.1307537E-01_	-0.18835456-01
	-0.6500000E 00	0.2238721E 00	-0.3593353E 02	0.1362026E 03 0.1356290E-03	0.1597067E-01 	-0.1796677E 01 0.1710078E-01-
÷	-0.5500001E 00		-0.3470155E-02- -0.3248387E 02	0.1346695E 03	0.2375774E-01	-0.1624194E 01
	-0.5000001E-00	0.3162277E-00-	0.3079895E-02-	0.1333401E 03	0.2887696E-01	-0.1539468E-01
$\hat{}$	-0.4500002E 00	0.3548133E 00	-0.2912479E 02	0.1316652E 03	0.3497519E-01 	-0.1456240E 01 0.4374929E-01-
	-0.3500003E 00	0-3981070E00 0.4466833E 00	-0.2749858E-02- -0.2591649E 02	0.1296771E 03 0.1274155E 03	0.5060278E-01	-0.1295825E 01
<u> </u>	-0.30000C3E-00-	-0.501-1868E-00-	0.2438327E_02_	0.1249259E_03	0.6037195E=01	-0.1219164E-01
,	-0.2500004E 00	0.5623409E 00	-0.2290211E 02	0.1222572E 03 0.1194587E 03	0.7159674E-01 0.8438689E-01	-0.1145106E 01 -0.1073724E 01
	-0.20000045 00 -0.1500005E 00	0.6309568E 00 - 0.7079450E 00	-0.2010020E 02	0.1165779E 03	0.9885269E-01	-0.1005011E 01
	-0.1000005E-00	0.79432736 00	-0.1877763E-02	0.1136571E_03	0.1151111E_00_	-0.9388824E-00-
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) '	-0.5960464E-06 0.4999864E-01	0.9999986E 00 0.1122015E 01	-0.1627541E_02 -0.1508801E 02	0.1049658E 03	0.1760352E 00	-0.7544003E 00
	0.9999888E-01	0.1255922E_01_	-0.1393749t 02	0.1021536F 03	0.2009673E 00	-0.6968746E 00
3	0.1499990E 00	0.1412535E 01	-0.1281991E 02	0.9939413E 02	0.2285621E 00	-0.6409953E 00 -0.5865864E 00
		0.1778273E 01	-0.1173173E-02 -0.1066996E 02	0.9668375E-02- 0.9401411E 02	0.25906776 00 0.2927532E 00	-0.5334982E 00
<del>~</del>	0.29999865 00	0.1995256E_01	-0.9632131E_01_	0.9137375E 02	0.3299083E 00	-0.4816065E-00
) <b>F</b>	0.3499988E 00	0.2238715E 01	-0.8616458E 01	0.8874956E 02 0.8612885E 02	0.3708318E 00 0.4158328E 00	-0.4308229E 00
- 9	0.3999990E 00 0.4499983E 00	0.25118818 01 0.2818372E 01	-0.7621623E 01 -0.6646667E 01	0.8349980E 02	0.4652288E 00	-0.3323334E 00
<u>:                                    </u>	0.4999985E_00	0.3152267E_01	0.56906.76E-01	0.8085335E_02	0.5193572E 00	-0.2845338E 00
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	0.5999988E 00 0.6499981E 00	0.4466816E 01	-0.3829819E 01 -0.2918818E 01	0.7277647E 02	0.7145935E 00	-0.1459409E 00
	0.4999983E 00	0.5011852E_01	-0-2012150E-01	0.7004272E 02	0.7932178F 00	-0.1006075E 00
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	0.8499979E 00	0.7079423E 01	0.6508540E 00	0.6148209E 02	0.1102917E 01	0.4254270E-01
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٠	0.9499983E 00 0.9999985E 00	0.8912474E 01 0.9999965E 01	0.3245031E 01 0.4707366E 01	0.5350861E 02 0.4633690E 02	0.1452953E 01 0.1719366E 01	0.1622516E 00 0.2353683E 00
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	0.1249997E 01	0.1778268E 02	0.2276337E 01	-0.8603992E 01	0.1299622E 01	0.1138169E 00
	0.12999975-01	0.1995250E-02	0.1364489E 01	-0.7533766F 01	0.1170104E 01	0.6822443E=01
	0.1349998E 01 0.1399998E 01	0.2239708E 02 0.2511873E 02	0.8104062E 00 	-0.5898328E 01	0.1097793E 01 0.1057132E 01	0.4052031E-01 0.2412912E-01
	0.1449997E 01	0.2818362E 02	0.2894126E 00	'-0.3187364E 01	0.1033881E 01	0.1447063E-01
	0.1499997E 01	-0.3162257E-02-	0.1749709E-00	-0.2285169E-01	0.1020349E 01 0.1012348E 01	0.8748546E=02 0.5329899E-02
	0.1549997E 01 0.1599998E-01	0.3548112E 02 -0.3981049E 02	0.1065980E 00 -0.6536704E-01	-0.1627623E 01	0.1012348E 01 0.1007554E 01	0.3268354E-02
	0.1649997E 01	0.4466803E 02	0.4031325E-01	-0.8180165E 00	0.1004652E 01	0.2015662E-02
	0.1699997E 01	0.5011838E 02	- 0.2496372E-01	-0.5795133E 00 -0.4100884E 00	0.1002878E 01 0.1001788E 01	0.1248186E-02 0.7758853E-03
	0.1749997E 01 0.1799997E 01	0.5623376E 02 -0.6309535E 02	0.1551770E-01 	-0.4100884E 00	0.10017882 01	0.7738833E-03 0.4839012E-03
٠	0.1849997E 01	0.7079402E 02	0.6044853E-02	~0.2052789E 00	0.1000696E 01	0.3022428F-03
	0.1899997E 01	0.79432245 02	0.3776457E-02	-0.1452416E 00 -0.1027696E 00	0.1000435E 01 0.1000273E 01	0.1888229E-03 0.1184380E-03
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The configuration of the second multiloop example is also similar to that shown in Fig. 4.8. In this case however the  $G_{\rm c}$  block is simply a direct connection as shown in Fig. 4.11. Figures 4.11a through 4.11f include the NASAP printout of the Bode plots and the step response.



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LOG(FREQ)CREQ20.*LOG(ABS(H))PHI(H)ABS(H)LOG(ABS(H))	<sub>4</sub> C +1
-0.9999995E 00  0.1000001F 00  0.4088327E 00  -0.2078052E 02  0.1048194E 01  0.2044164E-01	
	:
-0.899997E 00 0.1258928E 00 0.6587968E 00 -0.2661081E 02 0.107879TE 01 0.3293984F-01 -0.9649997F 00 0.1412539E 00 0.389407TE 00 -0.3024033E 02 0.110133TE 01 -0.412039T-01	
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### CHAPTER, V

### CONTROL SYSTEMS ANALYSIS IN THE TIME DOMAIN

## VA INPUT SIGNALS FOR TIME RESPONSE

The impulse function is the basic tool for analysis and synthesis of linear systems. However specifically for the study of linear control systems the unit step function response is the most widely used with the unit impulse and the unit ramp functions also commonly used as test inputs.

We note in passing that these three functions are related to each other by one or more integrations or differentiations. For example the unit ramp as a function of time is the integral of the unit step function. On the other hand the unit impulse may be regarded as the derivative of the unit step function (this concept is adequate for the purposes of this manual even though this derivative does not exist in the sense of calculus).

One of the first steps in adapting NASAP to control system design was to investigate the feasibility of incorporating additional input functions. This is discussed next.

# VB ADDITIONAL INPUTS FOR CONTROL APPLICATIONS

Although the NASAP 69/I package provides the time response of the output only for an impulse excitation, the time response subroutine INV of NASAP can easily be extended to the other basic input signals often used in control theory. The necessary additions to NASAP incorporate the step and ramp excitations are given in Appendix A.

The algorithm used by NASAP to determine the residues of the poles of the transfer function assumes that the poles are simple. This poses no problem since the root-finding subroutine of NASAP will not find double or higher roots but will locate a number of simple roots furthe neighborhood of the actual higher order root location. Thus for an actual double root on the negative  $\sigma$ -axis, say at

$$s_{1,2} = -a,$$

the root finding algorithm of NASAP will indicate complex root pair at

$$s_{1,2} = a + jb$$

where the imaginary parts of  $s_{1,2}$  are extremely small in comparison to the real part. Thus while the analytic time response for a system with higher order poles will not be correct, strictly speaking, the table and plot of discrete time values will be sufficiently accurate for practical purposes.

Given a rational transfer function

$$\widetilde{H}(s) = \frac{C(s)}{R(s)}$$
 (5.1)

and the Laplace transform of the excitation R(s), the Laplace transform of the output can be expressed

$$C(s) = H(s)R(s)^{\frac{1}{2}}$$

Then, by finding the residues of the poles of H(s)R(s), the time response of the output c(t) is readily obtained.

If the excitation is an impulse function, R(s) = 1, then the Laplace transform of the output C(s) is numerically equal to the transfer function H(s). This is method used by NASAP to find the impulse response. Once the

transfer function and its poles have been determined, all that is necessary to find the corresponding time response of the output is to calculate the residues of the poles of the transfer function.

However, if the excitation is a unit step,  $R(s) = \frac{1}{s}$ , then the poles of the Laplace transform of the output are the poles of transfer function H(s) in addition to a pole at the origin. If H(s) has no higher order poles and no pole at the origin, then the analytic expression and the tabular values of the output will be correct. Note that the residue of the pole at the origin is the steady-state value of the output. If H(s) has higher order poles but no pole at the origin, then even though the analytic expression for the output as determined by NASAP will be somewhat in error, the tabular values will be correct. If H(s) does have a pole at the origin, then the results obtained from NASAP for a step response will be in error and will . probably cause premature termination of the execution due to division by zero. This can be seen as follows:

Given 
$$H(s) = \frac{K(s+a_1)(s+a_2) \dots (s+a_m)}{s(s+b_1)(s+b_2) \dots (s+b_n)}$$
 (5.3)

Then

$$C(s) = \frac{1}{s} \frac{K(s+a_1)(s+a_2)...(s+a_m)}{s(s+b_1)(s+b_2)...(s+b_n)}$$
 (5.4)

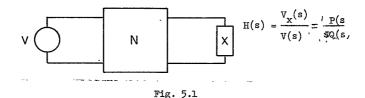
when  $R(s) = \frac{1}{s}$ .

The residue at the pole at  $s = b_1$  can be found by

Res(s - b<sub>1</sub>) = (s + b<sub>1</sub>) C(s) 
$$\Big|_{s=b_1}$$
  
=  $\frac{1}{-b_1} \frac{K(a_1-b_1)(a_2-b_1)\dots(a_m-b_1)}{-b_1(b_2-b_1)\dots(b_n-b_1)}$  (5.5)

Since the algorithm used in NASAP cannot indicate double poles, it assures two distinct poles at the origin. When the algorithm proceeds to determine the residue of one of these poles at the origin, the presence of the other pole at the origin causes the denominator of (3) to go to zero and thus the

residue approaches infinity. This situation can be avoided by the addition of some elements to the original circuit to put a zero at the origin and thereby determining the ramp response of this new network. In Fig. 5.1 is given a two port network N with a source V (either an independent current or voltage source) and an element x whose voltage is the required output quantity. The transfer function of this network has a pole at the origin and it is required to find the response of the voltage across the element x to a unit step excitation.



Now consider the modification of the network in Fig. 5.1 shown in Fig. 5.2.

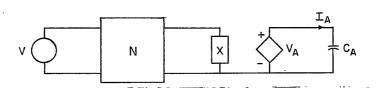


Fig. 5.2

where  ${\tt V}_{\!A}$  is a dependent voltage source whose voltage equals that across the element x and  ${\tt C}_{\!A}$  is a one farad capacitor. Now

$$\frac{I_{A}(s)}{V(s)} = \frac{sC_{A}V_{A}(s)}{V(s)} = \frac{sV_{A}(s)}{V(s)}$$
(5.6)

But

$$V_A(s) = V_X(s)$$

so that

$$\frac{I_{\underline{A}}(s)}{V(s)} = \frac{sV_{\underline{X}}(s)}{V(s)} = \frac{sP(s)}{sQ(s)} = \frac{P(s)}{Q(s)}$$
(5.7)

Thus the pole at the origin is effectively eliminated. The response of  $\dot{\textbf{1}}_{a}(t) \text{ to a ramp input is equivalent to the response of } \textbf{v}_{x}(t) \text{ to a step input.}$ 

A similar method can be used if the output quantity is a current through an element x. In this case  $V_A$  is a dependent voltage source whose voltage equals the current through the element x.

If the excitation is a ramp, r(t) = t, then  $R(s) = \frac{1}{s^2}$ . Thus the poles of the Laplace transform of the output are the poles of H(s) in addition to the double pole at the origin. As noted earlier the algorithms of NASAP can only approximate double poles. To illustrate this assume that the double pole at the origin is approximated by a complex pole pair located on the j axis a distance)  $\alpha$  if from the origin. Thus

$$R(s) = \frac{1}{(s+j\alpha)(s-j\alpha)}$$
 (5.8)

partial fraction expansion yields

$$R(s) = \frac{1}{2j \alpha} \left[ \frac{1}{s-j \alpha} - \frac{1}{s+j \alpha} \right]. \tag{5.9}$$

Taking the inverse Laplace transform yields

$$r(t) = \frac{1}{2j\alpha} \left( e^{j\alpha t} - e^{-j\alpha t} \right) = \frac{1}{\alpha} \sin \alpha t$$

$$= -\frac{1}{2} \frac{1}{2\alpha} e^{j\alpha t} + j\frac{1}{2\alpha} e^{-j\alpha t}$$
(5.10)

However if  $\alpha t$  is small, sin  $\alpha t$  can be approximated by  $\alpha t$  . Thus  $i(t) \not\approx t \qquad \text{if} \ \alpha t \ << 1 \quad \text{or} \quad t << \frac{1}{\alpha} \ .$ 

Thus the smaller of is, the larger the range of time values for which the approximation closely resembles a ramp input.

Note that the coefficients of the exponential terms in (5.10) are conjugate imaginary. However, in general, these coefficients will be complex conjugate. The significance of this is now demonstrated. Let us assume that the coefficient of  $e^{j \alpha t}$  is A-jB while that of  $e^{-j \alpha t}$  is A+jB. Thus we have

$$(A-jB)e^{j\alpha t} + (A+jB)e^{-j\alpha t} = A(e^{j\alpha t} + e^{-j\alpha t}) - jB(e^{j\alpha t} - e^{-j\alpha t})$$

$$= 2A \cos \alpha t + 2B \sin^{2}\alpha t \qquad (5.11)$$

Now let

$$2A = M \sin \theta$$
 (5.12)

$$2B = M \cos \theta' \tag{5.13}$$

Substituting (5.12) and (5.13) into (5.11) and then simplifying yields

$$(A-jB)e^{j \sigma t} + (A+jB)e^{-j \sigma t} = M\sin (\alpha t + \theta)$$
 (5.14)

where

$$M = 2\sqrt{A^2 + B^2}$$
 (5.15)

and

$$\Theta = \tan^{-1} \frac{A}{B}$$
 (5.16)

Now if A << B, then (5.15) and (5.16) can be approximated by

$$M \approx 2B$$
 (5.17)

$$\Theta \approx \frac{A}{B}$$
 (5.18)

Since  $\theta$  and  $\alpha$  are both small, there is a range of values of t where the approximation

$$sin(\alpha t + \theta) \approx \alpha t + \theta$$

is valid. Thus

$$(A-jB)e^{j \alpha t} + (A+jB)e^{-j \alpha t} \approx 2 \alpha Bt + 2A$$
 (5.19)

for A << B which represents a ramp with slope 2  $\alpha\,B$  plus a step function of magnitude 2A.

If the constant A is zero, then the above equations approximates only a ramp of slope 2  $\alpha B$ . This agrees with equation (5.10). On the other hand, if A >> B, then (5.15) and (5.16) can be approximated by

$$\theta \approx \frac{\pi}{2}$$
.

Thus  $\sin(\alpha t + \phi) \cong \sin(\alpha t + \frac{\pi}{2})$  cos  $\alpha t$ . Since  $\alpha t$  is quite small for a wide range of time values, then

cos at ≈ :

This results in

$$(A-jB)e^{j\alpha t} + (A+jB)e^{-j^{1}\alpha t} \approx 2A$$
 (5.20)

where A >> B which represents a step function of magnitude 2A.

A simple example will illustrate these points. In Fig. 5.3 is the block diagram of a plant whose transfer function is known. It is required to determine the output c(t) for a ramp input of unit slope.

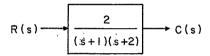


Fig. 5.3

Thus

$$C(s) = \frac{2}{s^2(s+1)(s+2)}.$$
 (5.21)

By partial fraction expansion and the inverse Laplace transform, one can obtain the exact solution

$$c(t) = t - \frac{3}{2} + 2e^{-t} - \frac{1}{2}e^{-2t}$$
 (5.22)

In Fig. 5.4 is the equivalent circuit model for the plant given in Fig.

5.3 for computer analysis with NASAP.

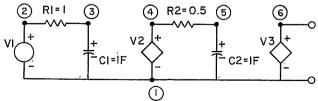


Fig. 5.4: Circuit Model for Fig. 5.3

V1 = input r(t) V2 = VC1 V3 = VC2 = output c(t)

Desired Transfer Function VV3/VV1.

Since the ramp response is desired, the NASAP program will evaluate the residues of the poles of the function

$$C(s) = \frac{2}{(s+j\alpha)(s-j\alpha)(s+1)(s+2)}$$
 (5.23)

$$Res(s = -1) = \frac{+2}{1+\alpha^2} \approx +2$$

Res(s = -2) = 
$$\frac{-2}{4+8}$$
  $\approx -\frac{1}{2}$ 

Res(s = j 
$$\alpha$$
) =  $\frac{-j}{\alpha(1+j\alpha)(2+j\alpha)} \approx -\frac{j}{2\alpha}$ 

Res(s = 
$$-j\alpha$$
) =  $\frac{j}{\alpha(1+j\alpha)(2+j\alpha)} \approx \frac{j}{2\alpha}$ 

The computer results for the transient analysis of the circuit in Fig. 5.4 are given in Fig. 5.5. Note that for  $\alpha=0.001$ , the coefficient A and B are -0.75 and 500 respectively. Indeed B >> A and thus by use of (5.18) we obtain

$$c(t) = t-1.5$$
 for large t

which agrees with the exact results obtained from (5.22).

## NASAP RAMP RESPONSE

NONE
RAMP RESPONSE
V1 1 2 1
R1 2 3 1
C1 3 1 1F
V2 1 4 1 VC1
R2 4 5 0.5
C2 5 1 1F
V3 1 6 1 VC2
DUTPUT
VV3/VV1
TIME 1.5
EXECUTE

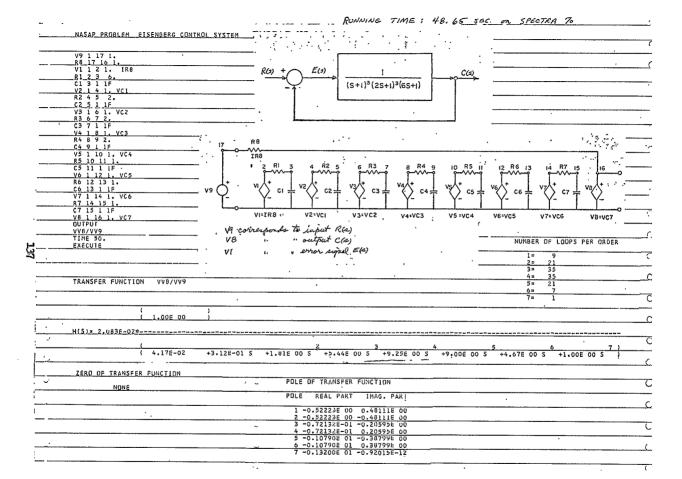
	TIME	VV3/VV1	
	0.0000E 00	-0,22649765E-05	
	0.3000E-01	0.57220459E-05	
1.00E 00	0.6000E-01	0.66041946E-04	
	0.9000E-01	0.22459030E-03	
H(S)* 2.000E 00*	0.1200E 00	0.52416325E-03	
• • •	0.1500E 00	0.10040998E-02 0.16986132E-02	
( 2 )	0.1800E 00 0.2100E 00	0.26420355E-02	
( 2.00E 00 +3.00E 00 S +1.00E 00 S )	0.2400E 00	0.38610697E-02	
	0.2700E 00	0.538194188-02	
	0.3000E 00	C.72265863E-02	
	0.3300E 00	0.94183683E-02	
ZERO OF TRANSFER FUNCTION	0.3600E 00	0.11973619E-01	
ZERU UF TRANSPER TONOTZEN	0.3900E 00	0.14907360E-01	
NONE	0.4200E 00	0.18234968E-01	
	0.4500E 00	0.21967888E-01	
	0.4800E 00	0.26117563E-01	
	0.5100E 00	0.30690789E-01 0.35696208E-01	
	0.5400E 00 0.5700E 00	0.41138569E-01	
POLE OF TRANSFER FUNCTION	0.6000E 00	0.47023952E-01	
POLE REAL PART IMAG. PART NUMBER OF LOOPS PER ORDER	0.6300E 00	0.53353786E-01	
POLE REAL PART IMAG. PART NUMBER OF LOOPS PER DRUER	0.6600E 00	0.60132444E-01	
1n 3 .	0.6900E 00	0.67359865E-01	
1 -0.10000E 01 0.00000E 00 . 2= 1	0.7200E 00	0.75038612E-01	
2 -0.20000E 01 0.00000E 00	0.7500E 00	0.83165944E-01	
2 -0.200002 01 0.00002 00	0.7800E 00	0.91742098E-01	
	0.8100E 00	0.10076451E 00	
	0.8400E 00	0.11023188E 00	
\	0.8700E 00	0.12014079E 00 0.13048774E 00	
	0.9000E 00	0.13046774E 00	
RAMP RESPONSE FUNCTION .	0.9300E 00 0.9600E 00	0.15248007E 00	
	0.9900E 00	0.16411662E 00	
F(T) =	0.1020E 01	0.17617333E 00	
(-0.1000E 01 J 0.0000E 00 ) T	0.1050E 01	0.18364465E 00	
( 0.2000E 01 J 0.4210E-09 ) E	0,1080E 01	0.20152563E 00 0.21481055E 00	
( 0.20002 01 3 0.42102-07 / 5	0.1110E 01	0.21481055E 00	
(-0.2000E 01 J 0.0000E 00 ) T	0.1140E_01	0.2284929BE 00	
(-0.5000E 00 J-0.5262E-10 ) E	0.11708 01	0.24256706E 00	
	Q.1200E_Q1	0.25702637E_00	
( 0.0000E 00 J 0.1000E-02 ! T	0.1230E 01	0.271864411 00	
(-0.7500E 00 J-0.5000E 03 ) E	0.1260E 01	0.28707469E 00 0.30265069E 00	
	0.1290E 01 0.1320E 01	0.31858605E 00	
( 0.0000E 00 J-0.1000E-02 ) T	0.1350E 01	0.33487368E 00	
(-0.7500E 00 J 0.5000E 03 ) E	0.1380E 01	0.35150689E 00	
	0.1410E 01	0.36847913E 00	
For &= 0.001	0.1440E 01	0.38578355E 00	
	0.1470E 01	0.40341347E 00	
A = -0.75	0.1500E 01	0.42136174E 00	
B>>A			
B = 500			
thus $2 \times Bt + 2A = t - 1.5$			
thus $2 \propto B t + \lambda A = t - 1.5$	,	A	
2455a			12/16/69

RAMP RESPONSE

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Although a few examples of NASAP printout of step response appeared earlier in this manual we include a specific example here. This step response is for the Eisenberg control problem shown previously in Fig. 4.3. The NASAP printout is shown in Fig. 5.6. We shall refer to this problem again in Chapter VII.

We are not including any examples of impulse response since all the previous references to NASAP only show such printouts.



STEP ' RESPONSE FUNCTION	. STEP RESPONSE			•
F(T) =	TIME	VV8/VV9		
1	0.0000E 00	0.11920929E-06		
(-0.5222E 00 J 0.4811E 00 ) T	0.1000E 01	0.26226044E-05		
(-0.7046E-01 J 0.1088E 00 ) E	0.2000E 01	0.16987324E-03		
/ 2 FRONT 20 / 0 / 0115 00 h TI	0.3000E 01	0.16793013E-02		,
(-0.5222E 00 J-0.4811E 00 ) T'	0.4000E 01	0.7393419/E-02 0.21032572E-01		
(-0.7040E-01 3-0.1000E 00 7 E	· 0.6000E 01	0.45632005E-01	•	
(-0.7213E-01 J-0.2060E 00 ) T	0.7000E 01	0.824/90001-01		
(-0.9572E-01 J-0.3404E 00 ) E	0.8000E 01	0.130899311 00		
	0.9000E 01	0.18865520E 00		
(-0.7213E-01_J`0.2060E_00_) T	0.1000E 02	0.252583566 00		
(-0.9572E-01 J 0.3404E 00 ) E	0.1100E 02	0.31920141E 00		
	0.120ÓE 02	0.38515985E 00		
(-0.1079E 01 J-0.3880E 00 ) T'	0.1300E 02	0.44752681L 00		
) (-0.5657E-01 J-0.4702E-01 ) E	0.1400E 02 0.1500E 02	0.50393325E 00 0.55262429E 00		
(-0.1079E 01 J 0.3880E 00 ) T	0.1500E 02	0.592452416 00		
(-0.5657E-01 J 0.4702E-01 ) E	0.17006 02	0.62283635E 00		
3 (-0.50572-01 )	0.1800E 02	U.64370114E 00		
(~0.1320E 01 J-0.9202E-12 ) T	0.1900E 02	0.65540731E 00		
O (-0.54505-0) J-0.6949E-08 ) 6	0.2000E 02	. 0.65867203E 00	$t_p = 20$ sec.	peal
	0.2100E 02	0.65448/3/E 00	0 +	- 12.70
* ( 0.0000E 00 J 0.0000E 00 ) T	0.2200E 02	0.64404070E 00	overshool	= ,31.1/
( 0.5000E 00 J 0.9109E-07 ) E	0.2300E 02	0.62863541E 00	•	•
	0.2400E 02` 0.2500E 02	0.60961848E 00 0.56831459E 00		
· ·	0.2500E 02	0.56597197E 00		
4	0.2700E 02	0.543/1685E 00		
$e_{ss} \equiv c_{ss} = o. \tau$	0.2800E 02	0.52252042E 00		:
·	0.2900E 02	0.50317657E 00		
	0.3000E 02	· 0.48629081E 00	•	
	0.3100E 02	0.4722/865E 00		
,	0.3200E 02 .	0.4613729/E 00		
	0.3300E 02	0.453638208 00		. `
	0.3400E 02	0.44898993E 00	-	
•	0.3500E 02 0.3600E 02	0.44721884E 00 0.44801658E 00		
	0.3700E 02	0.45100296E 00		
	0.3800E 02	0.455751908 00		
,	0.3900E 02	0.461816975 00		
i	0.4000E 02	0.468/5346E 00		
	0.4100E 02	0.476137946 00	,	
	0.4200E 02	0.46358405E 00	,	
	0.4300E 02	0.490/5466E 00		,
	0.4400E 02	0.49737012E 00		
,	0.4500E 02	0.503212691 00	,	
	0.4600E 02 '	0.50812829± 00 0.51202422E 00		
*·	0.4700E 02 0.4800E 02	0.514865466 00		
	0.4900E 02	0.51666820£ 00		
	0.5000E 02	0.51749223E 00	,	
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) ·		t t=50 sec	overshoot = 3.5	57

0.0000E 00	3.40E-01 -2.	405-01 -1.								05 01 4 (05 0
			40E-01 -4.	.00E-U2 6.	00E-02 1.	50E-01 2.	60E-01 3.	60E-01 4.	60E-01 5.0	00E-01 6.60E-0
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NASAP RAMP RESPONSE ERRCE RESPONSE	RAMP KE	ESPUNSE .
E. K. E. K. S. F. C. W. S.	TIME	IR3/VV1
	0.0000E 00	0.10728836E-05
NONE	0.3000E-01	0.299930576-01
RAMP RESPONSE	0.6000E-01	L 0.59932828E-01
	0.9000E-01	0.89774251E-01
	0.1200E 00	0.11947465E 00
V1 1 2 1	0.1500E 00	
R1 2 3 1	0.1800E 00	
C1 3 1 1F	0.2100E 00	0.20735681E 00
V2 1 4 1 VC1 .	0.2400E 00	
R2 4 5 0.5 . NUMBER OF LOOPS PER ORDER .	0.2700E 00	0.26461649E 00
C2 5 1 1F	0.3000E 00	0.29277182E 00
V3 1 6 1 VC2	0.3300F 00	0.32058012E 00
R3 2 6 1 2= 3	0.3600E 00	0.34802485E 00
OUTPUT 3= 1	0.3900E 00	0.375091208 00
1 IR3/VV1 .	0.4200E 00	0.40176356E 00
TIME 1.5	0.4500E 00	0.428030736 00
EXECUTE	0.4800E 00	0.45388103E 00
	0.5100E 00	
	0.5400E 00	
TRANSFER FUNCTION IR3/VV1	0.5700E 00	0.52885991E 00
`	0.6000E 00	
•	0.6300E 00	0.576644786 00
	0.6600E 00	
2)	. 0.6900E 00	0.62263888E 00
( 0.00E 00 +3.00E 00 S +1.00E 00 S )	0.7200E 00	0.64495999E 00
	0.750UE 00	0.66683275E 00
H(5)= 1.000E 00*	0.7800E 00	0.68825656E 00
	0.8100E 00	
. ( 2 )	0.8400E 00	0.72976661E 00
( 2:00£ 00 +3:00E 00 S +1:00E 00 S )	0.8700E 00	0,74985778E 00
	0.90006 00	0.76951081E 00
	0.9300E 00	0.78572955E 00
	0.9600E 00	0.80751842E 00
	0.9900E 00	0.825881841 00
ZERO OF TRANSFER FUNCTION POLE OF TRANSFER FUNCTION	0.1020E 01	. 0.84382498£ 00
	0.1050E 01	
ZERO REAL PART IMAG. PART POLE REAL PART IMAG. PART	0.1080E 01	0.87847179E 00
	0.1110E 01	
	0.1140E 01	0.91150403E 00
1 0.00000E 00 0.00000E 00 1 -0.10000E 01 0.00000E 00	0.1170E 01	0.9274298UE 00
2 -0.30000E 01 0.00000E 00 2 -0.20000E 01 0.00000E 00	0.1200E 01	0.94297022E 00
	0.1230E Q1	
	0.1260E 01	0.97292125E 00
	0.1290E 01	0.98734486E 00
	0.1320E 01	0.10014086E 01
RAMP RESPONSE FUNCTION	0.1350E 01	0.10151215E 01
	0.1380E 01	0.10284872E 01
F(T) =	0.1410E 01	0.10415154E 01
	0.1440E 01	0.10542107E 01
(-0.1000E 01 J 0.0000E 00 ) T	0.1470E 01	0.10665808E 01
(-0,2000E 01 J-0,4210E-09 ) E	0.1500E 01	0.10786314E 01
(~0.2000E 01 J 0.0000E 00 ) T		
( 0.5000E 00 J 0.5262E-10 ) E		
	200 X = 0,0	001
( 0.0000E 00 J 0.1000E-02 ) T	Δ	
( 0.7500E 00 J-0.8750E-03 ) E	A = Q	
	B = 0.8	
( 0.0000E 00 J-0.1000E-02 ) T	72 = 0.8	/\ X/U
( 0.7500E 00 J 0.8750E-03 ) E	4 . C :	
	2 × B t	+2A = 1.5
X		

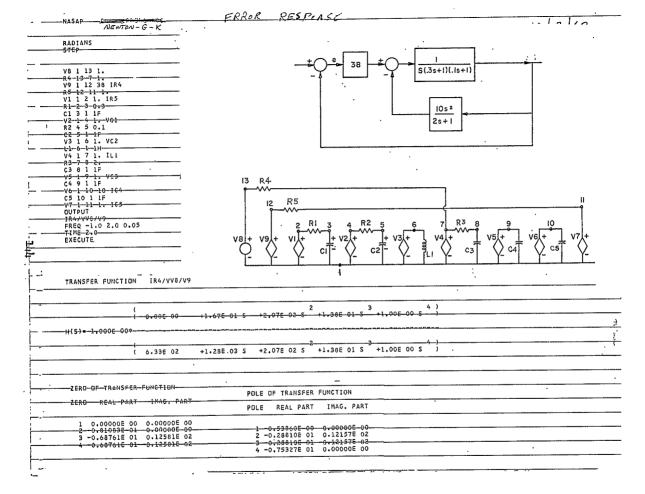
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We continue with the Newton Gould and Kaiser problem, see Fig. 4.9, to illustrate error responses. In Fig. 5.8 gives the step error. Figure 5.9 gives the step response. The latter is included here to emphasize that only a single NASAP computer card need be changed to get the alternative response output. Finally in Fig. 5.10 we show the ramp error response for this same control system.



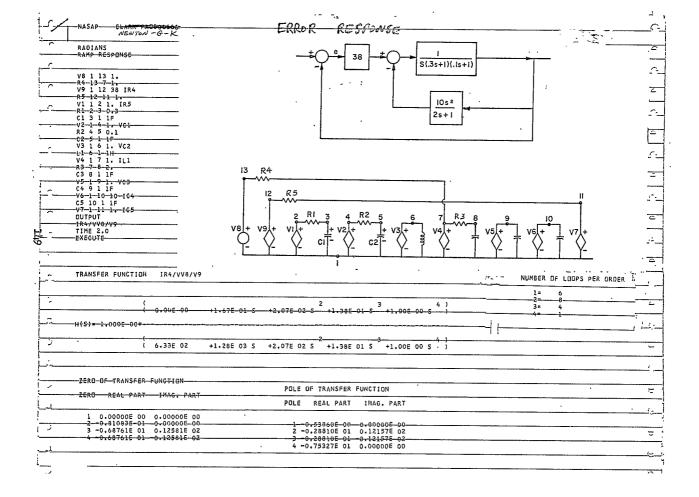
STEP RESPONSE FUNCTION	STEP RESE	PONSE	
F(T) =	TIME	IR4/VV8 0,99999970E-00-	
(-0.5386E 00 J 0.0000E 00 ) T	0.4000E-01	0.98830140E 00	~
(-0.8468E-01 1.0.1472E-07 ) E	0.8000E-01 0.1200E 00	0.726714918-00 0.77826107E 00	^
	0-1600E-00-	0.34088778E 00	
	0-2400E-00-	-0.11746454E-00 -0.62708139E-01	<del> </del>
(-0.2881E 01 J-0.1216E 02 ) T ·	0.2800E 00 0.3200E 00		
	0.3600E 00 	-0.22616476E 00 -0.21346736E-00	
( 0.9979E 00 J-0.2777E-07 ) E	0.4400E 00	-0.15973860E 00 -0.87881029E-01	
( 0.0000E 00 J 0.0000E 00 ) T	0.5200E 00	-0.19262429E-01	
( 0,0000E-00	0.5600E 00 0.6000E 00	0.30433368E-01 0.53309571E-01	
	0.6800E 00	0.49267378E-01 0.24339374E-01	
	07200E-00-		
	0.7600E 00	-0.49438279E-01	
	0.8400E 00	-0.97540200E-01 -0.10153145E-00	:
	0.8800E-00-	-0.93511105E-01	
	0.9600E-00- 0.1000E 01	-0.77544510E-01 -0.58580298E-01	
	0-10405-01	-0.41192196E-01	
	0.1080E 01 0.1-1-20E-01	-0.28661814E-01 -0.22530064E-01	
£	0.1160E 01 0.1200E 01	-0.22621151E-01 -0.27435813E-01	
<b>₹</b>	0.1240E 01	-0.34752585E-01	
	0.1280E-01 0.1320E 01	-0.42262293E-01 -0.48091702E-01	· ·
,	0.1369E-01-	-0.51122818E-01 -0.51082207E-01	
	0.1400E 01 0.1440E 01	-0.48427440E-01	· · · · · · · · · · · · · · · · · · ·
	0.1480E 01 0.1520E 01	-0.44095926E-01 -0.39202157E-01	
	0.1560E 01	-0.34757502E-01	
,	0.1600E-01- 0.1640E 01	-0.314705G7E-01 -0.29654402E-01	
	0.1686E-01 0.1720E 01	-0.29869609E-01	
	0.1760E 01	-0-31934324E-01-	<del></del>
	0.1800E 01 0.1840E-01-	-0.32216437E-01 -0.33004209E-01	·
•	0.1880E 01 0.1929E-01	-0.33160023E-01 -0.32636251E-01	
1	0.1960E 01	-0.31546686E-01	Ţ.
<u> </u>	0.2000E-01	0-30108280E-01	
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STEP RESPONSE FUNCTION	. STEP RESPON	SE
. F(T) =	_ TIME 0000E_00	VV4/VVB 0.00000000E 00
	0.0000E_00	0.11698127E-01
(-0.5386E 00 J 0.0000E 00 ) T	0.4000E=01	0.792847288-01
	0.1200E 00	0.22173876E 00
(-0+2881E 01 J 0+1216E 02 J T	0.1600F 00	G.42591405E.00
(-0.4340E-01 J 0.3176E 00 ) E	0.2000E 00	0,65911257E 00
(10)113102101 0 031102 00 7 2	0.2400F_00	0.88253599E 00
(-0.2881E 01 J-0.1216E 02 ) T	0.2800E 00	0.10627079E 01
(-0,4340E-01, J-0,3176E-00), E	0.320:15 00	0.11789455E 01
	0.3600E 00	0.12761648E 01 - Peak 22,6
	0.4.000E_00_	0.12134676E 01
(-0.9979E 00 J 0.3546E-07 ) E	0.4400E 00	0.11597385E 01
· · · · · · · · · · · · · · · · · · ·	0.4800E_00	0.10878811E 01
( 0.0000E 00 J 0.0000E 00 ) T	0.5200F 00	0.10192623E 01
	0.5600E 00	0.96956694E 00
	0.6000E 00 	0.94669074E 00 .
	0.6800E 00	0.97566098E 00
	0.0000E 00	0.10119514E 01
	0.7600E 00	0.10494355E 01
	0.8000F 00	0.1079693BE 01
	0.8400E 00	0.10975399E 01
	0.8800E_00_	0.11015310E 01
	0.9200E 00	0.10935106E 01
	0.960tE_00	0.10775442E_01
•	0.1000E 01	0.10585804E 01
	0.1040E 01	0.10411921E 01
ı	0.1080E 01	0.10286617E 01
	0.1120E_01	0.10225296E 01
	0.1160E 01 0.1200E 01	0.10226212E 01/ 0.10274353E 01
	0.1240E 01	0.10347528E 01
		0.10473262 01
,	0.1320E 01	0.10480919E 01
	0.1360E 01	0.10511227E 01
	0.1400E 01	0.10510817E 01
	0.1440F 01	0.10484276E 01
	0.1480E 01	0.10440960E 01
	0.1520E_01	0.10392017E 01
	0.156UE 01	6.10347576E 01
	0.1600F_01	0.103147.03E_01
	0.1640E 01	0.10296545E 01
	0.1680E 01	0-10292397E_01>
	0.1720E 01	0.10298691E 01
	0.1760F 01	0.10310345E 01
•	0.1800E 01 0.1840E 01	0.10322161E 01 0.10330038E 01
	0.1880E 01	0.10330038E 01
	0.19205 01	0.10331602E 01
	. 0.1960E 01	0.10325357E 01
	0.2000F 01	0.10301085E 01

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RAMP RESPONSE FUNCTION	RAMP	RESPONSE :	
F(T) =	TIME	IR4/VV8 -0	
(-0.5386E 00 J 0.0000E 00 ) T	0.4000E-	01 0.398792856-01	7
(-0.1572E-00-J-0.2739E-07-)-E	0.1200E		
(-0-2001E-01-J-0-1216E-02-) T,	0.1600E	00-0-13972944E-00	
(-0.2553E-01 J 0.2481E-02 ) E	0.2400F	00-16713339E-00	<b>f</b> =
(-0.2881E 01 J-0.1216E 02 ) T	0.2800E		
(-0,2553E-01 J-0,2481E-02 ) E	0.3600E	00 0.15465176E 00	
(-0,1325E 00 J 0,3688E-08 ) E	0-4000E- 0.4400E	00 0.13812327E 00	
, ( 0.0000E 00 J 0.1000E-02 ) T	0.4800E-		
( 0.1316E-01 J 0.1365E-03 )-E	0-5600E	00 0.13135147E 00	
	0.6000E		
( 0.1316E-01 J-0.1365E-03 ) E	0.6800E 0.7200E		
	0.7600E	00 0.13581055E 00	-
	0.8400E		
	O.8800E-	-00	
	0.9200E 0.9600E	-00	. 6
<b>○</b>	0.1000E	01 0.11547697E 00	
	0.1080E	01 0.11211604E 00	6
_9	0.1120E-		
	0.1200E-	01 0.10924119E 00	5
	0-1280E	01 0.10645854E-00	
1500	0.1320E 0.1360E		<u> </u>
	0.1400E	01 0.10059488E 00	
,	0.1440E- 0.1480E	01 0.96743226E-01	G
	0.1520E 0.1560E		
•	0-1600E-	01 0.92280924E-01	<u></u> <u></u> -
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# VD. FIGURES OF MERIT BASED ON ERROR SIGNAL

The conventional criteria on this basis are the transient performance and the steady state performance. These were briefly summarized in Chapter IV.

The overall response of a control system is determined by the poles and zeros of its transfer function  $G_f(s) = N_f(s) / D_f(s)$ ; it is not possible to tell it from the degree of  $D_f(s)$  and the difference of the degrees of  $D_f(s)$  and  $N_f(s)$  alone. However it is found that for the same  $\delta N_f$  an optimal system with a smaller  $\delta D_f$  is better than such a system with a larger  $\delta D_f$ ; where we have let  $\delta(\cdot)$  denote the degree of the polynomials. Similarly for the same  $\delta D_f$ , an optimal system with a smaller  $(\delta D_f - \delta N_f)$  is better than such a system with a larger  $(\delta D_f - \delta N_f)$ . Therefore, given a plant, for which we can choose the degree of  $\delta D_f$  and  $\delta N_f$ , it is desirable to choose a smaller  $\delta D_f$  and a smaller  $(\delta D_f - \delta N_f)$ . Now the smallest possible  $(\delta D_f - \delta N_f)$  is governed by the given plant.

It can be shown [CH 1] that the absolute minimum of  $\delta D_{\hat{f}}$  is  $\delta D$  -  $\delta N$ ; where D and N refer to the uncompensated system. To achieve this minimum,  $\delta N_{\hat{f}}$  is required to be zero. In general  $\delta N_{\hat{f}} \geq \delta N$ , unless some pole-zero cancellations are employed in the design.

The transient performance of, a system may be specified by percentage overshoot, rise time and settling time. These specifications are dictated by the poles and zeros of the transfer function. Since we do not have control over the zeros of a system, usually we just try to put the poles of the over-all system in some desired location. For a second order transfer function with a constant numberator, the desired pole locations can be readily determined from the transient specifications. For high order transfer functions, the concept of dominant poles can often be used. Then a pair of complex conjugate poles is located as in the second order transfer function and the rest of the poles are located in the far left half plane with real parts at least ten times as large as the real parts of the conjugate poles. In choosing these poles, the steady state performance should be kept in mind.

The steady-state performance of a control system  $G_{\hat{\mathbf{f}}}(s)$  depends only on the coefficients of  $G_{\hat{\mathbf{f}}}(s)$ . Let

$$G_{\hat{\mathbf{f}}}(s) = \frac{b_0 + b_1 s + b_2 s^2 + \dots + b_{n-1} s^{n-1}}{a_0 + a_1 s + a_2 s^2 + \dots + a_{n-1} s^{n-1} + s^n},$$

If the steady-state error due to a step input and a ramp input are required to be smaller than  $k^a/_b$ , then we need, respectively,

$$\left| \frac{b - a_0}{a_0} \right| \le k/100;$$
 and  $a_0 = b_0, \left| \frac{b - a_1}{a_0} \right| \le k/100.$ 

Hence the steady-state performance of a system can be rather easily controlled. When using these criteria it is necessary to check the response of the chosen overall transfer function with an analog or a digital computer to be sure that it is satisfactory before continuing the design.

In addition to the conventional criteria just discussed, we shall mention a few other criteria based on the error signal that serve to make the control system "optimum" in some sense.

(i) <u>ITAE criterion</u> (Integral of time-multiplied absolute-value of error):

This criterion was first introduced by Graham and Lathrop [GA 1]. For a given plant, the problem is to design an overaall system which minimizes

$$\int_0^{\infty} t |r(t) - c(t)| dt$$

where r is the reference or desired signal and c is the output of the over-all system. It is clear that |r(t) - c(t)| is the error between the desired signal and the actual output. The multiplication of t on |r(t) - c(t)| provides an increasingly heavy penalty for a sustained error. Using step functions as reference inputs, Graham and Lathrop obtained, by analog computer simulation a set of optimal transfer functions [GA 1].

To choose an optimal transfer function  $G_{\mathbf{f}}(s)$  for a given plant G(s) note that if all the forward paths from r to c pass through the plant, then the zeros of the plant (the roots of N(s)) will be independent of how the compensators are introduced. Consequently if the numerator of  $G_{\mathbf{p}}(s)$  does not contain all the zeros of G(s), the missing zero must be cancelled by a pole. The advantage of this criterion is that it is very selective; however it cannot be studied analytically. This criterion is not widely used, because a complete list of optimal transfer functions is not available.

(ii) Quadratic criterion: The optimal system is the one which minimizes

$$\int_{0}^{\infty} \left[ u^{2}(t) + (r(t) - c(t))^{2} \right] dt$$

where u is the input to the plant. In this criterion, if u<sup>2</sup> is not included, the optimal transfer function will always be unity and the required compensators may not be physically realizable; furthermore the magnitude of u may be large and the system will be saturated. The optimal transfer function for a given plant and a given reference input r can be obtained by applying Chang's root-square-locus method [CH 1] as well as by using the dynamical equation description [see AT 1]

The design by using the quadratic criterion can be solved rigorously. However there are three arguments against using this criterion. First, it is not very selective [GR 1]. Second, the criterion is chosen mainly for mathematical convenience rather than practical reasons. Finally and most seriously, the resulting optimal transfer function may not be realizable in practice. If all the zeros of the transfer function of the plant  $G(s) = \frac{N(s)}{D(s)}$  have negative real parts and if the reference input is a step function, the optimal

transfer function is of the form  $\frac{k\mathbb{N}(s)}{D_f(s)}$  and  $\delta D_f(s) = \delta D$ . In this case, it is easily realized. However for plants with nonminimum-phase transfer function, the design by using quadratic criterion might have difficulty. Another difficulty in using this criterion occurs when the reference input is a ramp.

(iii) ISE criterion (the integral of the error squared): Here one seeks to minimize

$$\int_{0}^{t} e^{2}(t) dt.$$

To obtain any of these criteria from NASAP use of an external integration subroutine is required. To illustrate this we follow Beck [BE 1] and use the integral of the squared error as the performance index although other criteria can be applied with equal ease since an analytical solution is not required. The formation of the chosen performance index is indicated in Fig. 5.7 taken from [BE 1] where it is shown that the

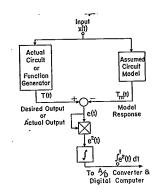


Fig. 5.7: Index of performance formation

ISE is generated in the analog computer and returned to the digital computer through the analog to digital converters. In the hybrid computer application an optimization algorithm operates upon this output.

#### CHAPTER VI

#### SENSITIVITY ANALYSIS

### VIA INTRODUCTION TO SENSITIVITY

The NASAP sensitivity results, given in tabular and graphical form, can be used to predict the percent change, absolute change, and modified value of the transfer function to changes in a particular network parameter. By definition the sensitivity of some real function o (in NASAP, ReH,  $\hat{\alpha}n\hat{H}$  |H| and  $\phi$ ) to a change in a real parameter x (in NASAP, resistance, capacitance, inductance and dependency value) is defined as

$$S_{x}^{\alpha} \stackrel{\Delta}{=} \frac{x}{\alpha} \frac{dx}{dx} = \frac{\frac{d\alpha}{\alpha}}{\frac{dx}{x}} = \frac{d\ln \alpha}{d\ln x}$$
 (6.1)

By rearranging (6.1), the differential  $d\alpha$  can be related to the differential dx,

$$d \alpha = \alpha \int_{-\infty}^{\infty} \frac{dx}{x}$$
 (6.2)

For an incremental change,  $\Delta x$ , in the parameter x the incremental change,  $\Delta \alpha$ , in  $\alpha$  can be approximated from (6.2)

$$\Delta \cdot dc \approx \alpha \int_{\mathbf{x}}^{\alpha} \frac{\Delta \mathbf{x}}{\mathbf{x}}$$
 (6.3a)

If the change in x is expressed as some percentage of x, then (6.3a) can be expressed as

$$\Delta \propto \approx \alpha \lesssim_{x} \frac{P_{x}}{100}$$
 (6.3b)

where Px is the percent change in the parameter x. The percent change in  $\alpha$  is easily found by dividing both sides of (6.3½) by  $\alpha$ , thus

$$P \alpha \approx \int_{x}^{\alpha} Px$$
 (6.4)

where P  $\alpha$  is the percent change in the function  $\alpha$ . The modified value of  $\alpha$ , realled  $\alpha$ , can be expressed as

$$\alpha' \quad \underline{\Delta} \quad \alpha + \underline{\lambda} \alpha \qquad (6.5)$$

$$\alpha' \approx \alpha \left(1 + \int_{x}^{\alpha} \frac{\Delta x}{x}\right)$$
 (6.6a)

or

$$\alpha' \approx \alpha \left(1 + \int_{x}^{\alpha} \frac{p_{x}}{100}\right)$$
 (6.6b)

Naturally the smaller  $\Delta_X$  or  $P_X$ , the more accurate  $\Delta \alpha$ ,  $\alpha$ , and  $P_{OX}$  will be. The accuracy will also be enhanced if  $\alpha$  is roughly a linear function of x over the range of x under investigation.

If indeed  $\alpha$ :is a linear function of x of the form

$$\alpha = Kx, \tag{6.7}$$

then from (6.1) it is seen that

$$\int_{-\infty}^{\alpha} A = 1 \tag{6.8}$$

Furthermore from (6.1) if  $\alpha$  is independent of x, then

$$\int_{\mathbf{x}}^{\alpha} \pi \, \theta \tag{6.9}$$

or the function  $\alpha$  is insensitive to changes in x.

Similarly the root sensitivity printed out by NASAP can be used to predict the new pole and zero locations for a small change in some network parameter. The root sensitivity is defined as

$$\sigma_{\mathbf{x}}^{\mathbf{p}'} \triangleq \mathbf{x} \frac{\mathrm{dp}}{\mathrm{dx}} \tag{6.10}$$

where p is a zero or pole of the given transfer function. The differential dp can be expressed in terms of the root sensitivity as

$$dp = \sigma_{k}^{p'} \frac{dx}{x} = \sigma_{k}^{p'} d\ln x$$
 (6.11)

Note that dp will be complex since  $\sigma_x^{p}$  is also a complex number while  $\frac{dx}{x}$  is a real quantity.

The incremental change in p,  $\Delta p$ , for an incremental change in x is derived from (6.11)

$$\Delta p \cong \sigma_{x}^{p'} \frac{\Delta x}{-x}$$
 (6.12)

If  $\Delta x$  is expressed as some percentage of x then (6.12) becomes

$$\Delta p \cong \sigma_{x}^{p} \frac{P_{x}}{100} \tag{6.13}$$

where  $P_{\mathbf{x}}$  is the percent change in  $\mathbf{x}$ .

# YIB DERIVATION OF SENSITIVITY FORMULAS

Although the formulas used in NASAP to calculate the transfer function sensitivity were derived from a tagging technique on the loops of the flow-graph (see [MA 1]); these sensitivity formulas can be obtained by using simple calculus. Suppose the transfer function is given

$$H(s) = \frac{N(s)}{D(s)}$$
 (6.14)

where N(s) and D(s) are polynomials in s.

Since H(s) is the transfer function of a linear circuit it can be expressed as a bilinear function of any element in the circuit. That is, both N(s) and D(s) can be expressed as the sum of two polynomials in s where one polynomial does and the other does not contain the specified element. Thus

$$H(s) = \frac{N(s)}{D_1(s)} = \frac{A(s) + x B(s)}{C(s) + x D(s)}$$
(6.15)

where x is the specified element in the circuit and A,B,C, and D are polynomials in s.

The sensitivity of the transfer function H(s) to some parameter  $\boldsymbol{x}$  is defined as

$$\int_{x}^{H(s)} \Delta \frac{dH/H}{\sin dx/x} = \frac{d\ln H}{d\ln x}$$
 (6.16)

Thus to find the sensitivity of H(s) to changes in x in (6.15), one obtains

$$S_{x}^{H(s)} = S_{x}^{N(s)} - S_{x}^{D_{1}(s)}$$
 (6.17)

but

$$\sum_{x}^{N(s)} = \frac{x}{N(s)} \frac{d N(s)}{dx}$$

$$= \frac{x}{A+Bx} \frac{d}{dx} (A+Bx)$$

$$= \frac{Bx}{A+Bx}$$
(6.18)

Similarly

$$\sum_{x}^{D_{1}(s)} = \frac{Dx}{C+Dx}$$
 (6.19)

Substituting (6.18) and (6.19) into (6.17) yields

$$S_{x}^{H(s)} = \frac{Bx}{A+Bx} - \frac{Dx}{C+Dx}$$
 (6.20)

This expression remains unchanged if 1 is added and subtracted from the righthand side. Then we can write

$$S_{x}^{H(s)} = \frac{B_{x}}{A+B_{x}} - \frac{A+B_{x}}{A+B_{x}} - \frac{D_{x}}{C+D_{x}} + \frac{C+D_{x}}{C+D_{x}}$$
$$= -\frac{A}{A+B_{x}} + \frac{C}{C+D_{x}}$$

$$= -\frac{A(s)}{N(s)} + \frac{C(s)}{D_1(s)}$$
 (6,21)

This equation can also be derived from the tagging technique on the loops of the flowgraph and is the one used in subroutine SENSS of NASAP to determine the transfer function sensitivity.

VIC DISCUSSION OF SENSITIVITY FORMULAS: IN SENS-

In subroutine SENS of the NASAP program are calculated the sensitivity expressions  $S_x^{ReH}$ ,  $S_y^{ImH}$ ,  $S_y^{|H|}$  and  $S_y^{\phi}$ 

where  $H_{(j\omega)} = \text{ReH}(j\omega) + j\text{Im } H(j\omega)$ and  $H_{(j\omega)} = |H_{(j\omega)}|e^{j\phi}$ .

Again the tagging techniques of [MA 1] are used to determine the sensitivity expressions. The basis for the tagging procedure is that the transfer function H(s) can be written as in (6.15) where x is the sensitivity parameter. Since the polynomials A, B, C, and D are, in general, complex quantities for  $s = j\omega$ , (6.15) can be rewritten as

$$H(j\omega) = \frac{(\text{Re } A + x \text{ Re } B) + j (\text{Im } A + x \text{ Im } B)}{(\text{Re } C + x \text{ Re } D) + j (\text{Im } C + x \text{ Im } D)}$$
(6.22)

where  $A(j\omega) = ReA(j\omega) + j Im A (j\omega)$  etc.

After some mathematical manipulation, the right side of (6.22) can be separated into its real and imaginary parts. Thus

$$\operatorname{ReH}(j\omega) = \frac{N_R}{D} = \frac{(\operatorname{ReA} \operatorname{ReC} + \operatorname{ImA} \operatorname{ImC}) + x(\operatorname{ReB} \operatorname{ReC} + \operatorname{ReA} \operatorname{ReD} + \operatorname{ImB} \operatorname{ImC}) + x^2(\operatorname{ReB} \operatorname{ReD} + \operatorname{ImB} \operatorname{ImD})}{\left[(\operatorname{ReC})^2 + (\operatorname{ImC})^2\right] + 2x(\operatorname{ReC} \operatorname{ReD} + \operatorname{ImC} \operatorname{ImD}) + x^2\left[(\operatorname{ReD})^2 + (\operatorname{ImD})^2\right]}$$
(6.23)

and ...

$$ImH(j\omega) = \frac{N_{I}}{D} = \frac{(ImA ReC - ReA ImC) + x(ImA ReD - ReA ImD + ImB ReC - ReB". ImC) + x^{2}(ImB ReD - ReB ImD)}{\left[ (ReC)^{2} + (ImC)^{2} \right] + 2x(ReC ReD + ImC ImD) + x^{2} \left[ (ReD)^{2} + (ImD)^{2} \right]}$$
(6.24)

Thus by use of (6.17) one obtains

$$S_{x}^{ReH} = S_{x}^{N_{R}} - S_{x}^{D}$$
$$= \frac{x}{N_{R}} \frac{d}{dx} N_{R} - \frac{x}{D} \frac{d}{dx} D$$

or

$$S_{x}^{\text{ReH}} = \frac{x}{N_{R}D} \left( D \frac{d}{dx} N_{R} - N_{R} \frac{dD}{dx} \right)$$
 (6.25)

$$\frac{d\dot{N}_{R}^{'}}{d\dot{x}} = (\text{ReB ReC} + \text{ReA ReD} + \text{ImB ImC} + \text{ImA ImD}) + 2x(\text{ReB ReD} + \text{ImB ImD})$$
 (6.26)

and 
$$\frac{dD}{dx} = 2(\text{ReC ReD} + \text{ImC ImD}) + 2x \left[ (\text{ReD})^2 + (\text{ImD})^2 \right]$$
 (6.27)

and N $_{\rm R}$  and D are defined in (6.23).

By a similar use of (6.17) one arrives at the expression

$$S_{x}^{ImH} = \frac{x}{N_{I}D} D\left(\frac{dN_{I}}{dx} - N_{I}\frac{dD}{dx}\right)$$
 (6.28)

where  $\frac{dN_{I}}{dx}$  = (ImA ReD - ReA ImD + ImB ReC - ReB ImC) + 2x(ImB ReD - ReB ImD) (6.29) and  $\frac{dD}{dx}$  is given, (6.27), and  $N_{I}$  and D are defined in (6.24).

Equations (6.25) and (6.28) are used in subroutine SENS to evaluate the sensitivities of the real part and imaginary part of the transfer function to changes in the parameter x.

The sensitivities  $S_{\rm x}^{|\rm H|}$  and  $S_{\rm x}^{\phi}$  are evaluated in terms of the sensitivities found in (6.25) and (6.28). By definition

$$|H| = \sqrt{(ReH)^2 + (ImH)^2}$$
 (6.30)

Differentiating this with respect to the sensitivity parameter x yields

$$\frac{\mathrm{d}}{\mathrm{d}\mathbf{x}}|\mathbf{H}| = \frac{\mathrm{ReH} \frac{\mathrm{dReH}}{\mathrm{d}\mathbf{x}} + \mathrm{ImH} \frac{\mathrm{dImH}}{\mathrm{d}\mathbf{x}}}{\sqrt{\left(\mathrm{ReH}\right)^2 + \left(\mathrm{ImH}\right)^2}}$$
(6.31)

By definition

$$S_{\mathbf{x}}^{|\mathbf{H}|} = \frac{\mathbf{x}}{|\mathbf{H}|} \frac{\mathbf{d}|\mathbf{H}|}{\mathbf{d}\mathbf{x}} \tag{6.32}$$

Substituting (6.30) and (6.31) into (6.32) results in

$$S_{x}^{\mid H \mid} = \frac{x_{\text{ReH}} \frac{d_{\text{ReH}}}{dx} + x_{\text{ImH}} \frac{d_{\text{ImH}}}{dx}}{|H|^{2}}$$
 (6.33)

Recalling that

$$S_{x}^{\text{reH}} \stackrel{\triangle}{=} \frac{x}{\text{ReH}} \frac{\text{dReH}}{\text{dx}}$$
 (6.34)

and

$$S_{x}^{\text{ImH}} \triangleq \frac{x}{\text{EmH}} \frac{\text{dImH}}{\text{dx}}, \tag{6.35}$$

one can simplify (6.33) to

$$S_{x}^{|H|} = \frac{(\text{ReH})^{2} S_{x}^{\text{ReH}} + (\text{Im}H)^{2} S_{x}^{\text{Im}H}}{|H|}$$
(6.36)

The sensitivity of the phase of the transfer function to changes in x,  $S_x^\phi$  , is also easily obtained. By definition

$$\tan \phi = \frac{\text{Im}H}{\text{ReH}} \tag{6.37}$$

By implicit differentiation of (6.37) with respect to x, one obtains

$$\sec^{2}\phi \frac{d\phi}{dx} = \frac{\text{ReH} \frac{d\text{ImH}}{dx} - \text{ImH} \frac{d\text{ReH}}{dx}}{(\text{ReH})^{2}}$$
(6.38)

Since

$$S_{x}^{\phi} \stackrel{\triangle}{=} \frac{x}{\phi} \frac{d\phi}{dx} \tag{6.39}$$

one obtains by substituting (6.38) into (6.39)

$$S_{x}^{\phi} = \frac{\cos^{2}\phi}{\phi (ReH)^{2}} \left( xReH \frac{dImH}{dx} - xImH \frac{dReH}{dx} \right)$$
(6.40)

By use of the definitions in (6.34) and (6.35) and the relation

$$ReH = |H| \cos \phi, \qquad (6.41)$$

the expression in (6.40) can be simplified to

$$S_{x}^{\phi} = \frac{1}{\phi |\mathbf{H}|^{2}} \left( \text{ReH ImH} \right) \left( S_{x}^{\text{ImH}} - S_{x}^{\text{ReH}} \right)$$
(6.42)

Equations (6.36) and (6.42) are used in subroutine SENS to determine

$$S_{
m x}^{|{
m H}|}$$
 and  $S_{
m x}^{\phi}$  , respectively.

This is possible since the quantities  $\phi$ , |H|, ReH, and ImH have been previously calculated and stored during generation of the Bode tables and

plots while  $S_x^{ReH}$  and  $S_x^{ImH}$  have been determined earlier in subroutine SENS.

# VID DISCUSSION OF REVISED SENSITIVITY SUBROUTINE

In Appendix B is a revised version of subroutine SENSS which does the calculations of SENS and SENSS in a more efficient manner. This version of SENSS requires only 3/4 of the core storage required by the present SENS and SENSS and it utilizes a simpler algorithm that greatly reduces the number of mathematical operations required. This saves execution time and should increase the accuracy of the sensitivity calculations.

The version of SENSS given in Appendix B uses the same tagging procedure that is used in the present SENSS and calculates  $S_{\mathbf{x}}^{\mathrm{H}(j\omega)}$  with the use of equation (6.25) as does the present SENSS. However, the outputs of the present SENS, that is  $S_{\mathbf{x}}^{|\mathbf{H}|}$ ,  $S_{\mathbf{x}}^{\phi}$ ,  $S_{\mathbf{x}}^{\mathrm{ReH}}$ , and  $S_{\mathbf{x}}^{\mathrm{ImH}}$  are related to the real and imaginary parts of  $S_{\mathbf{x}}^{\mathrm{H}(j\omega)}$ . Thus the rather complication sensitivity expressions now used in the present SENS and described in equations (6.23) through (6.42) are completely avoided.

Since, in general, the sensitivity expression  $S_x^{\ H(j\omega)}$  is a complex quantity, it can be written as

$$S_{\mathbf{v}}^{\mathbf{H}(\mathbf{j}\omega)} = \operatorname{Re} S_{\mathbf{v}}^{\mathbf{H}(\mathbf{j}\omega)} + \mathbf{j} \operatorname{Im} S_{\mathbf{v}}^{\mathbf{H}(\mathbf{j}\omega)}$$
(6.43)

But

$$H(j\omega) = |H(j\omega)| e^{j\phi}$$
 (6.44)

where  $\phi$  is the phase of the transfer function  $H(j\omega)$ .

Thus one has

$$S_{x}^{H(j\omega)} = S_{x}^{|H|} e^{j\phi}$$

$$= S_{x}^{|H|} + S_{x}^{e^{j\phi}}$$
(6.45)

Let us examine the rightmost term of (6.45) more closely. By definition

$$\int_{\mathbf{x}}^{\mathbf{e}^{\mathbf{j}\phi}} \stackrel{\Delta}{=} \frac{\mathbf{x} \cdot \mathbf{x}}{\mathbf{e}^{\mathbf{j}\phi}} \frac{\mathbf{d}}{\mathbf{d}\mathbf{x}} \mathbf{e}^{\mathbf{j}\phi} .$$
(6.46)

By use of the differentiation chain rule, the derivative expression in (6.46) can be simplified to

$$\frac{\mathrm{d}}{\mathrm{dx}} e^{\mathrm{j}\phi} = \mathrm{j}e^{\mathrm{j}\phi} \frac{\mathrm{d}\phi}{\mathrm{dx}} . \tag{6:47}$$

Substituting (6.46) and (6.47) into (6.45) yields

$$S_{x}^{H(j\omega)} = S_{x}^{|H|} + jx \frac{d\phi}{dx}. \qquad (6.48)$$

Using the definition given in (6.39) this equation can be rewritten as

$$S_{x}^{H(j\omega)} = S_{x}^{|H|} + j\phi S_{x}^{\phi}$$
 (6.49)

If the sensitivity parameter is a real quantity, then the expressions

 $S_{\rm x}^{\rm |H|}$  and  $S_{\rm x}^{\rm \phi}$  ,will also be real. Thus if (6.49) is compared with (6.43) and the real and imaginary parts equated (under the assumption that x is real) then one obtains

$$S_{\mathbf{x}}^{|\mathbf{H}|} = \operatorname{Re} S_{\mathbf{x}}^{\mathbf{H}(\mathbf{j}\omega)} \tag{6.50}$$

and

--'

$$\phi = \text{Im} \int_{x}^{\theta} \left( \text{id} \right) dt$$
(6.51a)

or

$$S_{x}^{\phi} = \frac{1}{\phi} \operatorname{Im} S_{x}^{H(j\omega)}$$
 (6.51b)

where x is a real variable.

The sensitivity of the real part of H( $\S$ ) to changes in x, S can can also be obtained in terms of the real and imaginary parts of  $\S$  H( $\S$ ). By definition

$$ReH(j\omega) = |H(j\omega)| \cos \phi \tilde{.} \qquad (6.52)$$

Thus

$$S_{x}^{ReH} = S_{x}^{|H|\cos\phi}$$

$$= S_{x}^{|H|} + S_{x}^{\cos\phi}$$
(6.53)

But

$$\overset{\circ}{S}_{x}^{\cos \phi} = \frac{x}{\cos \phi} \frac{d}{dx} \cos \phi$$

$$= -x \tan \phi \frac{d\phi}{dx} .$$
(6.54)

Equation (6.54) can be rewritten as

$$S_{x}^{\cos \phi} = -\phi \tan \phi S_{x}^{\phi}$$
 (6.55)

by use of the definition in (6.39). Thus equation (6.53) becomes, after the substitution of (6.55),

$$S_{x}^{ReH} := S_{x}^{|H|} \rightarrow \tan \phi S_{x}^{\phi}. \tag{6.56}$$

However, after (6.50), (6.51a) and (6.37) are substituted into (6.56), the expression becomes

$$S_{x}^{ReH} = ReS_{x}^{H(j\omega)} - \frac{ImH}{ReH} ImS_{x}^{H(j\omega)}$$
 (6.57)

A similar expression can be derived for the sensitivity of the imaginary part of H(j $\omega$ ) with respect to changes in x,  $S_x^{ImH}$ . By definition

$$ImH(j\omega) = |H(j\omega)| \sin \phi$$
 (6.58)

Thus

$$S_{x}^{ImH} = S_{x}^{|H| \sin \phi}$$

$$S_{y}^{|H|} + S_{y}^{\sin \phi}. \qquad (6.59)$$

By a similar mathematical technique, it can be shown that

$$S_{x}^{\sin \phi} = \frac{\phi}{\tan \phi} S_{x}^{\phi} \tag{6.60}$$

Substituting this expression into (6.59) gives

$$S_{x}^{ImH} = S_{x}^{|H|} + \frac{\phi}{\tan \phi} S_{x}^{\phi} \qquad (6.61)$$

which can be further simplified by the substitution of (6.50), (6.51a) and (6.37)

$$S_{x}^{ImH} = Re S_{x}^{H(j\omega)} + \frac{ReH}{ImH} Im S_{x}^{H(j\omega)}$$
(6.62)

Equations (6.50), (6.51b), (6.57) and (6.62) are used in the version of SENSS given in Appendix B. This is possible since the real quantities  $\phi$ , ReH, and ImH have been calculated earlier in subroutine BODE while the complex quantity  $S_{\chi}^{H(j\omega)}$  is calculated in the Appendix B version of SENSS.

Note that (6.57) involves only 3 arithmetic operations while (6.25) involves 8 arithmetic operations plus the numerous operations involved in equations (6.23) and (6.26). The same comparison can be made between (6.62) and (6.28). With regard to  $S_{\rm x}$ , (6.50) involves no arithmetic operations while (6.36) uses 8 operations. Similarly in determining  $S_{\rm x}^{\phi}$  equation (6.51b) requires one arithmetic operation while (6.42) involves 6 operations. Since the sensitivity calculations must be redone for each frequency value, the number of arithmetic operations is quite substantially reduced with the version of SENSS given in Appendix B.

### VIE ROOT SENSTTIVITY

The sensitivites of the poles and zeros of the transfer function to changes in some specified network parameter are also determined by NASAP by use of the tagging technique and the formulas given in [KU1, PA1] which will be summarized here.

Suppose we have a polynomial in the complex frequency variable s, P(s), which can also be expressed as

$$P(s) = \alpha(s) + x\beta(s) = \sum_{k=0}^{N} a_k s^k$$
 (6.63)

where the degree of P(s) is N and P(s) has only positive powers of s and x is the sensitivity parameter. Furthermore the roots of the above polynomial are known, i.e., N values of s are known such that

$$P(r_i) = 0$$
  $i = 1, 2, \dots N$  (6.64)

where  $r_i$  is the i<sup>th</sup> root of P(s).

If the order of the root  $\mathbf{r}_i$  is m, then the root sensitivity,  $\mathbf{s}_x^{\text{ri}}$  , as defined by

$$s_x^{ri} \triangleq x \frac{dr_i}{dx}$$
 (6.65)

can be expressed in terms of the given polynomials  $\alpha(\hat{\vec{s}})$  and  $\beta(s)$ 

$$s_{x}^{r}i = \frac{\frac{d^{m-1}}{ds^{m}} (x\beta(s))}{\frac{d^{m}}{ds^{m}} (\alpha(s) + x\beta(s))}$$

$$s = r_{1}$$

$$i=1,2,\cdots N \quad (6.66)$$

If  $r_i$  is a simple root of P(s), then

$$s_{x}^{r}i = \frac{-x\beta(r_{i})}{\frac{d}{ds}(\alpha(s) + x\beta(s))}\bigg|_{s = r_{i}}$$
(6.67)

As was shown above, the transfer function H(s) can be written as

$$H(s) = \frac{N(s)}{D_1(s)} = \frac{A(s) + xB(s)}{C(s) + xD(s)}$$
(6.68)

where x is the sensitivity parameter.

If  $\mathbf{Z_i}$  is a simple zero of H(s), then the zero sensitivity with respect to x can be expressed as

$$s_{x}^{Z_{1}} = \frac{xB(Z_{1})}{\frac{d}{ds}(A(s) + xB(s))} \Big|_{s = Z_{1}} = \frac{-xB(Z_{1})}{\frac{d}{ds}N(s)} \Big|_{s = Z_{1}} = 1,2,\cdots M \quad (6.69)$$

where M is the number of distinct zeros and A(s), B(s), and N(s) are defined in (6.23).

Similarly, if  $\mathbf{p_i}$  is a simple pole of  $\mathbf{H(s)}$ , then the pole sensitivity with respect to x can be written as

$$s_{x}^{p_{\underline{i}}} = \frac{xD(p_{\underline{i}})}{\frac{d}{ds}(C(s) + xD(s))}\Big|_{s=p_{\underline{i}}} = \frac{-xD(p_{\underline{i}})}{\frac{d}{ds}D_{\underline{i}}(s)}\Big|_{s=p_{\underline{i}}} = 1,2,\dots, N \quad (6.70)$$

where N is the number of distinct poles of H(s) and C(s), D(s), and  $D_1$ (s) are defined in (6.68).

Since the polynomials A(s), xB(s), C(s), and xD(s) have been determined by the tagging process during the evaluation of the loops in subroutines

FLGRPH and HIGORL, the sensitivities of the poles and zeros are easily obtained by differentiating the denominator and numberator polynomials respectively and by evaluating the resultant polynomial and the appropriate tagged polynomial at the given pole or zero. These calculations are performed in subroutine ROOTSS.

### VIF EXAMPLES

In the foregoing sections of this chapter we have indicated many possibilities for sensitivity analysis with the aid of NASAP. We shall illustrate a few of these as follows:

1. Taking advantage of the background developed in Chapters TV and V on the unity feedback control system with lead cascade compensation see Fig. 6.1a (also Figs. 3.16 and 4.7) we obtain the sensitivity  $S_{\chi}^{\ H}$  of the transfer function VV4/VV5 with respect to resistor R1. This is a judicious choice of circuit element since one of the time constants of the control system plant is

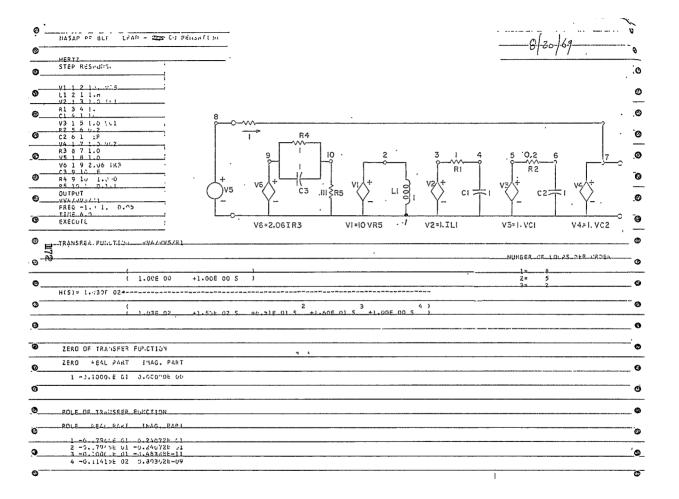
$$\tau_1 = (R1) (C1)$$

Hence if Cl is constant in value the sensitivity determined for Rl is the same as that for the time constant  $\tau_1$ . The NASAP printout for this example is shown in Fig. 6.1. The corresponding zero and pole sensitivities are given in Fig. 6.2.

- 2. The second example Fig. 6.2 follows up with the uncompensated unity feedback control system for which we obtain the ramp response in Fig. 6.3 and the sensitivity function  $S_K^H$ . Thus we seek the sensitivity of the transfer function VV4/VV5 with respect to system gain K, in this case K = 0.83. The NASAP printout is shown in Fig. 6.4 with the corresponding zero and pole sensitivities given in Fig. 6.5.
- 3. The third example furnishes sensitivity data, specifically S = K for the multiloop feedback compensated control system with K = 38. Since the pertinent NASAP model and transfer function print out were given in Fig. 5, they are not repeated here. The corresponding gain sensitivity print outs are given in Fig. 6.6 and the zero-pole sensitivity in Fig. 6.7.

4. For the final example we use one of the control subsystem of the Ranger space vehicle taken from Dorf [DO1, Problem 4.5]. The mission in 1965 was to scan the lunar surface with TV and other sensors. The requirement on the altitude control subsystem was to stabilize and control the Ranger space-craft from second stage separation to lunar impact. Briefly a high gain antenna furnished input signals to the earth horizon sensor which in turn fed the gyro loop. The latter consisted of the spacecraft, as the plant, with the altitude gyro in cascade as shown in Fig. 6.8z along with its NASAP model. To give some feel for the cut and try process in determining the gyro loop gain K that will keep the step response overshoot under the required 5%, we show for three values of gain the print outs of  $s_K^H$ , zero-pole sensitivities  $s_H^{D_1}$  and the corresponding step response. For convenience in examining the print outs we tabulate the pertinent figure numbers.

K	step response	s <sub>K</sub>	$s_{\mathrm{H}}^{\mathrm{p}_{\mathbf{i}}}$
6	6.8	Fig. 6.9	6.10
20	6.11	Fig. 6.12	6.13
75	6.14	Fig. 6.15	6.16



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	-0.4999797E 00	0.12519265 00	0.24586711 00	-U.4750122E 02	-0.6092993E Q0		<u> </u>
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	-0.7597 9 L 00 -0.7497799E 00	0.177-250E 00	0.4280353E 00	-0.6211020E 02	-0.44654416 00 -0.36857046 00		
	-0.6999.99= 00	0.19952031 00	0.42803336 00	-0.6763199E CZ	-C.292.4437E-60		
	-0.6500.00E 00	0.22357218 00	0.60354041 00	-0./356511E 02	-0.2192930E 00		
		C.251.1856E90 C.281.382F 00	0.7104592E 00 0.6301610E 00	-0.8000124E-02 -0.8705687E-02	-0.1984924E-00 -0.8083761E-01		
	-0.550a.01E 00	C.2013202F 00	0.053310198 00	-0.94853931 02	-0.173255E-U		
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	-0.7500.04E 00	0.56734096 00	0.1464842E 01	-0.14195348 03	0.147633/6 00		
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	-0.150; 63E 00	0.70774206 56	0. 34/3/86 01	-0.15695458 03	0.1294094E OU		
	-0.000105E-00 -0.5000:55E-01	0.89124936 00	0.12953-ct 01 0.12416/lt 01	-0.1523679b 63 -0.1665227E 03	0.1123836E 00 0.9400636E-01		
		0.0912493E 00	0.112/10/12 01	-0.10092576 09	0.76269965=91		
	0.4993:64E-01	0.11240156 01	0.11+8677t 01	-0.17189A7E 03	0.6020543=-01		
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	0.64997518 00	0.496/6166 31	0.10:15(3E 01 0.10:0536E 01	-0.1781749E 03 -0.1783464E 03	0.6522504E-03		
	0.7499785E 00	0.56233921 01	0.10J0450t 01	-U-1/849:5E 03	0.21614576-03		
	0.79993065 00	C.6302554E 01	0.2630Zo2E 01	-0-1786400E G3	0.1130551E-03		
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	-0.59034645-00	0.99779466 00	J. 58: 14/6-01	0.4401041E CO	0.05053236-01	-0.1146428E 01		0
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	6.1999595= 35	0.15348908 01	0.36.4855E-01	-0.8457/76E-01	0.24397026-01	-0.1529036E 01		
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ň.	. C.3999 /9-16 UD	0.451183118 01	J-2522124F-01	-0.2539130b-0.1	0.542/2/41-02	-0.1656794E 01		
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	0.6999781E J1	0.79432475 01	U-2644430L-01	-0.2632/22E-02	-0.647/151E-04	-0.1986667E 01		
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	-9,79999988 00	0.1584894E 00	0.1006290E 01	0.1796500E 03	0.2723344E-U2	•
	-0.499995 00 -0.6999996 00	0.1779280E 00 0.1995263E 00	0.1037751E-01- 0.1039505E 01	0.1795784E 03 0.1794881E 03	0.3353436E=02 0.4108589F=02	
		0.1793203E 00	-0.1011587E-01-	0-1793740E-03	0.5003300E-02	
	-0.6000000E 00	0.25118868 00	0.1014026E 01	0.1792297E 03	0.6048955E-02	
	-0-5500001E-00-	0.28163826-00-		0.1790480E 03	0.7253017E=02	
	-0.5000001E 00	0.3162277F 00	0.10200344 01	0.1788203F 03	0.86145746-02	
	-0-4500402E-00-	0.35481336 00	0.10235534-01-	0.1785374E 03	0.10123245-01	
	-0.4000002E 00	0.3981070E 00	0.10274408 01	0.1781895E 03	0.1175650E-01	
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	-9.3000003E 00 -6.2500004E-00-	0-5623409E00	0.1019748E-01-	0.1766624E_03_	0.1702297E=01	
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3	-0.8499997E 00	0.1258924E-Q0 0.1412538E 00	-0.9994902E-00	-0.1008173E-01 -0.1010143E 01	-0.1005072E Ul	0.2187954F-02	
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•	-0.7499799E 00	0.17782806 00	-0.1000606E 01	-0.1015450E 61	-0.1007725E 01 	0.3120501E-02 0.3789346E-02	
9	-0.6500000E 00	0.1995263E_00 0.2238721E 00	-0.1000870E-01	-0.1018930E-01- -0.1023054E 01	-0.1011527E 01	0.4649825E-02	,
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3	-0.5500001E 00	0.28183826 00	-0.9996098E 00	-0.10334n3E 01	-0.1016702E 01	0.71884285-02	· ·
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3		0.5623409E 00	-0.9636770E-09- -0.9422776E 00	-0.1069126E 01- -0.1076424E 01	-0.1038212E 01	0.2837518E-01	
	-0.2500004E 00	0.50234072 00	-0.9114126E-00-	-0.1083002E 01	-0.1041501E-01	0.35241475-01	
•	-0.1500005E 00	0.7079450E 00	-0.86751%5E 00	-0.1088455E Ol	-0.1044228E 01	0.4345018E-01	1
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9	0.49903646-01	0.1122015E OL	-0.4092495E 00	-0.1090918E 01	-0.1045459E 01	0.9282982E-01	
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9	0.1497590E 00 6.1993592E-00	0.1412535E 01 0.1584890E 01	0.3256893E 00 	-0.10/46126 01 -0.1060303E 01	-0.1030151E_01	0.15248295 00	
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9	9-2993-786E-00	-0-1-99-52-566-01-	0-1274615E-02-	0.1015816E_01	-0.1007908E 01 -0.9919078E 00 '	0.2068093E-00 0.2373481E-00	
ש	0.3499988E 00	0.2238715E 01 0.2511881E 01	-0.1797743E 02 -0.71.3210E-01	-0.9838155E 00	-0.9719261E 00	0.27599495 00	
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9	0.5999988E 00 0.6499981E 00	0.4466816E 01	-0.2990175E 01	-0.5768185E 00	-0.7884094E 00	0.5373604E 00	**
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9	0.9499983E 00	0.89124748 01	-0.1715013E 01	0.7281504E 00 0.13/4160E 01	-0.1359243F 00	0.1250772E 01 0.1537979E 01	
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<u> </u>	0.1099396E 01	0.12589188 02	0.8753910E 00	0.30/6895E_01	0.1038445E 01	0.2092329E_01	
	0.11499988 01	0.1412530E 02	0.8576519E 00	0.2713143E 01 0.2024986E 01	0.8576546E UO 0.5124903E UO	0.1855491E 01 0.1520636E 01	•
3	0.119099EE_01_ 0.1249997E 01	0.1584886E 02 0.1778268E 02	0.4879668E_00_ 0.2555774E_00	0.1569994E 01	0.2849960E UO	0.1294746 01	
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9	0.1549997E 01	0.3548112E 02	0.1112295E-01	0.1023878E 01	0.1194000E-01	0.10.2211E 01	,
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Ð	0.1649997E 01 0.1699997E 01	0.4466803E 02 0.5011838E 02	0.4343934E-02 0.2725046E=02	0.1009090E 01 0.1005658E 01	0.4349020E-02	0.1002865E 01	
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D	0.1799997E_01	0.6369535E_02	0.1076775E=02,	0.1002202E_01_	0.1102448E=02 0.6904602E=03	0.1001109E 01 0.1000692E 01	
<b>U</b>	0.18499976 01	0.7079402E 02	0.6776147E-03 0.4265395E-03	0.1001378E 01 0.1000850E 01	0.6904602E=03 0.4329681E=03	0.10008928 01	
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9	-0.84999985 00	0.1412538E 00	-0.6003369E-04	0.4382975E-02	0.2197018E-02	-0.2659961E 0		
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<b></b>	-0.6999999£-00-	0-1995263E-00-	0.2629217E-03 0.3775638E-03-	0.6658338E-02 	0.3341928E-02 0.4091356E-02	-0.25057/4E 0:		6
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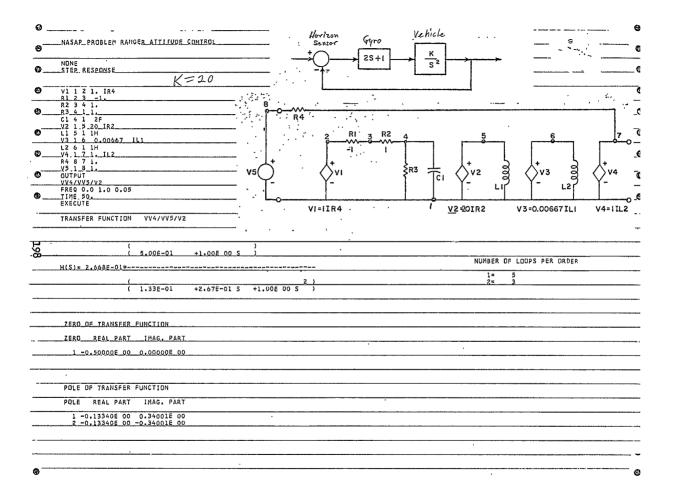
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		e (4),Q)	6,202	AB	S( CENS(4))			GLABS (SENS	(H)))				
٠		.95E-01	0.1157,016	e 01 0.	1000741E 01	0.6509	771E 00 -	0.9052085 0.3216951£ 0.2550571E	-03				
_	0. 499	## 1E=01	0.14:2537	(F 0) 0.	1000587E 01	0.5169	512E 00	U.2074340E	-03				
•	5.2499	,9 t U6	0.17/-276	FOL O.	10002946 01	0.4105	538E ()()	0.12754/26	-03				
	0.3497	7975 00 - 1975 00	0.223.715	EOL O.	10:0234E 01 10:0186E 01	0.3260	924E 00 856E 00	0.10145116	<b>-</b> 04				
	0.4499	94E_00	0.2819380	F 01 0.	1000147E_01 1000116E 01	0.2590	126E,00 )13E 00	0.63778326 0.50526468	-04				
٠.	0.5499	795E 00	0.3548130	E 01 0.	10000936 01 10000726 01	0.2057	230E 00	0.31476198	-04				
		994E 00	0.3931067		1060058E 01		179E 00 170E 00	0.25263965 0.19879958					
	0.,,997	.936 JJ .936 OG		E U1	10,0025t01	014263	352E00	0.15324218				· · · · · · · · · · · · · · · · · · ·	
	U.7999	978 JU	0.63: 1563	se of n.	1000uz3E 01	0.1156			-95				<i>-</i>
	. 0.5999	91E JU .	0.7943207	E 01 0.	10000141-01	0.9188	73DE-01.	0.62125876	-05				
		-916 UII	6.8712491 	.E. () 0 .	longuilt oi Locgooge oi	0.8189	146E-01 133E-01	0.49700/7E	-U5				
	LUG(FREQ)					1.06 ( A8 \$ (	SENSII						
•	LUG(FREQ)	-9.50±-05	-4.552-05	5.0vE-06	5.505-05	1.054-04	.55E-04 2	.05E-04 Z	.55E-04 3	.05E-04	3.55E-04 4	05E-04	
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	.5.0000£-01.	<i>-</i> :			**	<i></i>				••••••			
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	1.00004 00						* •*•••••			, ,,,,,,,,,,		•	

	. I DG(ER20)	FRFG	SENS (RE(H))	SENP(IN(H))	SENS(ABS(H))	SENS(PHL(H))	
0.	.0000.005 00					-0.7794116E-02 =0.6974593E-02	
Ŏ.	.4999995E-01	0-11220186-01-	0.8096220E-00-	0.1001353E Cl. 0.1001074E Ol	0.1000537E Ul	-0.6238859E-02	
	.99995956-01	0.12509258 01	0.8095778£ 00	0.10010746 01 0.10008536 01	0.1000426E_01	0.5578786E-02	
	-1499999E 00	0.141.2537E-01	0.80954375 00 0.80951661 00	U-1000677E 01	0.10003398 01	-0.4986938E-02	· ·
0	.1999994E 00	0.1584892F 01	0.8094950E-00	U.1000538E -01.		-0.4986938E-02 0.4456572E-02	
		0.15952616 01	0.2094779# 00	U.1000427E 01	0.10002146 01	-0 1001E20E-02	
0	.2999.976 00	0.22357196-01-		0.1000340E 01-	0.1000170E-01_	0.3556268E-02	
	.3999790E 00	0.25118350 01	0.60945321 00	U.1000269E 01	0.1000134E 01	-0.3175717E-02	
	.4499±96E00	G. 241-1805-05-	0.8034442E_00_	U - 1000214E -01-	0.1000107E_07	0.2635326E=02	
	10000065 00	0 41622765 01	0.80943746 00	0.1000170E 01	0.10000858 01	-0.2530954E-02	
	54997975-UQ	0.35411305_01_	0.80943;3E-00-	0.1600134E 01	0.1000067E_U1_		
0	.5999994E 00	0.3981007E 01	0.80942738,00			-0.2015772E-02 	
	.6499394E-UD	0.44658295.01.		0.10000024E 01.	0.1000044E_01	-0.1604602E-0Z	
	.6979 938 00	0.501(#65# 01	0.80942026 00	0.1000066E 01	0.1000032E 01	-0.1431390E=02	
	. 1499993E-00	0.55234055_01_	0.80.44.1921_00_	0.1000053E_01	0.1000JZ7E 01 0.1000JZ1E 01		
	.7999592E 00	0.63025638 01	0.8094174E 00	0.1000042E 01		-0.1276756E-02 =0.1138728E=02	
	.8499992E-00	0./0./9445E101_		0.1000032E_0L	0.1000013E U1	-0.1015543E-02	
0	.3999791E 00	0.79432676 01	0.8094155E 00	0.1000027E 01			
0	).9499591E_0Q ).9999/90E 00	0.9999978E 01	0.8094145E-00- 0.8094139E 00	0.1000016E G1	U.1000009E 01	-0.8075521E-03	
:					) 100((Chic(A2C(H))	) Ing/Sens(Dut(H))	
:					) 100((Chic(A2C(H))	) LOG(SENS(PHI(H))) 0,21002286_01	
	LBG(rREQ)	F330 0,1000000E-01-	LDG(SENS(RE(H)))	LOG(SENS(IM(H))	) L9G(SENS(AAS(H)) 0.3692873E=U3 -0.2935510E-U3	) LOG(SENS(PHI(H))) 	
0	LBG(rR#Q) ), 3000x CCE-00	F750 0,1000000E-01- 0.1122012E 01		LOG(SENS(IM(H)) 0.7344078E-03 -0.5373174E-03	) L9G(SENS(ABS(H)) 0.3692673E=U3. -0.2935510E=U3. -0.233118ZE=U3.	)) LOG(SENS(PHI(H))) 	
0	LBG(rR#Q) ), JOOO: COE-00 , 4997:75E-01 , 299799:E-01	F330 0,1000000E-01-	Lpg(SEMS(RE(H)))0.91.89234-01- 0.71718346-01	LOG(SENS(14(H)) 0.7340078E-03 0.734174E-03 0.4664251E-03 0.4704288E-03	) LOG(SENS(ABS(H)) 	1) LOG(SENS(PHI(H))) 	
	LBG(-REQ) ), 3000; 608-00- ), 4997;958-01 ; 3987;958-01- ; 7987975 U	F750 0,10600005E-01- 0.1122016E-01- 122015-55-01-	LDG(SENS(RE(H)))	LDG(SENS(11(H)) 0.7344078E-03 0.5973174E-03 0.4665251E-03 0.4705258E-63 0.2705258E-63	) L96(SENS(ABS(H)) 	1) LOG(SENS(PHI(H))) 	
0 0 0	LBG(rR#Q) ), JOOO: COE-00 , 4997:75E-01 , 299799:E-01	F730 0.1127012E 01 0.1127012E 01 0.1412757F 01 0.1412757F 01 0.171275F 01	LOG(SENS(RE(H))) -0.91.8923t-01- 0.91.7183ct-01- 0.91.74123c5-01- 0.91.795-16-01- 0.91.7482t-01- 0.91.76874t-01	LOG(SENS(1"(H1) 	) L06(SENS(A8S(H)) 0.30926738-02. -0.2935510E-03 -0.2321828-03. -0.1655110E-03 0.16700/3E-03. -0.1159536E-03	) LOG(SENS(PHI(H))) 0.2108222E-01 0.2156479E '01 0.2204894E-01 0.2273459E 01 0.2302161E-01 0.2302997E 01	
	LBG(-REQ)  0.0000000000000000000000000000000000	F730 0,10000000000000000000000000000000000	LOG(SENS(RE(H))) -0.91-89224-01- 0.7171836E-01 -0.91-74126-01 -0.917-7426-01 -0.917-74826-01 -0.917-7910-6-04	LOG(SENS(114(H))0.73400788-03 -0.59731748-03 -0.4662518-03 -0.4702288F-03 -0.4702288F-03 -0.27437908-03	) L9G(SEHS(ABS(H))	1) LOG(SENS(PHI(H)))	
	LUG(FREQ) 0,0000.CCE-00- 0,4997.99E-01 1,4997.99E-01 1,4997.97E-01 2,4997.8E-01 2,4997.8E-01 2,4997.8E-01	F7300,1069003E-01-0.1127012E 01-0.1127012E 01-0.141259F 01-0.171273E 01-0.171273E 01-0.171273E 01-0.171273E 01-0.22'.195 01-0.22'.195 01-0.22'.	LOG (SENS(RE(H))) -0.91-89234-01 -0.91-189234-01 -0.91-71936E-01 -0.91-74926-01 -0.917-74920 -0.917-96104-01 -0.917-96104-01	LDG(SENS(114H1) -0.7940078E-03 -0.5373174E-03 -0.370258E-03 -0.2943790E-03 -0.2943790E-03 -0.135510E-03 -0.135510E-03	) L0G(SENS(A8S(H))	) LOG(SENS(PHI(H))) 0.2108222E-01 0.2156479E 01 0.2253459E 01 0.2302161E-01 0.2302997E 01 0.239994E-01 0.239994E-01	
	LOG(-REQ) .0000 CCE-000000 CCE-00099795E-01 .799797E-00 .109797E-00 .2097977E-00 .3497977E-00	F730 	LOG(SENS(RE(H))) -0.91-8922+-01- 0.7171836E-01 0.91-74256-01 0.91795-16-01 0.9174826-01 0.91796746-01 0.91796106-04 0.91303196-01	LOG(SENS(]1(H1) 	) L9G(SEHS(ABS(H))	0) LOG(SENS(PHI(H))) 0.2104282-01 0.2104679-00 0.22044946-01 0.22043459-01 0.2302161E.01 0.2399946-01 0.2399946-01 0.2499010-01	
	LGG(-REQ) 0,5000.CGE-00- 0,4997.95E-01 1,7997.97E-01 1,7997.97E-00 1,7997.97E-00 1,7997.97E-00 1,7997.97E-00 1,7997.97E-00 1,7997.97E-00 1,7997.97E-00	F730 -0,1600008E-01 0.1127014F 01 0.122047.85 01 0.141257F 01 0.1571278 01 0.199(22)5-01 0.22'.195 01 0.25118486 01	LOG(SENS(RE(H))) -0.91-89228-01- 0.71718368-01 -0.9174256-01 -0.9174426-01- 0.91760746-01 -0.91780196-01 -1.109256-01 0.7110735-01	LDG(SENS(114H1) -0.7940078E-03 -0.5373174E-03 -0.5373174E-03 -0.3790E-03 -0.2943790E-03 -0.1355110E-03 -0.11/4214E-03 -0.11/4258E-03	) L0G(SENS(A8S(H))	) LOG(SENS(PHI(H)))	
	LGG(-REG) 1,0000; CGE-00 1,4997;95E-01 1,49979E-01 1,49979E-01 2,49398E-01 3,499997E-00 1,499997E-00 1,499998E-00 1,499998E-00	F730 	LDG(SENS(RE(H))) -0.91-8922-91- 0.7171836E-01 0.91-74126-01 0.91-74126-01 0.917195-16-01 0.91799101-01 0.91790101-01 0.91790101-01 0.91790101-01 0.91791010-01 0.91791010-01	LOG(SENS(]1(H1) 	) L9G(SEHS(ABS(H))	1) LOG(SENS(PHI(H)))	
	LUG(1-REQ) 0,0000,00E-00-00-00-00-00-00-00-00-00-00-00-00-	F730	LOG(SENS(RE(H))) -0.91-8923E-01- 0.717183GE-01 -0.9174125G-01 -0.9174425G-01 -0.9176074E-01 -0.9179010E-01 -0.9179010E-01 -0.9179010E-01 -0.9179010E-01 -0.9179010E-01 -0.9179010E-01 -0.9179010E-01 -0.9179010E-01	LDG(SZNS(114H))	) L0G(SENS(A8S(H))	1) LOG(SENS(PHI(H)))	
	LGG(FREQ),000.CGE.00,499795E-01,499795E-01,149979E-00,249798E-00,249798E-00,249796E-00,249796E-00,249796E-00,2497976E-00	F730	LOG(SENS(RE(H))) -0.91.8922x-01- 0.717183cE-01 0.91.74126c-01 0.917426c-01 0.9179576c-01 0.9179676c-01 0.9179600c-01 0.9179600c-01 0.9179600c-01 0.9179600c-01 0.9179600c-01 0.91797600c-01 0.917786c-01 0.917786c-01	LOG(SENS(]1(H1) 	) L9G(SEHS(ABS(H))	1) LOG(SENS(PHI(H)))	
	LD6(-REQ) ), \$\tilde{\text{\chi}}\), \$\tilde{\chi}\) 000. \$\tilde{\chi}\) 609. \$\tilde{\chi}\) 997. \$\tilde{\chi}\) 297. \$\tilde{\chi}\) 297. \$\tilde{\chi}\) 297. \$\tilde{\chi}\) 2497. \$\tilde{\chi}\) 2497. \$\tilde{\chi}\) 2497. \$\tilde{\chi}\) 2497. \$\tilde{\chi}\) 2497. \$\tilde{\chi}\) 2497. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\) 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}\\ 2499. \$\tilde{\chi}	F730 -0.1000003E-01 -0.1127012F 01 -1.22012F 01 -1.22012F 01 -0.1412537F 01 -0.154392E-01 -0.171273E 01 -0.22'.195 01 -0.2113435 01 -0.213435 01 -0.313435 01 -0.313435 01 -0.3134274E-01	LOG(SENS(RE(H))) -0.91c8923t-01- 0.717183tE-01 0.91741256-01 0.91741256-01 0.91780746-01 -0.91780746-01 0.91780746-01 0.91780746-01 0.91813786-01 0.91817866-01 0.91824178-01	LOG(SZNS(114H))	) L0G(SENS(A8S(H))	1) LOG(SENS(PHI(H)))	
	LOG(-REO) 1,0000; CCE-00 1,4997;95E-01 1,4997;95E-01 1,4997;95E-01 2,4937;8E-00 3,499997E-00 1,4499;95E-00 1,4499;95E-00 1,4499;95E-00 1,4999;95E-00 1,499E-00 1,499E-00 1,499E-00 1,499E-00 1,49E-00 1,49	F770	LOG (SENS(RE(H))) -0.91-8923-91- 0.7171836E-01 0.91741265-01 0.917495-6-01 0.91795-6-01 0.91796746-01 0.91796106-03 0.91303786-01 0.91313786-01 0.91313866-01 0.91313866-01 0.91313866-01 0.91313866-01 0.91313866-01	LOG(SENS(]1(H1) 	) LOG(SENS(ABS(H))	0) LOG(SENS(PHI(H))) 0, 21042326-01 0, 2154679-00 0, 2254679-00 0, 22549459-01 0, 2393459-01 0, 2393949-01 0, 2393997-01 0, 2393948-01 0, 249400-01 0, 24951528-01 0, 2547398-01 0, 2547398-01 0, 2547398-01 0, 27450618-01	
	LDG(-REQ)  , 4997;95E-01  , 4997;95E-01  , 4997;95E-01  , 1497;95E-01  , 2497;45E-01  , 2497;45E-01  , 2497;45E-01  , 2499;45E-01  , 2499;45E-01  , 2499;45E-01  , 4999;45E-01  , 4999;45E-01  , 599;494E-00  , 6999;49E-00  , 6999;49E-00  , 6999;49E-00	F770 -0.1000003E-01 -0.1127012F 01 -0.122012F 01 -0.12257F 01 -0.124892E-01 -0.171273E 01 -0.19402215-01 -0.22113436-01 -0.2313906-01 -0.34542745-01 -0.3941350 01 -0.3951067E-03 -0.446482E 01 -0.50413405E 01	LOG(SENS(RE(H))) -0.91-89232-01- 0.7171836E-01 0.91-741256-01 0.91-741256-01 0.91-7995-16-01 0.91-796-01 0.91-796-01 0.91-796-01 0.91-796-01 0.91-796-01 0.91-796-01 0.91-796-01 0.91-796-01 0.91-796-01 0.91-796-01 0.91-796-01 0.91-796-01 0.91-796-01 0.91-796-01 0.91-796-01 0.91-796-01	LOG(SZNS(17(H))	) L96(SENS(A8S(H))	0) LOG(SENS(PHI(H))) 0, 21042326-01 0, 2154679-00 0, 2254679-00 0, 22549459-01 0, 2393459-01 0, 2393949-01 0, 2393997-01 0, 2393948-01 0, 249400-01 0, 24951528-01 0, 2547398-01 0, 2547398-01 0, 2547398-01 0, 27450618-01	
	LUG(I-REQ)	F770	LOG(SENS(RE(H))) -0.91-8928-91- 0.7171836E-01 0.91741266-01 0.91741266-01 0.91748746-01 0.9179606-03 0.91303786-01 0.91303786-01 0.91313766-01 0.9131366-01 0.9132186-01 0.91325-11 0.91325-11 0.91325-11 0.91325-11 0.91325-11 0.91325-11 0.91325-11 0.91325-11 0.91325-11 0.91325-11	LOG(SENS(]7(H1) 	) LOG(SENS(ABS(H))	1) LOG(SENS(PHI(H))) -0.2108222-01 -0.2156479E 01 -0.2253459E 01 -0.239097E 01 -0.239097E 01 -0.249901E 01 -0.24990152E.01 -0.2547393F 01 -0.296712E.01 -0.2957548E.01 -0.27540501E 01 -0.27540501E 01 -0.27540501E 01 -0.27540501E 01 -0.27540501E 01 -0.27540501E 01 -0.27540501E 01 -0.27540501E 01 -0.27540501E 01 -0.27540501E 01 -0.27540501E 01 -0.27540501E 01 -0.27540501E 01 -0.27540501E 01 -0.27540501E 01 -0.27540501E 01	
	LDG(-REG)	F770 -0.10690003E-01-0.1127012E-01-0.1127012E-01-0.1127012E-01-0.112707E-01-0.1171270E-01-0.1171270E-01-0.1171270E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E-01-0.1171274E	LOG (SENS (RECH1)) -0.91-89238-01- 0.7171836E-01 0.91-74266-01 0.91-74826-01 0.91-796108-01 0.91-796108-01 0.91-796108-01 0.91-796108-01 0.91-796108-01 0.91-796108-01 0.91-796108-01 0.91-796108-01 0.91-796108-01 0.91-796108-01 0.91-796108-01 0.91-796618-01 0.91-796618-01 0.91-796618-01	LOG(SENS(11(H1))	) LOG(SENS(ABS(H))	0) LOG(SENS(PHI(H))) -0.21082328-01 -0.21564798' 01 -0.22524598' 01 -0.23921518-01 -0.23921518-01 -0.23921518-01 -0.24479011 01 -0.24479011 01 -0.24479018 01 -0.25473938' 01 -0.2646098' 01 -0.2646098' 01 -0.2646098 01 -0.27650618 01 -0.27650618 01 -0.27850618 01 -0.27850618 01 -0.2783288-01 -0.2783288-01	
	LDG(-REG)	F770	LOG(SENS(RE(H))) -0.91-8928-91- 0.7171636E-01 0.9174286-01 0.91747286-01 0.9179596-01 0.91796746-01 0.91796106-04 0.91796106-04 0.91796106-06 0.91737786-01 0.91737786-01 0.91737786-01 0.91737786-01 0.9172576E-01	LOG(SENS(]7(H1) 	) LOG(SENS(ABS(H))	1) LOG(SENS(PHI(H)))	

	ZERO	. RE4L	IPAG		SENSITIVITY	
	1	-0.5000V00E 00	0:000000E 00	0.0000U00E 00		
-	POLE	REAL	IRAG		SENSITIVITY	
	1	-0.40019906-01	0.1960058E 00	-0.4001988E-01	0.9391737E-01	,
	2	-0.4001990E-01	=0.1960058E_00	0.4001958E=01	±0.9391737E±01	
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-	STEP RESPONSE FUNCTION .	STEP	RESPONS	SE	
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	(-0.1334E 00 J 0.3400E 00 ) T	0.000		-0.59604645E-07 0.28948647E 00	
	(-0.5000E 00 J-0.1962E 00 ) E	0.200		0.593454661 00	
		0.300	OE 01	0.87331635E 00	
_	(-0,1334E 00 J-0,3400E 00 ) T	0.400		0.11023102E 01	
	(-0.5000E 00 J 0.1962E 00 ) E	0.500		0.12658339E 01 0.13602829E 01	
	( 0.0000E 00 J 0.0000E 00 ) T	0.700		0.13908958E 01	
	( 0.1000E 0) J 0.0000E 00 ) E	0.800	0E_01	0.1369077/E 01	
		0.900		U.13096333E 01	
		0,100		0.12282543C 01 0.11395025E 01	
		0.120		0.105538085 01	_
		0.130		0.984545956 00	
		0.140	0E_02	0.93208754E 00	
		0.150		0.89977700E 00	
		0.160		0.88663769E 00 0.88970166E 00	
		0.180	DE 02	0.90481949E 00	
_		0.190		0.92741/99E 00	
		0.200	0E_02	0.95312858E 00	
		0.210		0.97824574E 00	
_		0.220		0.10000000E 01	
		0.240		0.1016659/E 01 0.10274897E 01	
		0.250		0.10325994E 01	
		0.260		0.1032738/E 01	-
1-	_	0.270		0.10290546E 01	
	<u> </u>	0.2800		0.10228682E 01	
•	• /	0.2900		0.10154827E 01 0.10080338E 01	
		0.3100		0.10013990E 01	
		0.3200	DE 02	0.9961561eb 00	
		0.3300		0.992585606 00	
		0.3400		0.99070960E 00	
		0.3500		0.99034858E 00 0.99118954E 00	
		0.3700		0.99285364E 00	
	·	0.3800	E 02	0.9949554ZE 00	
		0.3900		0.99714911E 00	
		0.4000		0.999159101 00	
		0.4100		0.10007954E 01 0.10019560E 01	
		0.4300		0.10019380E 01	
		0.4400	E 02	0.10028229E 01	_
		0.4500		0.10026522E 01	
		0.4600		0.10022144E 01	
		0.4700	E 02	0.10016222E 01 0.10009813E 01	
		0.4900		0.100037576 01	
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					STEP	RESPUNSE								
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© 1,0000F 00*  LUGGIFREQ) PHI -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  0.0000F 00 **  *  2.5000E-01 **  *  *  7.5000E-01 **  *  *  7.5000E-01 **  *  *  *  *  *  *  *  *  *  *  *  *	# # # # # # # # # # # # # # # # # # #	1,0000E 00	* * * * * * * * * * * * * * * * * * *	EQ) PHI
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LOG(FREQ)  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  0.0090E 00  **  **  2.5000E-01  **  **  7.5000E-01  **  **  **  **  7.5000E-01	5000E-01	7.5000E-01	7.5000E-01  **  LOG(FREQ)  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  **  -2.5000E-01  **  -3.5000E-01  **  -3	-01
7.5000E-01  **  LOG(FREQ)  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  **  **  7.5000E-01  **  **  7.5000E-01	5000E-01	7.5000E-01	7.5000E-01  **  **  **  **  **  **  **  **  **	-01
7.5000E-01	5000E-01	7.5000E-01	7.5000E-01	-01
7.5000E-01		7.5000E-01	7.5000E-01	EQ)  -01  -02  -03  -04  -05  -05  -06  -07  -08  -08  -08  -08  -08  -08  -08
7.5000E-01 **  1.0000F 00 **  1.0000F 00 **  1.0000F 00 **  2.5000E-01 *  3. **  4. **  2.5000E-01 *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *  4. *		7.5000E-01	7.5000E-01	EQ)  -01  -02  -03  -04  -05  -05  -06  -07  -08  -08  -08  -08  -08  -08  -08
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# # # # # # # # # # # # # # # # # # #	0000E-01	5.0000E-01  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  -3.0000E-01  -	5.0000E-01	-01
# # # # # # # # # # # # # # # # # # #	0000E-01	5.0000E-01  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  -3.0000E-01  -	5.0000E-01	-01
# # # # # # # # # # # # # # # # # # #	0000E-01	5.0000E-01  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  -3.0000E-01  -	5.0000E-01	-01
5.0000E-01	0000E-01	5.0000E-01  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  -3.0000E-01  -	5.0000E-01	-01
# # # # # # # # # # # # # # # # # # #	0000E-01	5.0000E-01  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  -3.0000E-01  -	5.0000E-01	-01
# # # # # # # # # # # # # # # # # # #	0000E-01	5.0000E-01  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  -3.0000E-01  -	5.0000E-01	-01
# # # # # # # # # # # # # # # # # # #	0000E-01	5.0000E-01  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  -3.0000E-01  -	5.0000E-01	-01
# # # # # # # # # # # # # # # # # # #	0000E-01	5.0000E-01  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  -3.0000E-01  -	5.0000E-01	-01
# # # # # # # # # # # # # # # # # # #	0000E-01	5.0000E-01  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  -3.0000E-01  -	5.0000E-01	-01
# # # # # # # # # # # # # # # # # # #	0000E-01	5.0000E-01  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  -3.0000E-01  -	5.0000E-01	-01
5.0000E-01	0000E-01	5.0000E-01  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  -3.0000E-01  -	# # # # # # # # # # # # # # # # # # #	-01
5.0000E-01	0000E-01	5.0000E-01  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  -3.0000E-01  -	# # # # # # # # # # # # # # # # # # #	-01
# # # # # # # # # # # # # # # # # # #	0000E-01	5.0000E-01  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  -3.0000E-01  -	5.0000E-01	-01
5.0000E-01	0000E-01	5.0000E-01  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  -3.0000E-01  -	# # # # # # # # # # # # # # # # # # #	-01
# # # # # # # # # # # # # # # # # # #	0000E-01	5.0000E-01  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  -3.0000E-01  -	5.0000E-01	-01
5.0000E-01	.0000E-01	7.5000E-01	5.0000E-01	-01
5.0000E-01	.0000E-01	7.5000E-01	5.0000E-01	-01
5.0000E-01	.0000E-01	7.5000E-01	5.0000E-01	-01
5.0000E-01	.0000E-01	7.5000E-01	5.0000E-01	-01
5.0000E-01	.0000E-01	7.5000E-01	5.0000E-01	-01
5.0000E-01	.0000E-01	7.5000E-01	5.0000E-01	-01
5.0000E-01	.0000E-01	7.5000E-01	5.0000E-01	-01
5.0000E-01	.0000E-01	7.5000E-01	5.0000E-01	-01
5.0000E-01	.0000E-01	7.5000E-01	5.0000E-01	-01
5.0000E-01	.0000E-01	7.5000E-01	5.0000E-01	-01
5.0000E-01	.0000E-01	7.5000E-01	5.0000E-01	-01
5.0000E-01	.0000E-01	7.5000E-01	5.0000E-01	-01
7.5000E-01		7.5000E-01	7.5000E-01	EQ)  -01  -02  -03  -04  -05  -05  -06  -07  -08  -08  -08  -08  -08  -08  -08
7.5000E-01		7.5000E-01	7.5000E-01	EQ)  -01  -02  -03  -04  -05  -05  -06  -07  -08  -08  -08  -08  -08  -08  -08
7.5000E-01		7.5000E-01	7.5000E-01	EQ)  -01  -02  -03  -04  -05  -05  -06  -07  -08  -08  -08  -08  -08  -08  -08
7.5000E-01		7.5000E-01	7.5000E-01	EQ)  -01  -02  -03  -04  -05  -05  -06  -07  -08  -08  -08  -08  -08  -08  -08
7.5000E-01		7.5000E-01	7.5000E-01	EQ)  -01  -02  -03  -04  -05  -05  -06  -07  -08  -08  -08  -08  -08  -08  -08
7.5000E-01		7.5000E-01	7.5000E-01	EQ)  -01  -02  -03  -04  -05  -05  -06  -07  -08  -08  -08  -08  -08  -08  -08
7.5000E-01		7.5000E-01	7.5000E-01	EQ)  -01  -02  -03  -04  -05  -05  -06  -07  -08  -08  -08  -08  -08  -08  -08
7.5000E-01		7.5000E-01	7.5000E-01	EQ)  -01  -02  -03  -04  -05  -05  -06  -07  -08  -08  -08  -08  -08  -08  -08
7.5000E-01		7.5000E-01	7.5000E-01	EQ)  -01  -02  -03  -04  -05  -05  -06  -07  -08  -08  -08  -08  -08  -08  -08
7.5000E-01		7.5000E-01	7.5000E-01	EQ)  -01  -02  -03  -04  -05  -05  -06  -07  -08  -08  -08  -08  -08  -08  -08
7.5000E-01		7.5000E-01	7.5000E-01	EQ)  -01  -02  -03  -04  -05  -05  -06  -07  -08  -08  -08  -08  -08  -08  -08
7.5000E-01		7.5000E-01	7.5000E-01	EQ)  -01  -02  -03  -04  -05  -05  -06  -07  -08  -08  -08  -08  -08  -08  -08
7.5000E-01		7.5000E-01	7.5000E-01	EQ)  -01  -02  -03  -04  -05  -05  -06  -07  -08  -08  -08  -08  -08  -08  -08
7.5000E-01 **  **  **  1.0000E 00 **  **  **  1.0000E 00 **  **  **  **  **  **  **  **  **	5000E-01	7.5000E-01	7.5000E-01	-01
7.5000E-01 **  **  **  1.0000E 00 **  **  **  1.0000E 00 **  **  **  **  **  **  **  **  **	5000E-01	7.5000E-01	7.5000E-01	-01
7.5000E-01	5000E-01	7.5000E-01	7.5000E-01	-01
7.5000E-01	5000E-01	7.5000E-01	7.5000E-01	-01
7.5000E-01	5000E-01	7.5000E-01	7.5000E-01	-01
7.5000E-01	5000E-01	7.5000E-01	7.5000E-01	-01
7.5000E-01	5000E-01	7.5000E-01	7.5000E-01	-01
7.5000E-01	5000E-01	7.5000E-01	7.5000E-01	-01
7.5000E-01	5000E-01	7.5000E-01	7.5000E-01	-01
Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo	# # # # # # # # # # # # # # # # # # #	1,0000E 00	1,0000E 00 ** * * * * * * * * * * * * * *	EQ) PHI
Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo   Todo	# # # # # # # # # # # # # # # # # # #	1,0000E 00	1,0000E 00 ** * * * * * * * * * * * * * *	EQ) PHI
1.0000E 00 **  LOG(FREQ) PHI  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  0.0000E 00 **  2.5000E-01 **  *  7.5000E-01 **  *  7.5000E-01 **	# # # # # # # # # # # # # # # # # # #	1,0000E 00	1.0000E 00	EQ) PHI
1.0000E 00 **  LOG(FREQ) PHI  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  0.0000E 00 **  2.5000E-01 **  *  7.5000E-01 **  *  7.5000E-01 **	# # # # # # # # # # # # # # # # # # #	1,0000E 00	1.0000E 00	EQ) PHI
1.0000E_00 *  LUG(FREQ) PHI	0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E	1,0000E 00	1.0000E 00 **.  LOG(FREQ)  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  0.0000E 00 **  *  2.5000E-01 **  *  7.5000E-01 **  *  *  7.5000E-01 **  *  *  *  *  *  *  *  *  *  *  *  *	PHI  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -01  -01  -01  -01  -01  -01  -01  -
1.0000E 00	0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E	1,0000E 00	1.0000E 00 **.  LOG(FREQ)  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  0.0000E 00 **  *  2.5000E-01 **  *  7.5000E-01 **  *  *  7.5000E-01 **  *  *  *  *  *  *  *  *  *  *  *  *	PHI  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -01  -01  -01  -01  -01  -01  -01  -
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1.0000E 00	0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E	1,0000E 00	1.0000E 00 **.  LOG(FREQ)  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  0.0000E 00 **  *  2.5000E-01 **  *  7.5000E-01 **  *  *  7.5000E-01 **  *  *  *  *  *  *  *  *  *  *  *  *	PHI  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -01  -01  -01  -01  -01  -01  -01  -
1,0000E-00 *  LUG(FREQ) PHI	0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  0000E	1,0000E 00	1.0000E 00 **  LUG(FREQ)  -2.00E 02 -1.00E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  0.0000F 00 **  *  2.5000E-01 **  *  7.5000E-01 **  *  7.5000E-01 **	PHI  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -01  -01  -01  -01  -01  -01  -01  -
LQG(FREQ)  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  *  *  *  5.0000E-01  *  *  7.5000E-01  *  *  *  *  *  *  *  *  *  *  *  *  *	QG(FREQ) PHI -2.006 02 -1.606 02 -1.206 02 -8.006 01 -4.006 01 0.006 00 4.006 01 1.206 02 1.606 02 2.006 02	LUG(FREQ)  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -3.5000E-01  -3	LQG(FREQ)  -2.006 02 -1.00E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.500E-01  -2.5000E-01  -2.500E-01  -2.500	EQ) PHI -2.006 02 -1.606 02 -1.206 02 -8.006 01 -4.006 01 0.006 00 4.006 01 1.206 02 1.606 02 2.006 02 02 00 00 00 00 00 00 00 00 00 00 00
LQG(FREQ)  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  *  *  *  5.0000E-01  *  *  7.5000E-01  *  *  *  *  *  *  *  *  *  *  *  *  *	QG(FREQ) PHI -2.006 02 -1.606 02 -1.206 02 -8.006 01 -4.006 01 0.006 00 4.006 01 1.206 02 1.606 02 2.006 02	LUG(FREQ)  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -3.5000E-01  -3	LQG(FREQ)  -2.006 02 -1.00E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.500E-01  -2.5000E-01  -2.500E-01  -2.500	EQ) PHI -2.006 02 -1.606 02 -1.206 02 -8.006 01 -4.006 01 0.006 00 4.006 01 1.206 02 1.606 02 2.006 02 02 00 00 00 00 00 00 00 00 00 00 00
LQG(FREQ) PHI	QG(FREQ) PHI -2.006 02 -1.606 02 -1.206 02 -8.006 01 -4.006 01 0.006 00 4.006 01 1.206 02 1.606 02 2.006 02	LUG(FREQ)  -2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -3.5000E-01  -3	LOG(FREQ)  -2.00E 02 -1.00E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.5000E-01  -2.500E-01  -2.5000E-01  -2.500E-01  -2.5000E-01  -2.500E-01  -2.50	EQ) PHI -2.006 02 -1.606 02 -1.206 02 -8.006 01 -4.006 01 0.006 00 4.006 01 1.206 02 1.606 02 2.006 02 02 00 00 00 00 00 00 00 00 00 00 00
-2.006 02 -1.606 02 -1.206 02 -8.006 01 -4.006 01 0.006 00 4.006 01 1.206 02 1.606 02 2.006 02	-2.006 02 -1.60E 02 -1.80E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.006 02 -1.60E 02 -1.80E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02	-2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02	-2.006 02 -1.00E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.00E 02 2.00E 02  -2.0000E 00 **  *  *  2.5000E-01 **  *  *  *  *  *  *  *  *  *  *  *  *	-2.00f 02 -1.60f 02 -1.20f 02 -8.00f 01 -4.00f 01 0.00f 00 4.00f 01 1.20f 02 1.60f 02 2.00f 02 00 00 00 00 00 00 00 00 00 00 00 00
-2.006 02 -1.606 02 -1.206 02 -8.006 01 -4.006 01 0.006 00 4.006 01 1.206 02 1.606 02 2.006 02	-2.006 02 -1.60E 02 -1.80E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.006 02 -1.60E 02 -1.80E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02	-2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02	-2.006 02 -1.00E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.00E 02 2.00E 02  -2.0000E 00 **  *  *  2.5000E-01 **  *  *  *  *  *  *  *  *  *  *  *  *	-2.00f 02 -1.60f 02 -1.20f 02 -8.00f 01 -4.00f 01 0.00f 00 4.00f 01 1.20f 02 1.60f 02 2.00f 02 00 00 00 00 00 00 00 00 00 00 00 00
-2.000 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02	-2.006 02 -1.60E 02 -1.80E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.006 02 -1.60E 02 -1.80E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02	-2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02	-2.006 02 -1.006 02 -1.206 02 -1.206 02 -1.206 02 -1.006 00 4.006 01 8.006 01 1.206 02 1.006 02 2.006 02 02 02 02 02 02 02 02 02 02 02 02 02	-2.00f 02 -1.60f 02 -1.20f 02 -8.00f 01 -4.00f 01 0.00f 00 4.00f 01 1.20f 02 1.60f 02 2.00f 02 00 00 00 00 00 00 00 00 00 00 00 00
-2.000 02 -1.60E 02 -1.70E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02	-2.006 02 -1.60E 02 -1.80E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.006 02 -1.60E 02 -1.80E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02	-2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02	-2.00E 02 -1.00E 02 -1.20E 02 -1.20E 02 -8.00E 01 -4.00E 01 8.00E 01 1.20E 02 1.60E 02 2.00E 02  0.0000E 00	-2.00f 02 -1.60f 02 -1.20f 02 -8.00f 01 -4.00f 01 0.00f 00 4.00f 01 1.20f 02 1.60f 02 2.00f 02 00 00 00 00 00 00 00 00 00 00 00 00
-2.000 02 -1.60E 02 -1.70E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02	-2.006 02 -1.60E 02 -1.80E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.006 02 -1.60E 02 -1.80E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02	-2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02	-2.00E 02 -1.00E 02 -1.20E 02 -1.20E 02 -8.00E 01 -4.00E 01 8.00E 01 1.20E 02 1.60E 02 2.00E 02  0.0000E 00	-2.00f 02 -1.60f 02 -1.20f 02 -8.00f 01 -4.00f 01 0.00f 00 4.00f 01 1.20f 02 1.60f 02 2.00f 02 00 00 00 00 00 00 00 00 00 00 00 00
-2.000 02 -1.60E 02 -1.70E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02	-2.006 02 -1.60E 02 -1.80E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.006 02 -1.60E 02 -1.80E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02	-2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02	-2.00E 02 -1.00E 02 -1.20E 02 -1.20E 02 -8.00E 01 -4.00E 01 8.00E 01 1.20E 02 1.60E 02 2.00E 02  0.0000E 00	-2.00f 02 -1.60f 02 -1.20f 02 -8.00f 01 -4.00f 01 0.00f 00 4.00f 01 1.20f 02 1.60f 02 2.00f 02 00 00 00 00 00 00 00 00 00 00 00 00
-2.000 02 -1.60E 02 -1.70E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02	-2.006 02 -1.60E 02 -1.80E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02  -2.006 02 -1.60E 02 -1.80E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02	-2.00E 02 -1.60E 02 -1.20E 02 -8.00E 01 -4.00E 01 0.00E 00 4.00E 01 1.20E 02 1.60E 02 2.00E 02	-2.00E 02 -1.00E 02 -1.20E 02 -1.20E 02 -8.00E 01 -4.00E 01 8.00E 01 1.20E 02 1.60E 02 2.00E 02  0.0000E 00	-2.00f 02 -1.60f 02 -1.20f 02 -8.00f 01 -4.00f 01 0.00f 00 4.00f 01 1.20f 02 1.60f 02 2.00f 02 00 00 00 00 00 00 00 00 00 00 00 00
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0.0000E 00 **  **  2.5000E-01 **  **  5.0000E-01 **  7.5000E-01 **	0000E-01 **  0000E-01 **  0000E-01 **  0000E-01 **  **  **  **  **  **  **  **  **  **	0.0000E 00 **  **  2.5000E-01 **  **  5.0000E-01 **  7.5000E-01 **  **  **  **  **  **  **  **  **  **	0.0000E 00 **	00 ************************************
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7.5000E-01	5000E-01 **	7.5000E-01	5.0000E-01	:01
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7.5000E-01	5000E-01 **	7.5000E-01	5.0000E-01	:01
7.5000E-01	5000E-01 **	7.5000E-01	7.5000E-01	:01
7.5000E-01	5000E-01 **	7.5000E-01	5.0000E-01	:01
7.5000E-01	5000E-01 **	7.5000E-01	7.5000E-01	:01
7.5000E-01	5000E-01 **	7.5000E-01	5.0000E-01	:01
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7.5000E-01	0000E-01	7.5000E-01	7-5000E-01 **  7-5000E-01 **	:01
7.5000E-01	0000E-01	7.5000E-01	7.5000E-01	:01
7.5000E-01	5000E-01	7,5000E-0i	7.5000E-01	
7.5000E-01	5000E-01	7,5000E-0i	7.5000E-01	
7.5000E-01	5000E-01	7,5000E-0i	7.5000E-01	
7.5000E-01 **	5000E-01	7,5000E-0i	7.5000E-01	
7.5000E-01 **	5000E-01	7,5000E-0i	7.5000E-01	
7.5000E-01	5000E-01	7,5000E-0i	7.5000E-01	
7.5000E-01	5000E-01	7,5000E-0i	7.5000E-01	
7.5000E-01	5000E-01	7,5000E-0i	7.5000E-01	
7.5000E-01	5000E-01	7.5000E-01	7.5000E-01	· · · · · · · · · · · · · · · · · · ·
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Ø	SENSITIVITY ANALYSIS **						6
<b>o</b> –	SENSITIVITY ANALISIS TO						
8	LDG(FREQ)FRLQ	ABS(SENS(H))	PHI (SENS(H)	)LQG(ABS(SENS()	1)))		
•	0.0000000E 00 0.10000 0.4999995E-01 0.11220 0.9999990E-01 0.12589	00E 01 0.100Z481E 01 18E 01 . 0.1001969E 01	0.2439694E ( 0.2173139E ( 0.1935930E (	01 0.1075936E-0	)2 )3		
	0.1499799E 00 0.14125 0.1999998E 00 0.15848	37E 01 0.1001242E 01	U.1724776E	01 0.53892176-0	)3	· · · · · · · · · · · · · · · · · · ·	
₾	0.2499998E 00 0.17762 0.2999997E 00 0.19952	78E 010.1000783E_01 61E 010.1000621E_01 ,	0.1369333 <u>E (</u>	01 0.33990486-0 01 0.26954436-0	93		
Ø	0,349997E_000.22387 0,3999'96E_000.25118 0,4499'96E_000.28183	85E 01 0.1000391E 01 80E 01 0.1000312E 01	0.9689891E (	00 0.16977878-0 00 0.13541425-0	13		
Ø _	0.4999/95E 00 0.31622 0.5499995E 00 0.35481	30E 01 0.1000196E 01	0.7695715E 0	00 0.85311/7E-U	14		
ø ·	0.5997994E 00 0.39810 0.6499994E 00 0.44668 0.4979993E 00 0.50116	29E 010.1000124E 0165E 010.1000097E 01	0.5447392E 0.4854859E	00 0.5383947t-0	94		
	0,749993E 00 0,56234 0,799992E 00 0,630936 0,8499992E 00 0,70794	63E 01 0.1000061E 01	0.4326795E ( 0.3856190E ( 0.3436785E (	00 0.33546916~0 00 0.26506426~0	14		
•	0.8999991E 00 0.794320 0.9999991E 00 0.891245	67E U1 0.1000038E 01	0.3063000E (	0.16566/01-0	14		
0	0.7999790E 00 0.99999	78E 01 0.1000024E 01	0,24,2992E	0.10354261-0			· · ·
<b>o</b>							
ø	-9.20E-04 -7.20E-04 0.0000E 00	4 -5.20E-04 -3.20E-04 -1.7	LUG(ABS(SENS)	)) -05 2.80&-04 4.8	0E-04 6.80E-04 8	80E-04 1.08E-03	
<u> </u>	0.0000E 00	***************************************			*	· · · · · · · · · · · · · · · · · · ·	
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0	2.5000E-01			*.			ø
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Θ-	5.0000E-01			· · · · · · · · · · · · · · · · · · ·		<u></u>	
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•	7.5000E-01	• • • • • • • • • • • • • • • • • • • •	*				
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ø	1,0000E 00		*********			• • • • • • • • • • • • • • • • • • • •	
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	LOG (FREQ)	2 -1.20E 02 -8.00E 01 -4.0	PHI (SENS)	) 40°	05 01 1 205 02 1	60E 02 7 00E 02	
	0.0000E 00	1 -1.200 02 -0.000 01 -4.0	***************************************			***************************************	
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•	2.5000E-01		******		· · · · · · · · · · · · · · · · · · ·		
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	5.0000F-01	· · · · · · · · · · · · · · · · · · ·	* • • • • • • • • • • • • • • • • • • •		• •••••••••••	, , , , , , , , , , , , , , , , , , ,	
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o	7.5000E-01	***************************************	*	.,	***************************************		····· @
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0	1.0000F 00		*		*	• •	<b>6</b> .

6 _ <sub>SE</sub>	NSITIVĪTI	ES OF ZERUES AND	POLES OF TRANSFER F	UNCTION		
9 <sup></sup>	<del> </del>					· · · · · · · · · · · · · · · · · · ·
Ð	ZERO	REAL	IMAG	REAL	SENSITIVITY INAG 0.0000000E 00	
	.1 .	-0.4999998E 00	0.0000000E 00	REAL -0.4468126E-06	0.0000000 00	
9					•	
B	POLE	REAL	IMAG	REAL	SENSITIVITY IMAG 0.1438336E 00	
	1 2	-0.1333996E 00 -0.1333996E 00	0.3400062E 00 -0.3400062E 00	REAL -0.1333997E 00 -0.1333997E 00	0.1438336E 00 -0.1438336E 00	
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<b>9</b>						•
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) NASAP PROBLEM RANGER ATTITUDE CONTROL	
NONE———————————————————————————————————	
3 SIEN VESKOUZE	
V1-1-2-1,-IR4 R1 2 3 -1. R2 3 4 1.	
R3 4 1 1. DC1_4_12F	
V2 1 5 75 IR2 L1_5_1_1H	
9 1 6 0.00667 IL1	
V4 1 7 1. IL2	
V5 1 8 1,	
7 VV4/VV5/V2 FREQ 0.0 1.0 0.05	
TIME 50. D EXECUTE	,
TRANSFER-FUNCTION	NUMBER-OF-LOOPS-PER-ORDER
20	- 1- 5
<u> </u>	NUMBER-OF-LOOPS-PER-ORDER
5.00E-01 +1.00E 00 S	- 1- 5
5.00E-01 +1.00E 00 S )  H(S)= 1,000E 00*	- 1- 5
5.00E-01 +1.00E 00 S	- 1- 5
( 5.00E-01 +1.00E 00 S )  H(S)= 1.000E 00*	- 1- 5
( 5.00E-01 +1.00E 00 S )  H(S)= 1,000E 00*	- 1- 5
5.00E-01 +1.00E 00 S  H(S)= 1.000E 00*  ( 5.00E-01 +1.00E 00 S +1.00E 00 S )  ZERO OF TRANSFER FUNCTION  ZERO REAL PART IMAG. PART	- 1- 5
( 5.00E-01 +1.00E 00 S )  H(S)= 1.000E 00*	- 1- 5
S	- 1- 5
( 5.00E-01 +1.00E 00 S )  H(S)= 1.000E 00*	- 1- 5
	1 = 5 2 = 3
( 5.00E-01 +1.00E 00 S )	1 = 5 2 = 3

	STEP-RESPONS	E	
·			
	0.0000E 00	-0.23841858E-06	
	0.1000E_01_	0.75870979E_00	
(-0.5000E 00 J-0.5002E 00 ) E	0.2000E 01 0.3000E01	0,11108913E 01 0,12067432E 01	
(-0.5002E 00 J-0.5000E 00 ) T .	0.4000E 01	0.11792612E 01	
	0.5000E.01	0,11147690E. 01	
•	0.6000E 01	0.10562334E 01	
( 0.0000E 00 J 0.0000E 00 ) T	0.7000E 01	0.10176487E_01	
( 0.1000E 01 J 0.0000E 00 ) E	0.8000E 01	0.99810702E 00	
	0.9000E_01	0.99149549E.00	
	0.1000E 02	0.99164456E 00 0.99423426E 00	
	0.1100E_02 0.1200E_02	0.99693567E 00	
	0.1200E 02	0.99885851E_00	
	0.1406E 02	0.99991173E 00	
	0.1500E-02-	0.10003252E_01	
	0.1600E 02	0.10003786E 01	
	0.1700E_02	0. 10002832E _01	
	0.1800E 02	0.10001621E 01	
	0→1-900E02	0.10000677E-01	,
	0.200UE 02	0,10000124E 01	
	0.2100E-02 0.2200E 02	0.99998844E_00 0.99998283E_00	
	0.2300E-02	0.99998581E_00	•
	0.2400E 02	0.99999106E 00	
	0.2500E-02	0.99999553E_00	
	0.2600E 02	0.99999839E QO	
	0.2700E_02	0.9999976E_00	
•	0.2800E 02	0.10000000E 01	
	0.2900E_02	0.10000000E_01	
	0.3000E 02	0.99999994E 00	
\$	0.3100E 02 0.3200E 02	0.99999970E 00 0.99999958E 00	
	0.3300E-02	0.9999995ZE 00	
	0.3400E 02	0.99999946E 00	
·	0.3500E_02	0.99999946E_00	
	0.3600E 02	0.99999946E 00	
	0.3700E 02	0.99999946E_00	
	0.3800E 02	0.99999946E 00	
	0.3900E_02	O.99999952E_00	<del> </del>
	0.4000E 02	0.99999952E 00	
	0.4100E_02	0,99999952E_00	<del></del>
	0.4200E 02 0.4300E 02	0.99999952E 00 0.99999952E 00	
· · · · · · · · · · · · · · · · · · ·	0.4400E 02	0,99999952E 0U	
	0.4400E 02	0.99999952E_00_	
	0.4600E 02	0.99999952E 00	
	0.4700E_02	0.99999952E_00	
	0.4800E 02	0.99999952E 00	
	0.490UE 02	0.99999952E 00	
	0.5000E 02	0,99999952E 00	
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## CHAPTER VII

## SPECIAL CONTROL SYSTEM EXAMPLES

In the previous chapters of this manual we have used a variety of control circuit problems to illustrate various facets of computer aided design with NASAP. The examples were basic to control theory with explicit or implicit connection to aerospace applications. In this final chapter we have selected a few control system examples that emphasize the capabilities and also the limitations of the present version of NASAP as modified at the Moore School. From these examples it will be apparent that, in general, NASAP can be an effective aid to the control system engineer dealing with moderately complex linear control systems.

## VIIA EXAMPLE INVOLVING TIME DOMAIN APPROXIMATION

Approximation of system response is a long standing problem related to control system analysis and synthesis. It is often necessary to approximate a system before suitable compensation can be applied. Eisenberg [EI 1] has described a technique for approximately identifying high order system responses based on certain characteristic responses to a unit step input. Many feedback systems exhibit time domain response to a unit step input that includes an overshoot followed by variations which subsequently settle to a steady state value. The approximate system response is generated by a closed loop transfer function whose open loop transfer function contains a transport lag and a first order lag. This technique only requires knowledge of the first peak overshoot, the time to peak and the settling time of the unknown system response.

We represent the unknown response by that of a unity-feedback control system with G(s) representing the plant. The general form of G(s) is assumed to be

$$G(s) = \frac{K_{p}e^{-sTd}}{\tau s + 1}$$
 (7.1)

This particular approximation is quite convenient and yields the system transfer function

$$\frac{C}{R}(s) = \frac{G(s)}{1 + G(s)} = \frac{\frac{K}{\tau} e^{-sTd}}{s + \frac{1}{\tau} + \frac{K}{\tau} e^{-sTd}}$$
(7.2)

To facilitate further consideration of this expression, we normalize it with respect to  $\mathbf{T}_{d}$ . Defining

$$\overline{s} = T_a s = \sigma T_a + j\omega T_a = \overline{\sigma} + j\omega$$

we can write

$$\frac{\mathbf{C}}{\mathbf{R}}(\mathbf{\bar{s}}) = \frac{\alpha e^{-\mathbf{\bar{s}}}}{\mathbf{\bar{s}} + 6 + \alpha e^{-\mathbf{\bar{s}}}} \tag{7.3}$$

where

$$\alpha = \frac{K_p T_d}{\tau}, \beta = \frac{T_d}{\tau}, \alpha = K_p \beta$$

The problem of system approximation is now reduced to that of determining the parameters  $\alpha$  and  $\beta$  such that the denominator of (7.3) has a pair of clearly dominant complex conjugate roots which will exhibit a second-order response. In particular it is desired that the responses shown in Fig. 7.1 be similar, for the set of conditions

$$M_h \cong M_s = M,$$
  $T_{ph} \cong T_{ps} = T,$   $T_{sh} \cong T_{ss} = T_s$  (7.4)

where the values of  $M_h$ ,  $T_{\mathrm{ph}}$ , and  $T_{\mathrm{sh}}$  are measured from the unknown system step response.

One way of accomplishing the selection of  $\alpha$  and  $\beta$  is to use the generalized curves found in [EI 1]. An alternative is to find a suitable electric circuit model for G(s) in (7.1) and then use NASAP. The new feature here is the exponential,  $e^{-sTd}$ . We can obtain a rational function representation for this exponential by a Padé approximation. Specifically we use the biquadratic

$$\frac{s^2 - as + b}{s^2 + as + b}$$

In Chapter III, we showed how to obtain a ladder network for this with negative as well as positive elements. The input impedance of the network is the desired circuit model.

To illustrate this approximation technique we again consider the seventh order system with an open loop transfer function

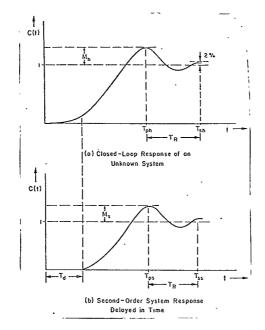


Fig. 7.1 System Approximation by Time Domain Response (Subscripts "h" and "s" refer to higher order and second order system respectively)

$$G(s) = \frac{1}{(6s+1)(2s+1)^3(s+1)^3}$$
 (7.5)

The step response for this in a unity feedback system was given in Chapter V as the "Eisenberg" problem. Consideration of the actual closed-loop, unit step response of this system, the lower response curve shown in Fig. 7.2 from [EI 1], yields the three data point  $M_h = 31.7\%$ ,  $T_{\rm ph} = 20$ s, and  $T_{\rm sh} = 55.4$ s<sup>2</sup>.

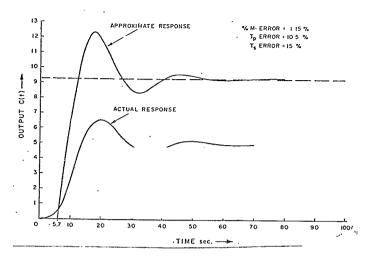


Fig. 7.2 Comparison of System Time Responses.

To obtain the approximate system parameters we must fall back on the well known relationships for a second-order system

$$M_{s} = e^{\frac{2}{3}\left(\frac{\pi k^{2}}{\sqrt{1-\xi^{2}}}\right)}$$
(7.6)

$$T_{ps} = \frac{\pi}{\omega_n \sqrt{1 - \zeta^2}} \tag{7.7}$$

$$T_{ss} = \frac{\mu}{\zeta \omega_s}$$
 (for a 2% deviation of the response envelope from the steady-state value) (7.8)

The determination of  $\zeta$  and  $\omega_n$  and ultimately location of the dominant roots involves use of (7.4). Since  $M_h \cong M_s$ , where  $M_h$  is a measured quantity, we have the numerical value  $M_s$ . Hence the value of  $\zeta$ -can either be computed from (7.6) as

$$\zeta = \frac{|\ln M|}{\sqrt{(\ln M)^2 + \frac{r^2}{\pi^2}}} \tag{7.9}$$

or it can be obtained from a universal curve of M versus  $\xi$ . Next to determine  $\omega_{\rm n}$ . Note from Fig. 7.1 a and b and (7.4) that

$$T_{R} = T_{sh} - T_{ph} = T_{ss} - T_{ps}$$
 (7.10)

Substituting the required values and solving for  $\omega_{_{\!\boldsymbol{\eta}}}$  gives

$$\omega_{n} = \frac{\frac{1}{T_{R} \zeta} - \frac{\pi}{T_{R} \sqrt{1 - \zeta^{2}}}$$
 (7.11)

Since  $\zeta$  is known  $\omega_n$  can be expressed in terms of measured quantities as

$$\omega_{\rm n} = \frac{\sqrt{(\ln M)^2 + \pi^2}}{T_{\rm p}} \left( \frac{\mu}{|\ln M|} - 1 \right)$$
 (7.12)

Next we find Td as a function of the measured parameters. From Fig. 7.1a and b

$$T_{d} = T_{ph} - T_{ps} \tag{7.13}$$

where  $T_{ph}$  is a measured quantity and  $T_{ps}$  can be obtained from (7.7). Substituting (7.7) into (7.13) gives

so that the values of  $\zeta$ ,  $\omega_n$ , and  $T_d$  are completely specified from the key characteristics of the unknown system response. Thus the values of the approximate system parameters are found to be  $T_d = 5.7s$ ,  $\tau = 89.7s$ , and

 $K_{p} = 13.1$ . These give an approximate open-loop transfer function of

$$G(s) = \frac{13.1e^{-5\cdot 7s}}{89.7s + 1}$$
 (7.15)

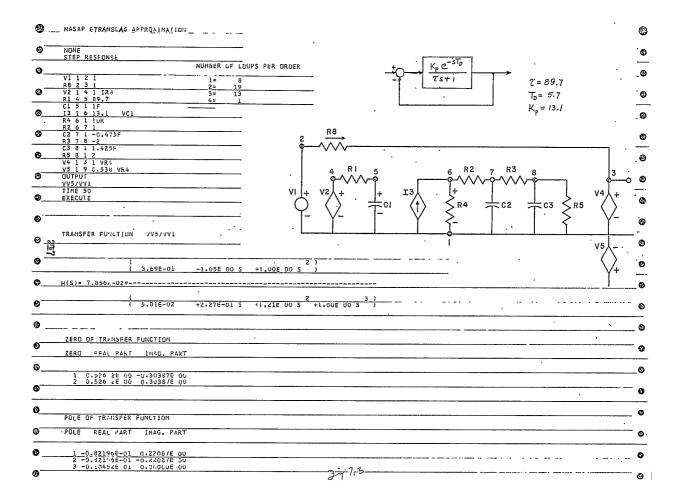
The closed-loop response corresponding to this G(s) obtained in the reference is shown in the upper response curve in Fig. 7.2. The percentage differences between the indicated characteristics of the two responses are also shown. It should be pointed out that altough the responses match quite closely with respect to M,  $T_p$ , and  $T_s$  the steady-state levels will not match. This mismatch is unimportant because the steady-state levels can always be matched exactly by simply adding gain outside the feedback loop. Also the gain of the unknown system response is easily computed from the measurable steady-state level, ( $c_{ss}(t)$ ), via the relationship

$$K = \frac{c_{SS}(t)}{1 - c_{SS}(t)}$$
 (7.16)

The NASAP print out and step response for (7.15) is shown in Figs. 7.3 and 7.4.

It should be noted for aerospace control applications a distinct advantage of the technique is that it is not necessary to open any feedback loops to effect the approximation. Thus, the system response can be approximated without interrupting normal operation. This is in contrast to some methods of system approximation, this technique is not hampered by the rare cases where the open-loop response is oscillatory. There are other methods available for system approximation that can be used on a closed-loop basis but these methods usually require that the system gain be increased until critical cycling is attained (oscillations). For many practical applications, however, it is not advisable to bring a control system to the verge of instability.

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## VIIB EXAMPLE OF A CONTROL SYSTEM WITH TRANSPORT LAG

As an extension of the concepts introduced in the previous example, we consider a given control system that has a plant with transport lag along with three simple lags shown in Fig. 7.5. Lupfer and Oglesby [LU 1] discussed such a problem wherein the object was to find a proportional-integral controller. They treated this problem with the aid of an analog computer. An alternative solution was presented by Eisenberg [EI 2] using the parameter plane approach to develop a graphical technique.

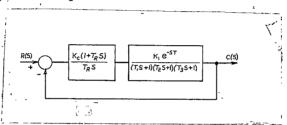


Fig. 7.5 Control system with transport lag Reactor process from [LU 1]

To use NASAP we must obtain a circuit model for the control system with transport lag. From the previous approximation problem we know how to handle e-sTD by using a Pade approximation that yields a rational function realized by a ladder network. For the controller of this system we require a different type of model. We can write

$$\frac{K_{c}(T_{r}s + 1)}{T_{r}s} = K_{c} \left(1 + \frac{1}{T_{r}s}\right)$$
 (7:17)

Now we use the model shown in Fig. 7.6 where V7 and I2 are dependent on the error signal and I1 is dependent on the current through L1. The first three elements model the  $\frac{1}{T_r s}$  term while the fourth element accounts for the unity term. The rest of the model poses no new problems.

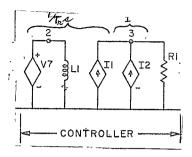


Fig. 7.6 Controller Circuit Model

To be specific then we are given the transfer function of the plant

$$G(s) = \frac{K_1 e^{-sT}}{(T_1 s + 1)(T_2 s + 1)(T_3 s + 1)}$$
 (7.18)

where

$$K_1 = 1.0$$

 $T_1 = 13.1 \text{ min}$ 

 $T_2 = 11.1 min$ 

 $T_2 = 0.5 \text{ min}$ 

 $T = 9.5 \min$ 

To obtain the unit step response we must determine the controller gain  $K_c$  and the reset time  $T_r$ . From [LU 1] we have the experimental results obtained with an analog computer. This is shown in Fig. 7.7 where the key response characteristics are labeled and the controller parameters used by Lupfer and Oglesby are indicated.

Following Eisenberg [EI 2] we can restate the design problem as: Choose values of controller gain constant  $K_c$  and reset time  $T_r$  to yield an output time domain response with

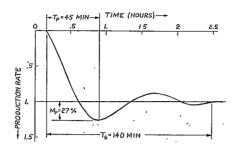
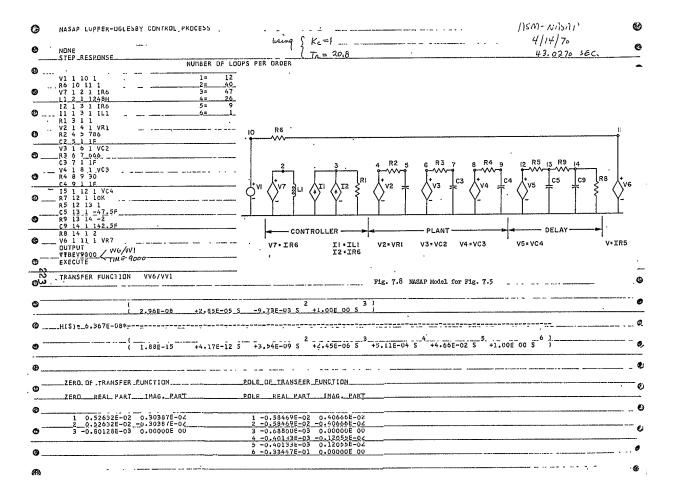


Fig. 7.7 Reactor process; response to unit step input,  ${\rm K_C}$  = 1.0 and  ${\rm T_r}$  = 20.8 min.

the characteristics of Fig. 7.7. Specifically, it is desired that (1) the peak overshoot  $M_p=27\%$ , (2) the time to reach a peak  $T_p=45$  min (where the output response begins after the initial T=9.5 min delay), and (3) the time for the response to reach 2% of the steady-state value  $T_S=140$  min.

At this point we do not have to reformulate the system transfer function as in [EI 2] but simply obtain the NASAP model shown in Fig. 7.8.

Finally we obtain the unit step response using NASAP. Compare this output Fig. 7.9 with that given in Fig. 7.7. This ability to handle transport lag considerably broadens the range of aerospace control problems that can be assisted by the use of NASAP. To permit detailed comparisons Fig. 7.9a is based on  $K_c=1$  and  $T_r=20.8$  min. while Fig. 7.9b is a rerun of this example using the values  $K_c=0.9$  and  $T_r=21.9$  min. taken from [EI 2].



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	0.1800E 04_ 0.1980E 04	0.81763464E 00
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·	2 0.526:46-02 -0.30367E-02 4 -0.47543E-	-03 0.11591E-02	20 7.96 1	
ම	3 -0.76104F-03 0-00000E 00 5 -0.61755b	-03 0.00000E 00 -01 0.000.0E 00		

STEP RESPUNSE FUNCTION . "	STEP RESPON	5Ē	
F(T) = .	TIME	VV6/VV1	
	0.0000E 00	-0.95367432b-06	
(-0.5815E-02 J 0.3987E-02 ) T	0.1800E 03	0.45130849E-02	
(-0.1012E 00 J 0.5839E-01 ) E	0.3600E 03 0.5400E 03	-0.25043488E-02	
(-0.5815E-02' J-0.3987E-02 ) T	0.7200E 03	U.13525188t-01	
(-0.10:26 CV J-0.58396-01 ) E	0.90001 03	0.662823321-01	
1-0,10122 00 0-0,30572 01 / 2	0.1080£ 04	0.14/36/845 00	4
(-0.4754E-03 J-0.1159E-02 ) T	, 0.126UE 04	0.24952/22E 00	
(-0.2453E 00 J-0.5323E 00 ) E	0.1440£ 04	0.365115648 00	,
(-0.4754E-03 J 0.1159E-02 ) T	0.1620E 04 0.1800E 04	0.48707902E 00 0.60921687E 00	
(-0.2453E 00 J 0.5323E 00 ) E	0.19805 04	0.726283431 00	
(-0.24756 00 3 0.5568 00 7 2	0.2160E 04	0.8340547/E 00	
(-0.6175E-03 J 0.0000E 00 ) T	0.23406 04	0.92936033E 00	····
. (-0.3038E 00 J-0.1050E-06 ) E	0.2520E 04	0.10100660E 01	•
	0.2700E 04	0.10750170E 01 0.11239424E 01	
(-0.30344E-01 J 0.0000E 00 ) T	0.2880E 04 0.3060E 04	0.11239424E 01	
(-0,3635E-02 J 0,7430E-10 ) E	0.3240E 04	0.117628578 01	
( 0.0000E 00 J 0.0000E 00 ) T	0.34206 04	0.11823950= 01	peak at 18,2% 57 min
( 0.1000E 01 J 0.6701E-06 ) E	0.3600E 04	0.117/56946 01	(3420 pec)
	0.378UE 04	0.11639090E 01	(3420 ALC.,
	0.39601 04	0.114357855 01	
	0.4140E 04 0.4320E 04	0.11187010E 01 0.10912590E 01	
	0.4500t 04	0.106303506 01	•
N	0.46806 04	0.10355549E 01	- 07
77	0'.4860F 04	0.101606035 01	2% at 4770 sec.
	0.5040E 04	0.58/49/5/6 00	,
	0.5220E 04	0.96851933E 00	
•	0.5400E 04 0.5580E 04	0.9535027/L 00 0.9425/486E 00	
	0.5760E 04	0.935047131 00	
	0.5940E 04	0.932453d1E 00	
	0.61201 04	0.93259305L 00	
	0.63UOE 04	0.93556798E 00	
	0.64BUF 04	0.94082105E 00	•
	0.6660F 04 0.6840E 04	0.947/781/E 00 0.95587045E 00	·,
	0.8840E 04	0.96456379t 00	
	0.720UE 04	0.97337794E 00	
,	0.7380L 04	U.98190069E 00_	
,	0.7560E 04	0.98979634E 00	
	0.77406 04	0.99580966E 00	
	0.7920E 04 0.8100F 04	0.10027647E 01 0.10075626E 01	
·	0.8180F 04	0.101117135 01	
•	0.84601 04	0.101361656 01	
	0.86408 04	0.10149803E OL	
	0.8820E 04	0.10153/23E 01	
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# VIIC. EXAMPLE SHOWING NASAP LIMITATION

We now present an active filter circuit which illustrates a flowgraph of great complexity and demonstrates some NASAP limitations. In particular the fact that it may not be sufficient that the user be judicious in the specific tree he allows the NASAP program to select. In Fig. 7.9 which is identical to Fig. 2.16 in [HU 1] is shown the 28-element NASAP circuit diagram of this Hutton problem. The input voltage VI is fed through a low-pass tee-network to the base of a transistor which is part of a twotransistor differential amplifier. The output voltage of this differential amplifier is connected directly to the base of a simple common emitter transistor stage. The voltage at the collector of this transistor, which is also the output voltage of the circuit, is fed back through an RC twin-tee network to the base of the other transistor in the differential amplifier. Each of these three transistors is represented in Fig. 7.9b by the h-parameter equivalent circuit with  $h_{1,2}=0$  and with a capacitor  $(C_2,\ C_3,\ C_7)$  connected between the base and collector terminals. This capacitance is included to take into account the frequency characteristic of the transistor.

The NASAP input listing used by Hutton is reproduced as Fig. 7.10.

There all 17 of the resistors are listed first and followed by the seven capacitors, in numerical sequence. With this listing, the NASAP tree selection algorithm selects as branches of the tree, the elements in the following order; V1, R17, C1, C2, C3, C4, C6, C7, R4, R5, R8, R15. This particular tree generates a flowgraph possessing a total number of loops of all orders of 2,440,105 a very complicated flowgraph indeed. As noted by Hutton, 10 minutes of execution time were required on the UNIVAC 1108.

Utilizing one of the options discussed in Chapter II, a tree can be selected to yield a flowgraph with considerably fewer loops. Seven of the

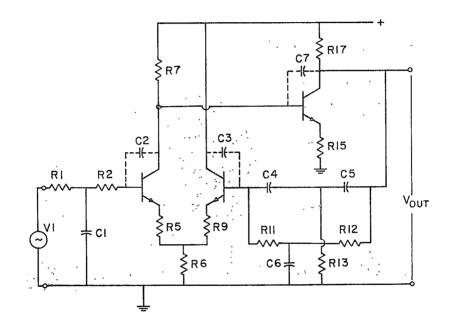


Fig. 7.9a Active Filter Circuit for Hutton Problem (Circuit 6)

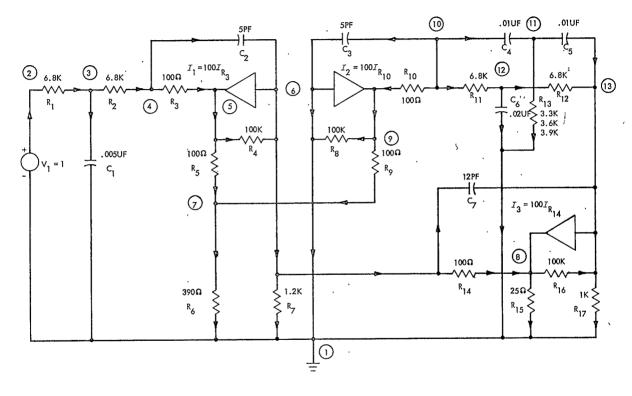


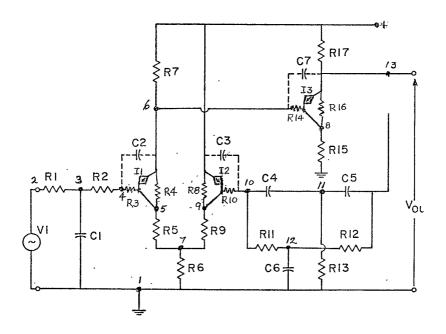
Fig. 7.95 Hutton Problem

```
NASAP
                               4/9/68
R1 2 3 6.8k
                                                                                . 51.70
R2 3 4 6.8K
                                                             NUMBER OF LOOPS PER ORDER
R3 4 5 100
R4 5 6 100k
                                                                                2 20
R5 6 7 140
                                                                       696
86 7 1 390
                                                                2=
                                                                      8969
R7 6 1 1.28
                                                                3= 1 52922
R6 9 1 100K
                                                                4= 105371
R$ 9 7 100
                                                                5= 419756
R10 10 9 100
                                                                b= 628827
K11 10 12 6.8K
                                                                7=
                                                                    616324
R12 12 13 5.8K
                                                                   380754
R13 11 1 3.6K
                                                                9= 138488
R14 6'8 100
                                                               10=
                                                                   26132
R15 8 1 25
                                                               11=
                                                                   -1896 --
R16 8 13 100K
R17 13 1 1K
C1 3 1 5UF
C2 4 6 .0050F
C4 10 1 .005UF
C4 10 11 10UF
C5 11 13 10UF
Cb 12 1 20UF
C7 6 13 .012UF
Vi 1 2 1.
II 6 5 100 IR3
12 1 9 100 TR10
I3 13 8 100 TR14
OUTPUT
VR17/VV1
FREQ -1 4 .1
TIME .005
EXECUTE
                   VR47/VVI
KANDER FUNCTION
                    .16+17
F(S)= .666+06*---
                               2 3 4 5 6 7)
+ .69+21 5 - .68+20 S - .60+19 S - .11+18 S - .38+13 S + .91+07 S + .10+01 S )
                    .11+23
```

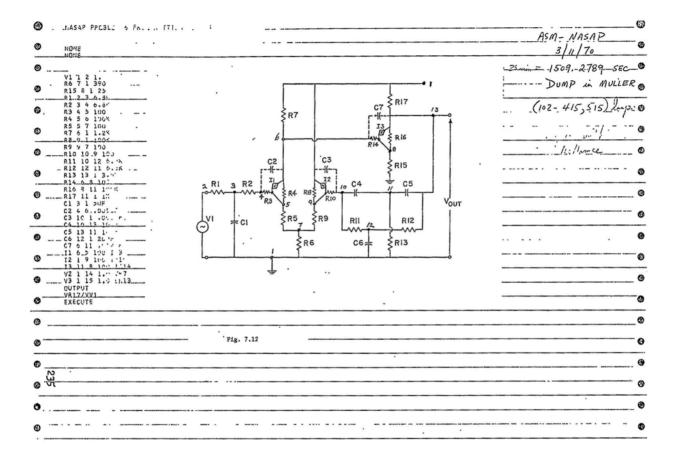
elements (namely, V1, R17, C1, C3, C6, R8, R15) in the above described tree are connected to the node numbered 1 in Fig. 7.11. However, three resistors, R6, R7, and R13 are also connected to node 1. If these three elements can be made branches of a tree which also contains the seven elements from the tree selected by Hutton, then ten of the twelve necessary tree branches will be connected to a common node. Such a tree with a definite star-like structure should yield a flowgraph with fewer loops. We shall now indicate how R6, R7, and R13 can be selected as tree branches and which branches of the original Hutton tree must be removed to make way for these resistors.

The resistor R7 forms a closed path with the original tree branches C7 and R17. Since the voltage across R17 is the specified output variable, R7 will become a tree branch only if C7 can be removed from the tree. This is easily accomplished by adding a dummy voltage source dependent on the voltage across R7. Likewise the resistor R13 forms a closed path with the original tree branches C3 and C4. Since C3 is connected to node 1, we wish to make R13 a tree branch in place of C4. A dummy voltage source dependent upon the voltage across R13 easily accomplishes this by making R13 a type 2 element instead of a type 4 element (see description of tree selection algorithm). Finally R6 can be included in the list of tree branches by making it the first resistor described in the NASAP input listing. With R6 in the tree, either R4 or R5 must be removed from the tree. The choice is easily made by noting that the co-tree element R3 will form a closed path with R4 and C2 when R4 is a tree branch. On the other hand, with R5 as a tree branch, R3 will form a closed path with R6, R7, R5 and C2. Hence R4 should remain as a tree branch. This is achieved by having R4 precede R5 in the NASAP input list.

The revised NASAP input listing that yields a tree with 10 elements connected to the same node is shown in Fig. 7.12. The controlled sources V2



·Fig. 7.11 Alternative NASAP Model for Hutton (compare Fig. 7.9)



and V3 are the dummy voltage sources necessary to include R7 and R13 in the tree selected by NASAP. With these 2 elements included, there are 30 elements in the equivalent circuit (NOTE: 30 elements are the maximum number of elements that can be used on the RCA Spectra 70 and IBM 360 machines because of their 32 bit computer words). Note in Fig. 7:12 that the flowgraph generated by this new tree contains 415, 515 loops of all orders. Thus a saving of over 2 million loops has been achieved by careful selection of the tree. The subsequent execution time was 25 minutes on the Spectra 70/46 (equivalent to approximately 3 minutes on the IBM 360/75). Note also the difference between the transfer function found by use of the original Hutton tree (Fig. 7:10) and that found by use of the tree described here (Fig. 7:12). The extra 2 million loops results in considerable error in the coefficients of the transfer function, see the discussion in [SE 1]. Note in Fig. 7.12 that only the zeros of the transfer function are given. Due to excessive floating point overflow, the MULLER (root-finding) subroutine was unable to determine the poles of the transfer function.

Through the cooperation of Prof. Alan B. Machee the Hutton problem was run using CIRAN (a program based on state variables) on the University of Michigan IBM 360/67 computer. The impedances were scaled by  $10^{-3}$  and frequency  $10^{-6}$ . The circuit was found to exhibit a pair of dominant conjugate complex poles near 2.4 KHz. For a  $\pm$  10% change in the value of R13 the Q of this pole ranged from 7.5 to 20. The fact that these three analyses took only 12.13 seconds of CPU time indicates a severe limitation of NASAP for this class of problems.

In Fig. 7.13 the compensation is seen to consist of two identical RC lag network. The transfer function of the RC lag network is

$$\frac{\frac{1}{RC}}{S + \frac{1}{RC}} \quad \text{or} \quad \frac{G}{S + G}$$

The parameter G, the RC lag network pole, is chosen different from all plant poles, usually farther inside the left half plane than any pole of the desired system.

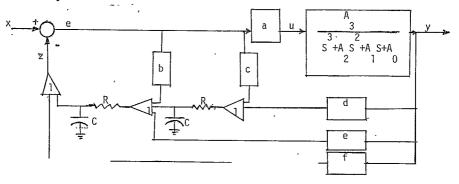


Fig. 7.13 Compensated Third Order Control System

Fig. 7.14 is equivalent to Fig. 7.13 with respect to the transfer function involved.

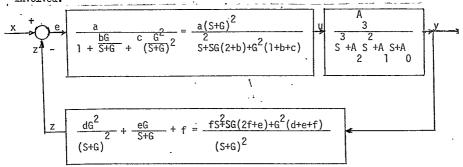


Fig. 7.14 Equivalent Feedback Control System Representation for Fig. 7.13

The closed-loop transfer function for y/x shown in Fig. 7.14 is

$$\frac{y}{x} = \frac{\frac{a(s+g)^{2}A_{3}}{\sqrt{(s^{2}+sg((2+b)+g^{2}(1+b+c)))(s^{3}+A_{2}s^{2}+A_{1}s+A_{0})}}}{\frac{aA_{3}(fsz+g((2f+e)s+gz(d+e+f))}{(s^{2}+sg((2+b)+g^{2}(1+b+c))(s^{3}+A_{2}s^{2}+A_{1}s+A_{0})}}$$
(7.21)

Equation (7.20) for the desired system, when multiplied top and bottom by  $(S+G)^2$  becomes

$$\frac{y}{x} = \frac{B_3(S+G)^2}{s^5 + (B_2 + 2G)S^4 + (B_1 + 2GB_2 + G^2)S^3 + (B_0 + 2GB_1 + G^2B_2)S^2 + (G^2B_1 + 2GB_0)S + G^2B_0}$$
(7.22)

This equation can be compared termwise with (7.21) after it has been rewritte to clear fractions. Thus we find that  $aA_3 = B_3$  and successively

$$b = \frac{(B_2 - A_2)}{G}$$
 where G is positive.

$$c = \frac{(B_1 - A_1) + (G - A_2) (B_2 - A_2)}{G^2}$$
 with G to positive.

$$f = \frac{(B_0 - A_0) + (B_1 - A_1)(2G - A_2) + (B_2 - A_2)((G - A_2)^2 - A_1)}{B_3}, B_3)/2$$

$$c = \frac{(B_1 - A_1)(-3G^2 - A_1 + 2GA_2) + (B_2 - A_2)(-2G(G - A_2)^2 + A_1A_2 - A_0)}{GB_3}$$

and finally

$$d = \frac{(B_1 - A_1)(G^3 - G^2A_2 + GA_1 - A_0) + (B_2 - A_2)(G^2A_1 + A_0A_2 - GA_0 + G^2(G - A_2)^2 - GA_1A_2)}{G^2G_3}$$
(7.23)

## VIID EXAMPLE INVOLVING LUENBERGER OBSERVER

For the last problem we consider an application of modern control theory based on state variables to show the versatility of NASAP. In particular we use the Luenberger observer method to implement compensation for a control system situation in which all the states of the system are not measurable.

For present purposes it is sufficient to note that the Luenberger observer [LU 1] is a device which constructs an estimate of the system state vector based upon the available system inputs and outputs. Then, based upon the reconstructed state vector, simple matrix algebra manipulations can be utilized to obtain estimates of the missing states or a combination of the missing states.

Luenberger has shown that for an n-th order system with m measureable states, the order of the required observed need only contain n-m poles. Furthermore these pole locations are arbitrary as long as they are different from the eigenvalues of the system matrix.

The Luenberger observer accomplishes the desired result by adding dynamics in the feedback path of the control system.

This theory suggests a unique form for general compensation of third order systems wherein the designer can place the closed-loop poles at any desired location. This development is adapted from Newman [NE 2].

The open loop descriptions of the control system shown in Fig. 7.13 is

$$\frac{y}{u} = \frac{A_3}{s^3 + A_2 s^2 + A_1 s + A_0}$$
 (7.19)

For convenience the desired closed-loop system transfer function is expressed as

$$\frac{y}{x} = \frac{\frac{y}{B_3}}{s^3 + B_2 s^2 + B_1 s + B_0}$$
 (7.20)

These six equations define unique values for the symbols a, b, c, f, e, and d respectively.

It is worth noting [NE 2] that this method of general system compensation may be extended to higher order systems. An N-th order system will require a string of N-1 RC lag networks. Each lag network is driven by the signal e and the signal y, both passing through gain blocks as in Fig. 7.13. The z signal is formed by adding the output of the string and a signal equal to fy, as in Fig. 7.13. The a block is used in cascade with the plant as in Fig. 7.13.

It is found easier to design compensators for plant transfer functions with numerator polynomials by reducing the coefficients in the equations to numbers, instead of trying to derive the general relationship.

For an illustrative example, we consider the open loop and desired closed loop transfer functions for the control system in Fig. 7.13.

Open Loop System

$$\frac{y}{u} = \frac{A_3}{s^3 + A_2 s^2 + A_1 s + A_0} = \frac{10}{s(s+1)(s+10)}$$
 (7.24)

Closed Loop System (Desired)

$$\frac{y}{x} = \frac{\frac{B_3}{S^3 + B_2 S^2 + B_1 S + B_0}}{\frac{B_3}{S^2 + B_1 S + B_0}} = \frac{\frac{5}{5} \cdot (\frac{5}{S + 5}) \cdot (\frac{5}{S + 20})^2}{\frac{5}{S + 20}}$$
(7.25)

Following the procedure outlined above, we determine the constants a, b, c, d, e, f, as listed.

The parameter G, was chosen as twenty (G = 20) which is different from all plant poles.

Having thus specified the Luenberger observer we need the corresponding electric circuit model for the compensated third order control system. This model is shown in Fig. 7.15. A NASAP run was made for the step response of this model. We note that the transfer function shows six critical frequencies near s=-20; two zeros and four poles. The step response shows a slight steady state error.

Execution time on the RCA Spectra 70/46 was 42.86 seconds. A comparison run was made of this third-order compensator system using CSMP (Continuous System Modeling Program) on the IBM 360/75. The CSMP step response for this control system checked very closely except that the execution time was 32 seconds (22 seconds CPU). This represents a significant cost advantage for NASAP since the 360/75 is faster by a factor of approximately 8 over the Spectra 70/46. The NASAP printout is shown in Fig. 7.16.

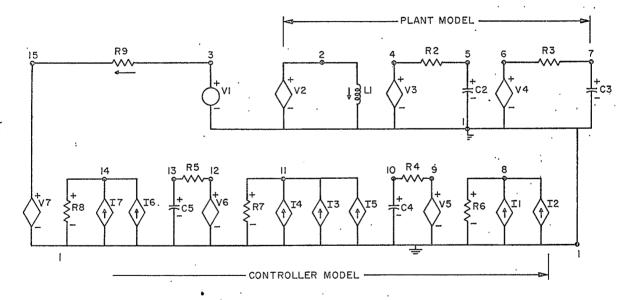
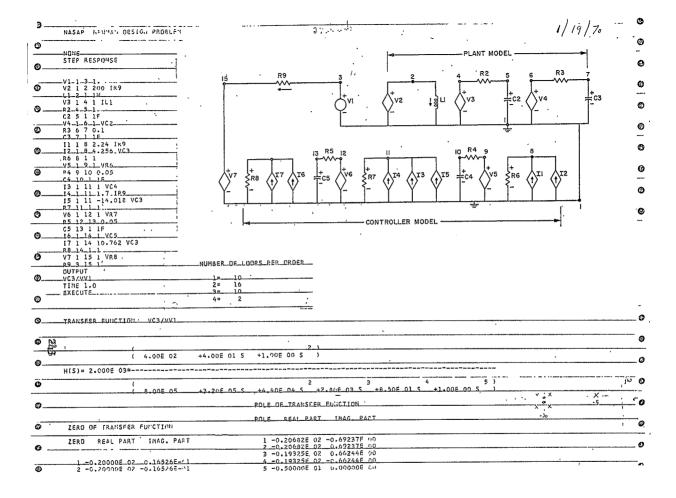


Fig. 7.15 NASAP Model for Third Order Control System in Fig. 7.13



		TIME	VC3/VV1	
<b></b> F-(T)		0.0000E 00	c.26226n44E-n5	
	(-0.2068F 02 J-0.6924F 00 )	0.2000E-01		
	(-0.1041E 01 J 0.1232F 01 ) E	0.4000E-01	(+1377R2A9E=01	
D		0.6000E-01	0.73712727-01 0.737137236-01	
	(-0.2068F 02 J 0.6924E 00 )	0.1000E 00	4.11717729E 00	
	(-0.1041E-01_J=0.1232E-01_) E	0.1200F 00	0.167417278 00	
<b>3</b>	(=0.1932F_02_J_0.6624F_00_)		0.22115954E 00	<u></u>
	0.1430E 01 J-0.120HE 01 ) E	Q.1600E 00	0.27627426F 00	
<b>2</b> 5		0.1500E.00	2.331117635 00	
	(-0.1932E 02 J-0.6624E 00 )	0.2000E 00	C.384495'2E 00	
	(-0+1430E-01-4-0+1203E-01-)-E	0.2200E.00	0.48388535E 00	
₿		0.2400E 00	0.52909475E 00	
	(-0.5000€ 01 ↓ 0.0000€ 00.)	0.2800E 00	0.57109714F 00	
_	(-0.1776E 01 J 0.4791E-08 ) E	0.300VE. 00	0.60989457E_00	
<i>7</i>	( 0.0000E 00 J 0.0000E 00 )		0.645568195 00	
	( 0.9994E 00 J=0.1198E-08 ) E	0.3400E_00_	0.67825329E.00	
A	(	0.3600E 00	0.70811856E 00	
		0.3800E 00	0.73534657E 00 0.76012969E 00	
		0.4000E 00	0.78265649800	
<b></b>		0.4200E 00	0.803112:9E 00	
		0.4600E_00	0.821671556.00	
~ <del></del>		0.4800E 00	0.83950056E 00	
<b>T</b>		0.5000E.00	0.353753.3F 00	
		0.5200E 00	0.86757113E 00	
<b>6</b> N		0.5400E.00	C.48008666F_QQ	
E	•	0.5600E 00	0.39141941E 00	
4		0.5800E.00	0.9107679676 00 0.91096765E 00	
€		0.6200E 00	0.919374536 00	
		0.6400E 00	0.926983366 00	
_		0,6600E_00	0.93386942E_00	
•		0.6800E 00	0.94010109E 00	
		0.7000E 00	2.94574.352E_30	
•		0.7200E 00	0.95084363F 00	
		0.7400E 00	0.95546150E 00 0.95954019E 00	
_		0.7603E 00 0.7800E 00	0.75347173E 00	
Ø		0.8000E 00	0.96634259E 00	
		0.8200E_00	0.969938464_00	
•		0.8400E 00	0.972739:28 00	
•		0.8600E 00	0.97527456E 30	
		0.8800E 00	0.97756815F 00	
<b>0</b>		0.9000E 00	0.97964346E 00 0.98152131E 00	
		0.9200E 00 0.9400E 00	0.983220528 00	
		0.9600F 00	0.98475796E 00	
Ψ.		0.9800E 00	C.98614913E 00	
		0.1000E 01	0.98740742E 00	
<b>6</b>				
•				
•				
0				

6	0.0000E 00		*********		90E-01_3.	********	9.0E=0.1_5.		90E-01_7.	90E=018.	90E-01 9	.90E-01	
		. *		:		:	<u> </u>	:	:		<del> </del>	: .	
ම		* *	:	:	:	:	I		:	-	:	•	
<b>3</b>	1.0000E=01		*	•	•.•.•.•.•.• •.• •		L.s	**************************************			•	•	<del></del>
	-	-:		* *	<del> </del>	:	<u> </u>		•	:	:	:	
9	2.0000E-01	-:			* * * * * *		I					• •	
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<i>9</i>	3.0000E=01		•	•		•	I	*	*.*.*.*.*.*.*.*.*.*.*.*.*.*.*			•	
3			:			:			*	•	•	•	
~	4.0000E-01								*			:	
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9					:					*	•	•	
25	5-0000E=01	•	•	•	•	•		,		*	•	•	
J		-:		:						:	*		
9	6.0000E-01	·······	. <del></del>	:						<del> ,</del>	*	•	
20		:		:	:	:					*	•	
<i></i>	7.0000E-01					:					. *	•	
9			·		,	• •.•.•	*				*		****
		<del>-:</del>		:	:	•					*	•	
J	8.0000E-01										*.	•	
<b>3</b>						•					. *		
b	9.0000E-01								,				
	2.000021-01	•	•	•	•				22/32/22		*	:	
<b>a</b>				:		:			·			*	
3	1.0000E 00						•••••					*	
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9 ~~													

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### APPENDIX A

### STEP AND RAMP RESPONSE CAPABILITY FOR NASAP

The algorithm used by NASAP to determine the impulse response of a circuit can be easily extended to find the step and ramp response. Listed below are the modifications that are necessary to accomplish this. Note that if, for example, both the impulse and step responses are required for a particular circuit, the problem must be executed twice.

To the COMMON/FREQ/ cards of subroutines NASINP and BODE must be added: .KRESP

The following additions must be included in subroutine NASINP. After card 1010, three cards must be added:

```
Go to 3
824 WRITE (6, 117)
                                                                               1011
117 FORMAT (35H INCLUDE TYPE OF TIME RESPONSE CARD)
                                                                               1012
                                                                               1013
After card 1180, nine cards must be added:
READ (5,101) INLST
                                                                               1181
WRITE (6,107) INLST
                                                                               1182
KRESP = 1000
                                                                               1183
IF (ICHAR (INLST(1)). EQ. 49. AND ICHAR (INLST(2))EQ. 54) KRESP = 1
                                                                               1184
IF (ICHAR(INLST(1)). EQ. 55. AND ICHAR(INLST(2)).EQ. 56)KRÉSP = 1-
IF (ICHAR(INLST(1)). EQ. 62) KRESP = 2
                                                                               1185
                                                                               1186
IF (ICHAR (INLST(1)). EQ. 59 AND ICHAR (INLST(2)).EQ.41 KRESP = 3
                                                                               1187
IF (KRESP. EQ.1000) GO TO 824
                                                                               1189
WRITE (6,116)
                                                                               1189A
     The following changes must be made in INV:
     Change card 14930
     From DIMENSION F(100), T(100), COE(2)
     To DIMENSION F(100), T(100), COE(2), TYPE (2,3)
     Change card 14990
     From WRITE (6,50)
    To WRITE (6,50) (TYPE(J, KRESP), J=1,2)
     Change card 1500
     From 50 FORMAT (26H1 IMPULSE RESPONSE FUNCTION //7H F(t)=)
     To 50 FORMAT (1H1, 2A4, 18H RESPONSE FUNCTION //7H F(t)=)
     Change card 15280
     From WRITE (6,40) TRNS, (T(K), F(K), K=1, 51)
     To WRITE (6,40) (TYPE (J,KRESP), J=1,2), TRNS, (T(K), F(K), K=1, 51)
     Change card 15290
     From 40 FORMAT(17H1 IMPULSE RESPONSE // 5H TIME, 18X, 10A1/(E12,4,E23.8))
To 40 FORMAT(1H1,2A4, 9H RESPONSE // 5H TIME, 18X, 10A1/(E12.4,E23.8))
     Change card 15300
```

From WRITE (6.41)

```
To WRITE (6,41) (TYPE(J,KRESP), J=1,2)
Change card 15310
From 41 FORMAT (1H1, 45X, 17HIMPULSE RESPONSE, /)
To 41 FORMAT (1H1, 45X, 2A4, 9H RESPONSE, /)
```

The following additions must be included in subroutine AINIV. After card 14930, two cards must be added:

DATA TYPE /4HIMPU,4HLSE, 4HSTEP, 4H ,4HRAMP, 4H 14931 COMMON/FREQ/THI, FEQ (3), CC,Q, KRESP

After card 15060, twelve cards must be added:

76	Go To (77,76,78,76), KRESP IAD2=IAD2+1 RootR (IAD2,2) = 0 RootI (IAD2, 2) =0	1:5061 1:5062 1:5063 1:5064
78	Go To 77 IAD2=IAD2+1 RootR(IAD2,2) = 0 RootI(IAD2,2) = 0.001	15066 15067 15068 15069
	IAD2= IAD2+1 RootR (IAD2,2) = 0	15069A 15069B 15079C
77	RootI (IAD2,2) = -0.001 CONTINUE	15069E

When the above modifications are incorporated in the NASAP program package, the only change from a user's point of view is that he <u>must</u> include one card, <u>immediately</u> following the NASAP PROBLEM card, on which is punched (beginning in column one) one of the four following comments:

NO RESPONSE IMPULSE RESPONSE STEP RESPONSE RAMP RESPONSE

The choice of which comment is to be used depends on what type of time response, if any, is desired. In actuality, only the first two letters of each of the above comments are really necessary. In cards 1181 through 1189A of subroutine NASINP, the program reads the card after the NASAP PROBLEM card and then prints it. If the letters in columns one and two are on R and a A respectively, the time response variable KRESP is set equal to 3. If there is an N in column one and an O in column two, KRESP thenis set equal to 1. If there is an I in column 1 and an M in column two KRESP is set equal to 1. If there is an S in column one, KRESP then has a value of 2. If the program encounters none of the above letter combinations on the second input card, it will print out the error message given on card 1013 and about the job.

The variable KRESP is used in subroutine INV to select the proper elements of the two-dimensional matrix TYPE such that the headings of the printout of the time response agree with the information on the second input card. Thus, if a step response is desired(KRESP=2), the elements in the second column of TYPE will be printed. The variable KRESP is also used in INV to select the proper poles that must be included with the transfer function poles to yield the particular time response. On lines 15061, if KRESP=1(impulse response), the

### APPENDIX B

Suggested Revision that combines Subroutines SENS & SENSS of NASAP 69/I into a single shorter Subroutine SENSS

In the University of Pennsylvania monthly report for July 1969, the possibility was mentioned of eliminating subroutine SENS by using the results of the calculations of subroutine SENSS (namely  $\mathbf{S}_{X}^{H}$ ) and the four equations.

$$\begin{aligned} s \stackrel{|H|}{X} &= \text{Re } s_X^H \\ s_X^{\phi} &= \frac{1}{\phi} \cdot \text{Im } s_X^H \\ s_X^{\text{Re } H} &= \text{Re } s_X^H - \left(\frac{\text{Im} H}{\text{Re} H} \cdot \text{Im } s_X^H\right) \\ s_X^{\text{Im} H} &= \text{Re } s_X^H + \left(\frac{\text{Re} H}{\text{Im} H} \cdot \text{Im } s_X^H\right) \end{aligned}$$

where  $S_X^H$  = Re  $S_X^H$  + j Im  $S_X^H$ 

and  $H(jw) = |H| e^{j\phi} = Re H + j Im H.$ 

This can be accomplished by making the following additions to subroutine SENSS. After card 17000, add the following 3 cards: cards 15370, 15380, and 15390 from SENS. After card 17030, remove cards 17040, 17050, and 17060 and add the following 6 cards:

COMMON/LOOPS/DM(100), PHIH(250), LOGF(250), LGBSNS(250), ABSH(250),

1 ABSENS(250), REH(250), IMH(250), PHISNS(250), CSENS(250), SENSRE(250), card 15440 from SENS

card 15450 from SENS with DUML(288) changed to DUML(38)

```
card 15490 from SENS
      card 15500 from SENS with the addition of .LGBSNS.
      After card 17110, add the following 2 cards: cards 15520 and
15530 from SENS.
     After card 17540, add the following 39 cards:
      card 15540 from SENS
      card 15550 from SENS with 1HO changed to 1H1.
      card 15560 from SENS
     Do 802 I=1, NITR
      Z = 10.** LOGF(I)
     RE = REAL (CSENS(I))
     AIM = AIMAG (CSENS(I))
     CALL QZERO (REH,I,SENSRE,I,GLAG, $81, $82)
  81 SENSRE (I) = RE - (IMH(I)/REH(I)) * AIM
  82 CALL CZERO (IMH,I,SENSIM,I,GLAG, $83, $84)
  83 SENSIM (I) = RE + (REH(I)/IMH(I)) * AIM
  -84 SENSBS (I) = RE
  97 CALL QZERO (PHIH, I, SENSFI, I, GLAG, $98, $99)
  98 \text{ SENSFI (I)} = (180./PI) * (AIM/PHIH(I))
  99 WRITE (6,180) LOGF(I), Z, SENSRE(I), SENSIM(I), SENSBS(I), SENSFI(I)
 180 FORMAT (5x,6(E 15.7, 2x))
 802 CONTINUE
     cards 16110 thru 16320 from SENS (22 cards)
```

The following 10 cards of SENSS must be slightly modified:

(NOTE - etc. means that the rest of the card remains unchanged).

Change card 17120

from WRITE(6,100)

to WRITE(6,200)

card 17130

from 100 FORMAT(1H1, etc.

to 200 FORMAT(1HO, etc.

card 17390

from 96 WRITE(6,105) etc.

to 96 WRITE(6,205) etc.

card 17400

from 105 FORMAT etc.

to 205 FORMAT etc.

card 17450

from WRITE(6,102)

to WRITE(6,202)

card 17460

from 102 FORMAT etc.

to 202 FORMAT etc.

card 17470

from WRITE(6,103) etc.

:0 WRITE(6,203) etc.,

```
card 17480
        from 103 FORMAT etc.
        to
             203 FORMAT etc.
     card 17520
        from WRITE(6,102)
             WRITE(6,202)
        to
     card 17530
        from WRITE(6,103) etc.
             WRITE(6,203) etc.
Finally in BODE remove card 13510. In SPLOT the following 2 minor
modifications are needed:
     On card 16670
        change ARR(1000), DUMM2(1750)
           to ARR(750) , DUMM2(2250)
     On card 16690
        change DUML(288)
           to DUML( 38)
```

These changes essentially delete cards 15570 thru 16100 from SENS.

The calculations in this block of cards are replaced by the Do-Loop

(labelled 802) given above. The remaining cards of SENS are then inserted into subroutine SENSS in the appropriate locations. On the RCA Spectra 70, the original version of SENS requires 4000 bytes of memory and the original version of SENSS requires 2540 bytes. However the suggested new version of SENSS requires 4392 bytes - thus realizing a saving of 2148

bytes. Enclosed is a listing of the new version of SENSS. Due to the use of a BCD coded program on a ERCDIC machine, the following symbols are equivalent:

Note that the printed output of the original SENSS now precedes , the printed output of the original version of SENS.